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(Draft) Technical Report on Standard Library Extensions

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1 General

[tr.intro]

- 1 This technical report describes extensions to the *C++ standard library* that is described in the International Standard for the C++ programming language [14].
- 2 This technical report is non-normative. Some of the library components in this technical report may be considered for standardization in a future version of C++, but they are not currently part of any C++ standard. Some of the components in this technical report may never be standardized, and others may be standardized in a substantially changed form.
- 3 The goal of this technical report is to build more widespread existing practice for an expanded C++ standard library. It gives advice on extensions to those vendors who wish to provide them.

1.1 Relation to C++ Standard Library Introduction

[tr.description]

- 1 Unless otherwise specified, the whole of the ISO C++ Standard Library introduction [lib.library] is included into this Technical Report by reference.

1.2 Categories of extensions

[tr.intro.ext]

- 1 This technical report describes four general categories of library extensions:
 1. New requirement tables, such as the regular expression traits requirements in clause 7.2. These are not directly expressed as software; they specify the circumstances under which user-written components will interoperate with the components described in this technical report.
 2. New library components (types and functions) that are declared in entirely new headers, such as the class templates in the <unordered_set> header 6.3.4.1.
 3. New library components declared as additions to existing standard headers, such as the mathematical special functions added to the headers <cmath> and <math.h> in clauses 5.2.1 and 5.2.2
 4. Additions to standard library components, such as the extensions to class `std::pair` in section 6.1.3.
- 2 The first three categories are collectively called *pure* extensions, and the last is called an *impure* extension. All extensions are assumed to be pure unless otherwise specified.
- 3 New headers are distinguished from extensions to existing headers by the title of the *synopsis* clause. In the first case the title is of the form “Header <foo> synopsis”, and the synopsis includes all namespace scope declarations contained in the header. In the second case the title is of the form “Additions to header <foo> synopsis” and the synopsis includes only the extensions, *i.e.* those namespace scope declarations that are not present in the C++ standard [14].

1.3 Namespaces and headers**[tr.intro.namespaces]**

- 1 Since the extensions described in this technical report are not part of the C++ standard library, they should not be declared directly within namespace `std`. Unless otherwise specified, all components described in this technical report are declared in namespace `std::tr1`. [Note: Some components are declared in subnamespaces of namespace `std::tr1`. —end note]
- 2 Unless otherwise specified, reference to other entities described in this technical report are assumed to be qualified with `std::tr1::`, and references to entities described in the standard are assumed to be qualified with `std::`.
- 3 Even when an extension is specified as additions to standard headers (the third category in section 1.2), vendors should not simply add declarations to standard headers in a way that would be visible to users by default. [Note: That would fail to be standard conforming, because the new names, even within a namespace, could conflict with user macros. —end note] Users should be required to take explicit action to have access to library extensions.
- 4 It is recommended either that additional declarations in standard headers be protected with a macro that is not defined by default, or else that all extended headers, including both new headers and parallel versions of standard headers with nonstandard declarations, be placed in a separate directory that is not part of the default search path.

1.4 Caveat**[tr.intro.caveat]**

- 1 **This is a draft. It's known to be incomplet and incorrekt, and it has some bad fomattting.**

2 General Utilities

[tr.util]

- 1 This clause describes basic components used to implement other library facilities. They may also be used by C++ programs.
- 2 The following subclauses describe reference wrappers and smart pointers, as summarized in Table 1.

Table 1: Utilities library summary

Subclause	Header(s)
2.1 Reference wrapper	<utility>
2.2 Smart pointers	<memory>

2.1 Reference wrappers

[tr.util.refwrap]

2.1.1 Additions to header <utility> synopsis

[tr.util.refwrp.synopsis]

```
namespace tr1 {
    template <class T> class reference_wrapper;
    template <class T> reference_wrapper<T> ref(T&);
    template <class T> reference_wrapper<const T> cref(const T&);
}
```

2.1.2 Class template reference_wrapper

[tr.util.refwrp.refwrp]

```
template <class T> class reference_wrapper {
public :
    // types
    typedef T type;
    typedef see below result_type; // Not always defined

    // construct/copy/destruct
    explicit reference_wrapper(T&);

    // access
    operator T& () const;
    T& get() const;

    // invocation
    template <class T1, class T2, ..., class TN>
```

```
    typename result_of<T(T1, T2, ..., TN)>::type
operator () (T1, T2, ..., TN) const;
};
```

- 1 `reference_wrapper`<`T`> is a `CopyConstructible` and `Assignable` wrapper around a reference to an object of type `T`.
- 2 `reference_wrapper` defines the member type `result_type` in the following cases:
 1. `T` is a function pointer, then `result_type` is the return type of `T`.
 2. `T` is a pointer to member function, then `result_type` is the return type of `T`.
 3. `T` is a class type with a member type `result_type`, then `result_type` is `T::result_type`.

2.1.2.1 `reference_wrapper` construct/copy/destruct

[tr.util.refwrp.const]

```
explicit reference_wrapper(T& t);
```

- 1 *Effects:* Constructs a `reference_wrapper` object that stores a reference to `t`.
- 2 *Throws:* Does not throw.

2.1.2.2 `reference_wrapper` access

[tr.util.refwrp.access]

```
operator T& () const;
```

- 1 *Returns:* The stored reference.
- 2 *Throws:* Does not throw.

```
T& get() const;
```

- 3 *Returns:* The stored reference.
- 4 *Throws:* Does not throw.

2.1.2.3 `reference_wrapper` invocation

[tr.util.refwrp.invoke]

```
template <class T1, class T2, ..., class TN>
typename result_of<T(T1, T2, ..., TN)>::type
operator ()(T1 a1, T2 a1, ..., TN aN) const ;
```

- 1 *Effects:* `f.get()(a1, a2, ..., aN)`
- 2 *Returns:* The result of the expression `f.get()(a1, a2, ..., aN)`

2.1.2.4 `reference_wrapper` helper functions

[tr.util.refwrp.helpers]

```
template <class T> reference_wrapper<T> ref(T& t);
```

1 *Returns:* reference_wrapper <T>(t)
 2 *Throws:* Does not throw.

```
template <class T> reference_wrapper<const T> cref( const T& t);
```

3 *Returns:* reference_wrapper <const T>(t)
 4 *Throws:* Does not throw.

2.2 Smart pointers

[tr.util.smartptr]

2.2.1 Additions to header <memory> synopsis

[tr.util.smartptrsynopsis]

```
namespace tr1 {
    // [2.2.2] Class bad_weak_ptr
    class bad_weak_ptr;

    // [2.2.3] Class template shared_ptr
    template<class T> class shared_ptr;

    // [2.2.3.6] shared_ptr comparisons
    template<class T, class U>
        bool operator==(shared_ptr<T> const& a, shared_ptr<U> const& b);

    template<class T, class U>
        bool operator!=(shared_ptr<T> const& a, shared_ptr<U> const& b);

    template<class T, class U>
        bool operator<(shared_ptr<T> const& a, shared_ptr<U> const& b);

    // [2.2.3.8] shared_ptr specialized algorithms
    template<class T>
        void swap(shared_ptr<T>& a, shared_ptr<T>& b);

    // [2.2.3.9] shared_ptr casts
    template<class T, class U>
        shared_ptr<T> static_pointer_cast(shared_ptr<U> const& r);

    template<class T, class U>
        shared_ptr<T> dynamic_pointer_cast(shared_ptr<U> const& r);

    template<class T, class U>
        shared_ptr<T> const_pointer_cast(shared_ptr<U> const& r);

    // [2.2.3.7] shared_ptr I/O
    template<class E, class T, class Y>
        basic_ostream<E, T>&
        operator<< (basic_ostream<E, T>& os, shared_ptr<Y> const& p);

    // [2.2.3.10] shared_ptr get_deleter
```

```

template<class D, class T>
D * get_deleter(shared_ptr<T> const& p);

// [2.2.4] Class template weak_ptr
template<class T> class weak_ptr;

// [2.2.4.6] weak_ptr comparison
template<class T, class U>
bool operator<(weak_ptr<T> const& a, weak_ptr<U> const& b);

// [2.2.4.7] weak_ptr specialized algorithms
template<class T>
void swap(weak_ptr<T>& a, weak_ptr<T>& b);

// [2.2.5] Class enable_shared_from_this
template<class T> class enable_shared_from_this;
}

```

2.2.2 Class bad_weak_ptr

[tr.util.smartptr.weakptr]

```

namespace tr1 {
    class bad_weak_ptr: public std::exception
    {
    public:
        bad_weak_ptr();
    };
}

```

- 1 An exception of type `bad_weak_ptr` is thrown by the `shared_ptr` constructor taking a `weak_ptr`.

`bad_weak_ptr();`

- 2 *Postconditions*: `what()` returns "tr1::bad_weak_ptr".
- 3 *Throws*: nothing.

2.2.3 Class template shared_ptr

[tr.util.smartptr.shared]

- 1 The `shared_ptr` class template stores a pointer, usually obtained via `new`. `shared_ptr` implements semantics of shared ownership; the last remaining owner of the pointer is responsible for destroying the object, or otherwise releasing the resources associated with the stored pointer.

```

namespace tr1 {
    template<class T> class shared_ptr {
    public:
        typedef T element_type;

        // constructors
        shared_ptr();
        template<class Y> explicit shared_ptr(Y * p);
    }
}

```

```

template<class Y, class D> shared_ptr(Y * p, D d);
shared_ptr(shared_ptr const& r);
template<class Y> shared_ptr(shared_ptr<Y> const& r);
template<class Y> explicit shared_ptr(weak_ptr<Y> const& r);
template<class Y> explicit shared_ptr(auto_ptr<Y>& r);

// destructor
~shared_ptr();

// assignment
shared_ptr& operator=(shared_ptr const& r);
template<class Y> shared_ptr& operator=(shared_ptr<Y> const& r);
template<class Y> shared_ptr& operator=(auto_ptr<Y>& r);

// modifiers
void swap(shared_ptr& r);
void reset();
template<class Y> void reset(Y * p);
template<class Y, class D> void reset(Y * p, D d);

// observers
T* get() const;
T& operator*() const;
T* operator->() const;
long use_count() const;
bool unique() const;
operator unspecified_bool-type() const;
};

// comparison
template<class T, class U>
bool
operator==(shared_ptr<T> const& a, shared_ptr<U> const& b);

template<class T, class U>
bool
operator!=(shared_ptr<T> const& a, shared_ptr<U> const& b);

template<class T, class U>
bool
operator<(shared_ptr<T> const& a, shared_ptr<U> const& b);

// other operators
template<class E, class T, class Y>
basic_ostream<E, T>&
operator<< (basic_ostream<E, T>& os, shared_ptr<Y> const& p);

// specialized algorithms
template<class T>
void swap(shared_ptr<T>& a, shared_ptr<T>& b);

```

```

// casts
template<class T, class U>
    shared_ptr<T> static_pointer_cast(shared_ptr<U> const& r);

template<class T, class U>
    shared_ptr<T> dynamic_pointer_cast(shared_ptr<U> const& r);

// get_deleter
template<class D, class T>
    D * get_deleter(shared_ptr<T> const& p);
}

```

2 `shared_ptr` is `CopyConstructible`, `Assignable`, and `LessThanComparable`, allowing its use in standard containers. `shared_ptr` is convertible to `bool`, allowing its use in boolean expressions and declarations in conditions.

3 [Example:

```

if(shared_ptr<X> px = dynamic_pointer_cast<X>(py))
{
    // do something with px
}

```

—end example.]

2.2.3.1 shared_ptr constructors

[\[tr.util.smartptr.shared.const\]](#)

`shared_ptr()`;

1 *Effects*: Constructs an *empty* `shared_ptr`.

2 *Postconditions*: `use_count() == 0 && get() == 0`.

3 *Throws*: nothing.

`template<class Y> explicit shared_ptr(Y * p);`

4 *Requires*: `p` is convertible to `T *`. `Y` is a complete type. The expression `delete p` is well-formed, does not invoke undefined behavior, and does not throw exceptions.

5 *Effects*: Constructs a `shared_ptr` that *owns* the pointer `p`.

6 *Postconditions*: `use_count() == 1 && get() == p`.

7 *Throws*: `bad_alloc` or an implementation-defined exception when a resource other than memory could not be obtained.

8 *Exception safety*: If an exception is thrown, `delete p` is called.

`template<class Y, class D> shared_ptr(Y * p, D d);`

9 *Requires*: `p` is convertible to `T *`. `D` is `CopyConstructible`. The copy constructor and destructor of `D` do not throw. The expression `d(p)` is well-formed, does not invoke undefined behavior, and does not throw exceptions.

- 10 *Effects:* Constructs a `shared_ptr` that *owns* the pointer `p` and the deleter `d`.
- 11 *Postconditions:* `use_count() == 1 && get() == p`.
- 12 *Throws:* `bad_alloc` or an implementation-defined exception when a resource other than memory could not be obtained.
- 13 *Exception safety:* If an exception is thrown, `d(p)` is called.
- ```
shared_ptr(shared_ptr const& r);
template<class Y> shared_ptr(shared_ptr<Y> const& r);
```
- 14     *Effects:* If `r` is *empty*, constructs an *empty* `shared_ptr`; otherwise, constructs a `shared_ptr` that *shares ownership* with `r`.
- 15     *Postconditions:* `get() == r.get() && use_count() == r.use_count()`.
- 16     *Throws:* nothing.
- ```
template<class Y> explicit shared_ptr(weak_ptr<Y> const& r);
```
- 17 *Effects:* Constructs a `shared_ptr` that *shares ownership* with `r` and stores a copy of the pointer stored in `r`.
- 18 *Postconditions:* `use_count() == r.use_count()`.
- 19 *Throws:* `bad_weak_ptr` when `r.expired()`.
- 20 *Exception safety:* If an exception is thrown, the constructor has no effect.
- ```
template<class Y> shared_ptr(auto_ptr<Y>& r);
```
- 21     *Requires:* `r.release()` is convertible to `T *`. `Y` is a complete type. The expression `delete r.release()` is well-formed, does not invoke undefined behavior, and does not throw exceptions.
- 22     *Effects:* Constructs a `shared_ptr` that stores and *owns* `r.release()`.
- 23     *Postconditions:* `use_count() == 1 && r.get() == 0`.
- 24     *Throws:* `bad_alloc` or an implementation-defined exception when a resource other than memory could not be obtained.
- 25     *Exception safety:* If an exception is thrown, the constructor has no effect.

**2.2.3.2 shared\_ptr destructor**

[tr.util.smartptr.shared.dest]

`~shared_ptr();`

- 1     *Effects:*

- If `*this` is *empty*, or *shares ownership* with another `shared_ptr` instance (`use_count() > 1`), there are no side effects.
- Otherwise, if `*this` *owns* a pointer `p` and a deleter `d`, `d(p)` is called.
- Otherwise, `*this` *owns* a pointer `p`, and `delete p` is called.

2 *Throws:* nothing.

### 2.2.3.3 shared\_ptr assignment

[tr.util.smartptr.shared.assign]

```
shared_ptr& operator=(shared_ptr const& r);
template<class Y> shared_ptr& operator=(shared_ptr<Y> const& r);
template<class Y> shared_ptr& operator=(auto_ptr<Y>& r);
```

1 *Effects:* Equivalent to `shared_ptr(r).swap(*this)`.

2 *Returns:* `*this`.

3 *Notes:* The use count updates caused by the temporary object construction and destruction are not considered observable side effects, and the implementation is free to meet the effects (and the implied guarantees) via different means, without creating a temporary. In particular, in the example:

```
shared_ptr<int> p(new int);
shared_ptr<void> q(p);
p = p;
q = p;
```

both assignments may be no-ops.

### 2.2.3.4 shared\_ptr modifiers

[tr.util.smartptr.shared.mod]

```
void swap(shared_ptr& r);
```

1 *Effects:* Exchanges the contents of `*this` and `r`.

2 *Throws:* nothing.

```
void reset();
```

3 *Effects:* Equivalent to `shared_ptr().swap(*this)`.

```
template<class Y> void reset(Y * p);
```

4 *Effects:* Equivalent to `shared_ptr(p).swap(*this)`.

```
template<class Y, class D> void reset(Y * p, D d);
```

5 *Effects:* Equivalent to `shared_ptr(p, d).swap(*this)`.

### 2.2.3.5 shared\_ptr observers

[tr.util.smartptr.shared.obs]

```
T * get() const;
```

1 *Returns:* the stored pointer.

2 *Throws:* nothing.

```
T& operator*() const;
```

```

3 Requires: get() != 0.
4 Returns: *get().
5 Throws: nothing.
6 Notes: When T is void, the return type of this member function is unspecified, and an attempt to instantiate it
renders the program ill-formed.

T * operator->() const;

7 Requires: get() != 0.
8 Returns: get().
9 Throws: nothing.

long use_count() const;

10 Returns: the number of shared_ptr objects, *this included, that share ownership with *this, or 0 when *this
is empty.

11 Throws: nothing.

12 Notes: use_count() is not necessarily efficient. Use only for debugging and testing purposes, not for production
code.

bool unique() const;

13 Returns: use_count() == 1.
14 Throws: nothing.

15 Notes: unique() may be faster than use_count(). If you are using unique() to implement copy on write, do
not rely on a specific value when get() == 0.

operator unspecified-bool-type () const;

16 Returns: an unspecified value that, when used in boolean contexts, is equivalent to get() != 0.
17 Throws: nothing.

18 Notes: This conversion operator allows shared_ptr objects to be used in boolean contexts. [Example: if (p &&
p->valid()) —end example.] The actual target type is typically a pointer to a member function, avoiding many
of the implicit conversion pitfalls.

```

## 2.2.3.6 shared\_ptr comparison

[tr.util.smartptr.shared.cmp]

```

template<class T, class U>
bool operator==(shared_ptr<T> const& a,
 shared_ptr<U> const& b);

1 Returns: a.get() == b.get().
2 Throws: nothing.

```

```
template<class T, class U>
bool operator!=(shared_ptr<T> const& a, shared_ptr<U> const& b);
```

3     *Returns:* a.get() != b.get().

4     *Throws:* nothing.

```
template<class T, class U>
bool operator<(shared_ptr<T> const& a, shared_ptr<U> const& b);
```

5     *Returns:* an unspecified value such that

- operator< is a strict weak ordering as described in section 25.3 [lib.alg.sorting];
- under the equivalence relation defined by operator<, !(a < b) && !(b < a), two shared\_ptr instances are equivalent if and only if they *share ownership* or are both empty.

6     *Throws:* nothing.

7     *Notes:* Allows shared\_ptr objects to be used as keys in associative containers.

**2.2.3.7 shared\_ptr operators**

[tr.util.smartptr.shared.op]

```
template<class E, class T, class Y>
basic_ostream<E, T>&
operator<< (basic_ostream<E, T>& os, shared_ptr<Y> const& p);
```

1     *Effects:* os << p.get();

2     *Returns:* os.

**2.2.3.8 shared\_ptr specialized algorithms**

[tr.util.smartptr.shared.spec]

```
template<class T>
void swap(shared_ptr<T>& a, shared_ptr<T>& b);
```

1     *Effects:* Equivalent to a.swap(b).

2     *Throws:* nothing.

**2.2.3.9 shared\_ptr casts**

[tr.util.smartptr.shared.cast]

```
template<class T, class U>
shared_ptr<T> static_pointer_cast(shared_ptr<U> const& r);
```

1     *Requires:* The expression static\_cast<T\*>(r.get()) is well-formed.

2     *Returns:* If r is *empty*, an *empty* shared\_ptr<T>; otherwise, a shared\_ptr<T> object that stores static\_cast<T\*>(r.get()) and *shares ownership* with r.

3     *Throws:* nothing.

4     *Notes:* the seemingly equivalent expression `shared_ptr<T>(static_cast<T*>(r.get()))` will eventually result in undefined behavior, attempting to delete the same object twice.

```
template<class T, class U>
shared_ptr<T> dynamic_pointer_cast(shared_ptr<U> const& r);
```

5     *Requires:* The expression `dynamic_cast<T*>(r.get())` is well-formed and does not invoke undefined behavior.

6     *Returns:*

- When `dynamic_cast<T*>(r.get())` returns a nonzero value, a `shared_ptr<T>` object that stores a copy of it and *shares ownership* with `r`;
- Otherwise, an *empty* `shared_ptr<T>` object.

7     *Throws:* nothing.

8     *Notes:* the seemingly equivalent expression `shared_ptr<T>(dynamic_cast<T*>(r.get()))` will eventually result in undefined behavior, attempting to delete the same object twice.

```
template<class T, class U>
shared_ptr<T> const_pointer_cast(shared_ptr<U> const& r);
```

9     *Requires:* The expression `const_cast<T*>(r.get())` is well-formed.

10    *Returns:* If `r` is empty, an empty `shared_ptr<T>`; otherwise, a `shared_ptr<T>` object that stores `const_cast<T*>(r.get())` and shares ownership with `r`.

11    *Throws:* Nothing.

12    *Notes:* the seemingly equivalent expression `shared_ptr<T>(const_cast<T*>(r.get()))` will eventually result in undefined behavior, attempting to delete the same object twice.

### 2.2.3.10 get\_deleter

**[tr.util.smartptr.getdeleter]**

```
template<class D, class T>
D * get_deleter(shared_ptr<T> const& p);
```

1     *Returns:* If `*this` owns a deleter `d` of type cv-unqualified `D`, returns `&d`; otherwise returns 0.

2     *Throws:* nothing.

### 2.2.4 Class template weak\_ptr

**[tr.util.smartptr.weak]**

1     The `weak_ptr` class template stores a “weak reference” to an object that’s already managed by a `shared_ptr`. To access the object, a `weak_ptr` can be converted to a `shared_ptr` using the member function `lock`.

```
namespace tr1 {
 template<class T> class weak_ptr {
 public:
 typedef T element_type;
```

```

// constructors
weak_ptr();
template<class Y> weak_ptr(shared_ptr<Y> const& r);
weak_ptr(weak_ptr const& r);
template<class Y> weak_ptr(weak_ptr<Y> const& r);

// destructor
~weak_ptr();

// assignment
weak_ptr& operator=(weak_ptr const& r);
template<class Y>
weak_ptr& operator=(weak_ptr<Y> const& r);
template<class Y>
weak_ptr& operator=(shared_ptr<Y> const& r);

// modifiers
void swap(weak_ptr& r);
void reset();

// observers
long use_count() const;
bool expired() const;
shared_ptr<T> lock() const;
};

// comparison
template<class T, class U>
bool operator<(weak_ptr<T> const& a, weak_ptr<U> const& b);

// specialized algorithms
template<class T>
void swap(weak_ptr<T>& a, weak_ptr<T>& b);
}

```

2 weak\_ptr is CopyConstructible, Assignable, and LessThanComparable, allowing its use in standard containers.

#### 2.2.4.1 weak\_ptr constructors

[tr.util.smartptr.weak.const]

`weak_ptr();`

- 1 *Effects:* Constructs an *empty* `weak_ptr`.
- 2 *Postconditions:* `use_count() == 0`.
- 3 *Throws:* nothing.

```

template<class Y> weak_ptr(shared_ptr<Y> const& r);
weak_ptr(weak_ptr const& r);
template<class Y> weak_ptr(weak_ptr<Y> const& r);

```

- 4     *Effects:* If `r` is *empty*, constructs an *empty* `weak_ptr`; otherwise, constructs a `weak_ptr` that *shares ownership* with `r` and stores a copy of the pointer stored in `r`.
- 5     *Postconditions:* `use_count() == r.use_count()`.
- 6     *Throws:* nothing.

**2.2.4.2 weak\_ptr destructor**

[tr.util.smartptr.weak.dest]

`~weak_ptr();`

- 1     *Effects:* Destroys this `weak_ptr` but has no effect on the object its stored pointer points to.
- 2     *Throws:* nothing.

**2.2.4.3 weak\_ptr assignment**

[tr.util.smartptr.weak.assign]

```
weak_ptr& operator=(weak_ptr const& r);
template<class Y> weak_ptr& operator=(weak_ptr<Y> const& r);
template<class Y> weak_ptr& operator=(shared_ptr<Y> const& r);
```

- 1     *Effects:* Equivalent to `weak_ptr(r).swap(*this)`.
- 2     *Throws:* nothing.
- 3     *Notes:* The implementation is free to meet the effects (and the implied guarantees) via different means, without creating a temporary.

**2.2.4.4 weak\_ptr modifiers**

[tr.util.smartptr.weak.mod]

`void swap(weak_ptr& r);`

- 1     *Effects:* Exchanges the contents of `*this` and `r`.
- 2     *Throws:* nothing.

`void reset();`

- 3     *Effects:* Equivalent to `weak_ptr().swap(*this)`.

**2.2.4.5 weak\_ptr observers**

[tr.util.smartptr.weak.obs]

`long use_count() const;`

- 1     *Returns:* 0 if `*this` is *empty*; otherwise, the number of `shared_ptr` instances that *share ownership* with `*this`.
- 2     *Throws:* nothing.
- 3     *Notes:* `use_count()` is not necessarily efficient. Use only for debugging and testing purposes, not for production code.

```

 bool expired() const;
4 Returns: use_count() == 0.
5 Throws: nothing.
6 Notes: expired() may be faster than use_count().
shared_ptr<T> lock() const;
7 Returns: expired() ? shared_ptr<T>() : shared_ptr<T>(*this).
8 Throws: nothing.

```

**2.2.4.6 weak\_ptr comparison**

[tr.util.smartptr.weak.cmp]

```

template<class T, class U>
bool operator<(weak_ptr<T> const& a, weak_ptr<U> const& b);
1 Returns: an unspecified value such that
 — operator< is a strict weak ordering as described in section 25.3 [lib.alg.sorting];
 — under the equivalence relation defined by operator<, !(a < b) && !(b < a), two weak_ptr instances
 are equivalent if and only if they share ownership or are both empty.
2 Throws: nothing.
3 Notes: Allows weak_ptr objects to be used as keys in associative containers.

```

**2.2.4.7 weak\_ptr specialized algorithms**

[tr.util.smartptr.weak.spec]

```

template<class T>
void swap(weak_ptr<T>& a, weak_ptr<T>& b)
1 Effects: Equivalent to a.swap(b).
2 Throws: nothing.

```

**2.2.5 Class template enable\_shared\_from\_this**

[tr.util.smartptr.enab]

- 1 A class can derive from the `enable_shared_from_this` class template, passing itself as a template parameter, to inherit the `shared_from_this` member functions that obtain a `shared_ptr` instance pointing to `this`.
- 2 [Example:

```

 struct X: public enable_shared_from_this<X>
 {
 };

 int main()
 {

```

```

shared_ptr<X> p(new X);
shared_ptr<X> q = p->shared_from_this();
assert(p == q);
assert(!(p < q) && !(q < p)); // p and q share ownership
}

```

—end example.]

```

namespace tr1 {
 template<class T> class enable_shared_from_this {
protected:
 enable_shared_from_this();
 enable_shared_from_this(enable_shared_from_this const&);
 enable_shared_from_this&
 operator=(enable_shared_from_this const&);
 ~enable_shared_from_this();
public:
 shared_ptr<T> shared_from_this();
 shared_ptr<T const> shared_from_this() const;
 };
}

```

```

enable_shared_from_this<T>::enable_shared_from_this();
enable_shared_from_this<T>::enable_shared_from_this(
 enable_shared_from_this<T> const&);

```

3     *Effects:* Constructs an enable\_shared\_from\_this<T> instance.

4     *Throws:* nothing.

```

enable_shared_from_this<T>&
enable_shared_from_this<T>
 ::operator=(enable_shared_from_this<T> const&);

```

5     *Returns:* \*this.

6     *Throws:* nothing.

```

enable_shared_from_this<T>::~enable_shared_from_this();

```

7     *Effects:* Destroys \*this.

8     *Throws:* nothing.

```

template<class T> shared_ptr<T>
enable_shared_from_this<T>::shared_from_this();

```

```

template<class T> shared_ptr<T const>
enable_shared_from_this<T>::shared_from_this() const;

```

9     *Requires:* enable\_shared\_from\_this<T> is an accessible base class of T. \*this is a subobject of an instance t of type T. There is at least one shared\_ptr instance p that owns &t.

10       >Returns: A `shared_ptr<T>` instance `r` that *shares ownership with p*.

11       >Postconditions: `r.get() == this`.

12 [Note: a typical implementation is shown below:

```
template<class T> class enable_shared_from_this
{
private:
 weak_ptr<T> __weak_this;

protected:
 enable_shared_from_this() {}
 enable_shared_from_this(enable_shared_from_this const &) {}
 enable_shared_from_this &
 operator=(enable_shared_from_this const &) { return *this; }
 ~enable_shared_from_this() {}

public:
 shared_ptr<T> shared_from_this()
 { return shared_ptr<T>(__weak_this); }
 shared_ptr<T const> shared_from_this() const
 { return shared_ptr<T const>(__weak_this); }
};
```

13 The three `shared_ptr` constructors that create unique pointers should detect the presence of an `enable_shared_from_this` base and assign the newly created `shared_ptr` to its `__weak_this` member. —end note.]

---

## 3 Function objects

[tr.func]

---

- 1 This clause defines components for creating and manipulating function objects, and for higher-order programming.
- 2 The following subclauses describe class template `result_of`, function template `mem_fn`, function object binders, and the polymorphic function wrapper function, as summarized in Table 2.

Table 2: Function object library summary

| Subclause                                    | Header(s)    |
|----------------------------------------------|--------------|
| <a href="#">3.2</a> <code>result_of</code>   | <functional> |
| <a href="#">3.3</a> <code>mem_fn</code>      | <functional> |
| <a href="#">3.4</a> Function object binders  | <functional> |
| <a href="#">3.5</a> Function object wrappers | <functional> |

### 3.1 Additions to <functional> synopsis

[tr.func.syn]

```
namespace tr1 {
 // [3.2] class template result_of
 template <class FunctionCallTypes> class result_of;

 // [3.3] function template mem_fn
 template<class R, class T>
 unspecified mem_fn(R T::* pm);

 // [3.4] Function object binders
 template<class T> struct is_bind_expression;
 template<class T> struct is_placeholder;

 template<class F>
 unspecified bind(F f);
 template<class R, class F>
 unspecified bind(F f);

 template<class F, class A1>
 unspecified bind(F f, A1 a1);
 template<class R, class T, class A1>
 unspecified bind(R T::* pm, A1 a1);
 template<class R, class F, class A1>
```

```

 unspecified bind(F f, A1 a1);

 // for all integers n in [2, N].

template<class F, class A1, ..., class An>
 unspecified bind(F f, A1 a1, ..., An an);
template<class R, class T, class A1, ..., class An>
 unspecified bind(R T::* pmf, A1 a1, ..., An an);
template<class R, class F, class A1, ..., class An>
 unspecified bind(F f, A1 a1, ..., An an);

namespace placeholders {
 // M is the implementation-defined number of placeholders
 extern unspecified _1;
 extern unspecified _2;
 .
 .
 .
 extern unspecified _M;
}

// [3.5] polymorphic function wrappers
class bad_function_call;

template<class Function> class function;

template<class Function>
void swap(function<Function>&, function<Function>&);

template<class Function1, class Function2>
void operator==(const function<Function1>&,
 const function<Function2>&);

template<class Function1, class Function2>
void operator!=(const function<Function1>&,
 const function<Function2>&);
}

```

## 3.2 Function return types

[tr.func.ret]

```

template <class FunctionCallTypes> // F(T1, T2, ..., TN)
class result_of {
public :
 // types
 typedef unspecified type;
};

```

<sup>1</sup> Given an lvalue  $f$  of type  $F$  and lvalues  $t_1, t_2, \dots, t_N$  of types  $T_1, T_2, \dots, T_N$ , respectively, the type member  $type$  defines the result type of the expression  $f(t_1, t_2, \dots, t_N)$ .

- 2 The implementation may determine the member type `type` via any means that produces the exact type of the expression `f(t1, t2, ..., tN)` for the given types. [Note: The intent is that implementations are permitted to use special compiler hooks —end note]
- 3 If the implementation cannot determine the type of the expression `f(t1, t2, ..., tN)`, or if the expression is ill-formed, the implementation shall use the following process to determine the member type `type`:
  1. If `F` is a function pointer or function reference type, `type` is the return type of the function type.
  2. If `F` is a member function pointer type, `type` is the return type of the member function type.
  3. If `F` is a function object defined by the standard library, the method of determining `type` is unspecified.
  4. If `F` is a possibly *cv*-qualified class type with a member type `result_type`, `type` is `F::result_type`.
  5. If `F` is a possibly *cv*-qualified class type with no member named `result_type` or if `F::result_type` is not a type:
    - (a) If  $N=0$  (no arguments), `type` is `void`.
    - (b) If  $N>0$ , `type` is `F::result<F(T1, T2, ..., TN)>::type`.
  6. Otherwise, the program is ill-formed.

3.3 Function template `mem_fn`

[tr.func.memfn]

```
template<class R, class T>
unspecified mem_fn(R T::* pm);
```

- 1 `mem_fn(&X::f)`, where `f` is a member function of `X`, returns an object through which `&X::f` can be called given a pointer, a smart pointer, an iterator, or a reference to `X` followed by the argument list required for `X::f`, if any. The returned object shall be `CopyConstructible` and `Assignable`, its copy constructor and assignment operator shall not throw exceptions, and it shall have a nested typedef `result_type` defined as the return type of `f`.
- 2 `mem_fn(&X::m)`, where `m` is a data member of `X`, returns an object through which a reference to `&X::m` can be obtained given a pointer, a smart pointer, an iterator, or a reference to `X`. The returned object shall be `CopyConstructible` and `Assignable`, its copy constructor and assignment operator shall not throw exceptions, and it shall have a nested typedef `result_type` defined as either `M` or `M const &`, where `M` is the type of `m`.

```
template<class R, class T>
unspecified mem_fn(R T::* pm);
```

3 *Returns*:

- When `pm` is a pointer to a member function taking  $n$  arguments, a function object `f` such that the expression `f(t, a1, ..., an)` is equivalent to `(t.*pm)(a1, ..., an)` when `t` is an lvalue of type `T` or derived from `T`, `((*t).*pm)(a1, ..., an)` otherwise.
- When `pm` is a pointer to a data member, a function object `f` such that the expression `f(t)` is equivalent to `t.*pm` when `t` is an lvalue of type `T` or derived from `T`, `(*t).*pm` otherwise.

4 *Throws*: nothing.

5 *Notes*: Implementations may implement `mem_fn` as a set of overloaded function templates.

### 3.4 Function object binders

[tr.func.bind]

- 1 3.4 describes a uniform mechanism for binding arguments of function objects.

#### 3.4.1 Class template is\_bind\_expression

[tr.func.bind.isbind]

```
namespace tr1 {
 template<class T> struct is_bind_expression {
 static const bool value = see below;
 };
}
```

- 1 is\_bind\_expression can be used to detect function objects generated by bind. bind uses is\_bind\_expression to detect subexpressions. The template can be specialized by users to indicate that a type should be treated as a subexpression in a bind call.

```
static const bool value;
```

- 2 true if T is a type returned from bind, false otherwise.

#### 3.4.2 Class template is\_placeholder

[tr.func.bind.isplace]

```
namespace tr1 {
 template<class T> struct is_placeholder {
 static const int value = see below;
 };
}
```

- 1 is\_placeholder can be used to detect the standard placeholders \_1, \_2, and so on. bind uses is\_placeholder to detect placeholders. The template can be specialized by users to indicate a placeholder type.

```
static const int value;
```

- 2 value is N if T is the type of tr1::placeholders::\_N, 0 otherwise.

#### 3.4.3 Function template bind

[tr.func.bind.bind]

- 1 The function  $\lambda(x)$  is defined as x.get() when x is of type reference\_wrapper<F> for some F, x otherwise.
- 2 The function  $\mu(x, v_1, \dots, v_m)$ , where m is a nonnegative integer, x is of type X, and k is is\_placeholder<X>::value, is defined as:
  - x.get(), when X is a reference\_wrapper<T> for some T;
  - $v_k$ , when  $k \neq 0$ ;
  - $x(v_1, \dots, v_m)$ , when is\_bind\_expression<X>::value is true;
  - x otherwise.
- 3 A function object f of type F is called *simple*, if f is a pointer to a function with C++ linkage or F::result\_type is a type.

- 4 The maximum number of supported arguments ( $N$  in the synopsis) is implementation defined. Implementations are allowed to define additional, more specialized, bind overloads, or to fold the pointer to member overload into the general function template, as long as the behavior of the bind calls is unchanged.
- 5 Given a list of arguments  $a_1, a_2, \dots, a_n$ , a function object  $h$  as returned from a call to bind, and the definition:

```
struct forward {
 template<class T1, class T2, ..., class Tn>
 void operator()(T1&, T2&, ..., Tn&);
};
```

If the expression  $\text{forward}(\cdot)(a_1, a_2, \dots, a_n)$  is well-formed, then the expression  $h(a_1, a_2, \dots, a_n)$  must be well-formed and must have the same argument passing semantics as  $\text{forward}(\cdot)(a_1, a_2, \dots, a_n)$ . [Note: Implementations are encouraged to support argument forwarding for non-const temporaries. —end note]

```
template<class F> unspecified bind(F f);
```

- 6 *Requires:*  $F$  must be CopyConstructible.  $\lambda(f)()$  must be a valid expression. If  $f$  is not a *simple* function object, the behavior is implementation defined.

- 7 *Returns:* A function object  $g$  of an unspecified CopyConstructible type  $G$  such that the expression  $g(v_1, \dots, v_m)$  is equivalent to  $\lambda(f)()$ . The type of the expression  $g(v_1, \dots, v_m)$  is  $\text{result\_of}\langle R()\rangle::\text{type}$  where  $R$  is the type of  $\lambda(f)$ . If the function application is made via a cv-qualified reference to, or copy of,  $g$ , the same cv-qualifiers are applied to  $f$  before the evaluation. When  $f$  is a pointer to a function with C++ linkage,  $G::\text{result\_type}$  is defined as the return type of the  $f$ . When  $F::\text{result\_type}$  is defined,  $G::\text{result\_type}$  is defined as the same type.

- 8 *Throws:* nothing unless the copy constructor of  $f$  throws an exception.

- 9 *Notes:* Implementations are allowed to impose an upper limit on  $m$  (typically one more than the number of supported placeholders). It is implementation defined whether  $G$  is Assignable or DefaultConstructible.

```
template<class R, class F> unspecified bind(F f);
```

- 10 *Requires:*  $F$  must be CopyConstructible.  $\lambda(f)()$  must be a valid expression convertible to  $R$ .

- 11 *Returns:* A function object  $g$  of an unspecified CopyConstructible type  $G$  such that the expression  $g(v_1, \dots, v_m)$  is equivalent to  $\lambda(f)()$ , implicitly converted to  $R$ . If the function application is made via a cv-qualified reference to, or copy of,  $g$ , the same cv-qualifiers are applied to  $f$  before the evaluation.  $G::\text{result\_type}$  is defined as  $R$ .

- 12 *Throws:* nothing unless the copy constructor of  $f$  throws an exception.

- 13 *Notes:* Implementations are allowed to impose an upper limit on  $m$ . It is implementation defined whether  $G$  is Assignable or DefaultConstructible.

```
template<class F, class A1> unspecified bind(F f, A1 a1);
```

- 14 *Requires:*  $F$  and  $A1$  must be CopyConstructible.  $\lambda(f)(w_1)$  must be a valid expression for some value  $w_1$ . If  $f$  is not a *simple* function object, the behavior is implementation defined.

- 15 *Returns:* A function object  $g$  of an unspecified CopyConstructible type  $G$  such that the expression  $g(v_1, \dots, v_m)$  is equivalent to  $\lambda(f)(\mu(a_1, v_1, \dots, v_m))$ . The type of the expression  $g(v_1, \dots, v_m)$  is  $\text{result\_type}$ .

of  $\langle R(T) \rangle :: type$  where  $R$  is the type of  $\lambda(f)$  and  $T$  is the type of  $\mu(a_1, v_1, \dots, v_m)$ . If the function application is made via a cv-qualified reference to, or copy of,  $g$ , the same cv-qualifiers are applied to  $f$  and  $a_1$  before the evaluation. When  $f$  is a pointer to a function with C++ linkage,  $G :: result\_type$  is defined as the return type of the  $f$ . When  $F :: result\_type$  is defined,  $G :: result\_type$  is defined as the same type.

16     *Throws:* nothing unless the copy constructors of  $f$  or  $a_1$  throw an exception.

17     *Notes:* Implementations are allowed to impose an upper limit on  $m$ . It is implementation defined whether  $G$  is `Assignable` or `DefaultConstructible`.

```
template<class R, class T, class A1>
unspecified bind(R T::* pm, A1 a1);
```

18     *Requires:*  $pm$  must be a pointer to data member or pointer to a member function taking no arguments.

19     *Returns:* `bind(mem_fn(pm), a1)`.

```
template<class R, class F, class A1>
unspecified bind(F f, A1 a1);
```

20     *Requires:*  $F$  and  $A1$  must be `CopyConstructible`.  $\lambda(f)(w_1)$ , for some value  $w_1$ , must be a valid expression convertible to  $R$ .

21     *Returns:* A function object  $g$  of an unspecified `CopyConstructible` type  $G$  such that the expression  $g(v_1, \dots, v_m)$  is equivalent to  $\lambda(f)(\mu(a_1, v_1, \dots, v_m))$ , implicitly converted to  $R$ . If the function application is made via a cv-qualified reference to, or copy of,  $g$ , the same cv-qualifiers are applied to  $f$  and  $a_1$  before the evaluation.  $G :: result\_type$  is defined as  $R$ .

22     *Throws:* nothing unless the copy constructors of  $f$  or  $a_1$  throw an exception.

23     *Notes:* Implementations are allowed to impose an upper limit on  $m$ . It is implementation defined whether  $G$  is `Assignable` or `DefaultConstructible`.

```
template<class F, class A1, ..., class An>
unspecified bind(F f, A1 a1, ..., An an);
```

24     *Requires:*  $F$  and  $A_i$  must be `CopyConstructible`.  $\lambda(f)(w_1, \dots, w_n)$  must be a valid expression for some values  $w_i$ . If  $f$  is not a *simple* function object, the behavior is implementation defined.

25     *Returns:* A function object  $g$  of an unspecified `CopyConstructible` type  $G$  such that the expression  $g(v_1, \dots, v_m)$  is equivalent to  $\lambda(f)(\mu(a_1, v_1, \dots, v_m), \dots, \mu(a_n, v_1, \dots, v_m))$ .

26     The type of the expression  $g(v_1, \dots, v_m)$  is `result_of<R(T1, T2, ..., Tn)> :: type` where  $R$  is the type of  $\lambda(f)$  and each  $T_i$  is the type of  $\mu(a_i, v_1, \dots, v_m)$ .

27     If the function application is made via a cv-qualified reference to, or copy of,  $g$ , the same cv-qualifiers are applied to  $f$  and  $a_i$  before the evaluation. When  $f$  is a pointer to a function with C++ linkage,  $G :: result\_type$  is defined as the return type of the  $f$ . When  $F :: result\_type$  is defined,  $G :: result\_type$  is defined as the same type.

28     *Throws:* nothing unless the copy constructors of  $f$  or  $a_i$  throw an exception.

29     *Notes:* Implementations are allowed to impose an upper limit on  $m$ . It is implementation defined whether  $G$  is `Assignable` or `DefaultConstructible`.

```
template<class R, class T, class A1, ..., class An>
unspecified bind(R T::* pmf, A1 a1, ..., An an);
```

30     *Requires:* pmf must be a pointer to a member function taking  $n-1$  arguments.

31     *Returns:* bind(mem\_fn(pmf), a1, ..., an).

```
template<class R, class F, class A1, ..., class An>
unspecified bind(F f, A1 a1, ..., An an);
```

32     *Requires:* F and  $A_i$  must be CopyConstructible.  $\lambda(f)(w_1, \dots, w_n)$ , for some values  $w_i$ , must be a valid expression convertible to R.

33     *Returns:* A function object g of an unspecified CopyConstructible type G such that the expression g( $v_1, \dots, v_m$ ) is equivalent to  $\lambda(f)(\mu(a_1, v_1, \dots, v_m), \dots, \mu(an, v_1, \dots, v_m))$ , implicitly converted to R. If the function application is made via a cv-qualified reference to, or copy of, g, the same cv-qualifiers are applied to f and  $a_i$  before the evaluation. G::result\_type is defined as R.

34     *Throws:* nothing unless the copy constructors of f or  $a_i$  throw an exception.

35     *Notes:* Implementations are allowed to impose an upper limit on m. It is implementation defined whether G is Assignable or DefaultConstructible.

#### 3.4.4 Placeholders

[tr.func.bind.place]

```
namespace tr1 {
 namespace placeholders {
 extern unspecified _1;
 extern unspecified _2;
 extern unspecified _3;
 // implementation defined number of additional placeholders
 }
}
```

- All placeholder types are DefaultConstructible and CopyConstructible, and their default constructors and copy constructors do not throw. It is implementation defined whether placeholder types are Assignable. Assignable placeholders' copy assignment operators do not throw exceptions.

#### 3.5 Polymorphic function wrappers

[tr.func.wrap]

- 3.5 describes a polymorphic wrapper class that encapsulates arbitrary function objects.

##### 3.5.1 Class bad\_function\_call

[tr.func.wrap.badcall]

- The bad\_function\_call exception class is thrown primarily when a polymorphic adaptor is invoked but is empty (see 20.3.10).

```
namespace tr1 {
 class bad_function_call : public std::exception
 {
 public:
 // [trfunc.wrap.badcall.const] constructor
```

```

 bad_function_call();
 };
}

```

### 3.5.1.1 bad\_function\_call constructor

[tr.func.wrap.badcall.const]

```
bad_function_call();

1 Effects: constructs a bad_function_call object.
```

### 3.5.2 Class template function

[tr.func.wrap.func]

- 1 The library provides polymorphic wrappers that generalize the notion of a function pointer. Wrappers can store, copy, and call arbitrary function objects given a function signature (denoted by a set of argument types and a return type), allowing functions to be first-class objects.
- 2 A function object *f* of type *F* is *Callable* given a set of argument types *T*<sub>1</sub>, *T*<sub>2</sub>, ..., *T*<sub>*N*</sub> and a return type *R*, if one of the following conditions holds given rvalues *t*<sub>1</sub>, *t*<sub>2</sub>, ..., *t*<sub>*N*</sub> of types *T*<sub>1</sub>, *T*<sub>2</sub>, ..., *T*<sub>*N*</sub>, respectively:
  - If *F* is not a pointer to member function type, the expression *f*(*t*<sub>1</sub>, *t*<sub>2</sub>, ..., *t*<sub>*N*</sub>) is well-formed and is convertible to *R*.
  - If *F* is a pointer to member function type, the expression *mem\_fn(f)*(*t*<sub>1</sub>, *t*<sub>2</sub>, ..., *t*<sub>*N*</sub>) is well-formed and is convertible to *R*.
- 3 The function class template is a function object type whose call signature is defined by its template argument (a function type).

```
namespace tr1 {
 // Function type R (T1, T2, ..., TN), 0 ≤ N ≤ Nmax
 template<class Function>
 class function
 : public unary_function<R, T1> // iff N == 1
 : public binary_function<R, T1, T2> // iff N == 2
 {
 public:
 typedef R result_type;

 // [3.5.2.1] construct/copy/destroy
 explicit function();
 function(const function&);
 template<class F>
 function(F);
 template<class F>
 function(reference_wrapper<F>);
 function& operator=(const function&);
 template<class F>
 function& operator=(F);
 template<class F>
 function& operator=(reference_wrapper<F>);
 ~function();
}
```

```

// [3.5.2.2] function modifiers
void swap(function&);
void clear();

// [3.5.2.3] function capacity
bool empty() const;
operator unspecified-bool-type() const;

// [3.5.2.4] function invocation
R operator()(T1, T2, ..., TN) const;
};

// [3.5.2.5] specialized algorithms
template<class Functionr>
void swap(function<Function>&, function<Function>&);

// [3.5.2.6] undefined operators
template<class Function1, class Function2>
void operator==(const function<Function1>&,
 const function<Function2>&);
template<class Function1, class Function2>
void operator!=(const function<Function1>&,
 const function<Function2>&);
}

```

### 3.5.2.1 function construct/copy/destroy

[tr.func.wrap.func.con]

```

explicit function();

1 Postconditions: this->empty().
2 Throws: will not throw.

```

```

function(const function& f);

3 Postconditions: this->empty() if f.empty(); otherwise, *this targets a copy of f.
4 Throws: will not throw if the target of f is a function pointer or a function object passed via reference_wrapper.
 Otherwise, may throw bad_alloc or any exception thrown by the copy constructor of the stored function object.

```

```

template<class F>
function(F f);

5 Requires: f is a callable function object for argument types T1, T2, ..., TN and return type R.
6 Postconditions: this->empty() if any of the following hold:
 — f is a NULL function pointer.
 — f is a NULL member function pointer.

```

— *f* is an instance of the function class template and *f*.empty()

7     Otherwise, *\*this* targets a copy of *f* if *f* is not a pointer to member function, and targets a copy of *mem\_fn(f)* if  
*f* is a pointer to member function.

8     *Throws*: will not throw when *f* is a function pointer. Otherwise, may throw *bad\_alloc* or any exception thrown  
by *F*'s copy constructor.

```
template<class F> function(reference_wrapper<F> f);
```

9     *Requires*: *f.get()* is a callable function object for argument types *T1, T2, ..., TN* and return type *R*.

10    *Postconditions*: *!this->empty()* and *\*this* targets *f.get()*.

11    *Throws*: will not throw.

```
function& operator=(const function& f);
```

12    *Effects*: *function(f).swap(\*this)*;

13    *Returns*: *\*this*

```
template<class F>
function& operator=(F f);
```

14    *Effects*: *function(f).swap(\*this)*;

15    *Returns*: *\*this*

```
template<class F>
function& operator=(reference_wrapper<F> f);
```

16    *Effects*: *function(f).swap(\*this)*;

17    *Returns*: *\*this*

18    *Throws*: will not throw.

```
~function();
```

19    *Effects*: if *!this->empty()*, destroys the target of *this*.

### 3.5.2.2 function modifiers

[tr.func.wrap.func.mod]

```
void swap(function& other);
```

1     *Effects*: interchanges the targets of *\*this* and *other*.

2     *Throws*: will not throw.

```
void clear();
```

3     *Effects*: If *!this->empty()*, deallocates current target.

4     *Postconditions*: *this->empty()*.

## 3.5.2.3 function capacity

[tr.func.wrap.func.cap]

`bool empty() const`

1     *Returns:* true if the function object has a target, false otherwise.

2     *Throws:* will not throw.

`operator unspecified-bool-type() const`

3     *Returns:* if !this->empty(), returns a value that will evaluate true in a boolean context; otherwise, returns a value that will evaluate false in a boolean context. The value type returned shall not be convertible to int.

4     *Throws:* will not throw.

5     *Notes:* This conversion can be used in contexts where a bool is expected (e.g., an if condition); however, implicit conversions (e.g., to int) that can occur with bool are not allowed, eliminating some sources of user error. (See clause 2.2.3.5.) One possible implementation choice for this type is pointer-to-member.

## 3.5.2.4 function invocation

[tr.func.wrap.func.inv]

`R operator()(T1 t1, T2 t2, ..., TN tN) const`

1     *Effects:* f(t1, t2, ..., tN), where f is the target of \*this.

2     *Returns:* nothing, if R is void; otherwise, the return value of the call to f.

3     *Throws:* bad\_function\_call if this->empty(); otherwise, any exception thrown by the wrapped function object.

## 3.5.2.5 specialized algorithms

[tr.func.wrap.func.alg]

`template<class Function>
void swap(function<Function>& f1, function<Function>& f2);`

1     *Effects:* f1.swap(f2);

## 3.5.2.6 undefined operators

[tr.func.wrap.func.undef]

`template<class Function1, class Function2>
void operator==(const function<Function1>&, const function<Function2>&);`

1     This function shall be left undefined.

2     *Note:* the boolean-like conversion opens a loophole whereby two function instances can be compared via ==. This undefined void operator == closes the loophole and ensures a compile-time or link-time error.

`template<class Function1, class Function2>
void operator!=(const function<Function1>&, const function<Function2>&);`

- 3 This function shall be left undefined.
- 4 *Note:* the boolean-like conversion opens a loophole whereby two function instances can be compared via !=. This undefined void operator != closes the loophole and ensures a compile-time or link-time error.

---

## 4 Metaprogramming and type traits [tr.meta]

---

- 1 This clause describes components used by C++ programs, particularly in templates, to: support the widest possible range of types, optimise template code usage, detect type related user errors, and perform type inference and transformation at compile time.
- 2 The following subclauses describe type traits requirements, unary type traits, traits that describe relationships between types, and traits that perform transformations on types, as summarized in Table 3.

Table 3: Type traits library summary

| Subclause                         | Header(s)     |
|-----------------------------------|---------------|
| 4.1 Requirements                  |               |
| 4.3 Unary type traits             | <type_traits> |
| 4.4 Relationships between types   | <type_traits> |
| 4.5 Transformations between types | <type_traits> |

### 4.1 Requirements

[tr.meta.rqmts]

#### 4.1.1 Unary type traits

[tr.meta.rqmts.unary]

- 1 In table 4, X is a class template that is a unary type trait and T is any arbitrary type.

Table 4: UnaryTypeTrait requirements

| expression       | return type                          | requirement                                                                                                                                        |
|------------------|--------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------|
| X<T>::value_type | An integral type                     | The type of X<T>::value.                                                                                                                           |
| X<T>::value      | value_type                           | An integral constant expression that takes the value of the specified trait.                                                                       |
| X<T>::type       | integral_constant<value_type, value> | A type for use in situations where a typename is more appropriate than a value. The class template integral_constant is declared in <type_traits>. |

| expression                                     | return type | requirement                                                                                                                                                   |
|------------------------------------------------|-------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <code>X&lt;T&gt;::type t = X&lt;T&gt;()</code> |             | Both lvalues of type <code>X&lt;T&gt;</code> const& and rvalues of type <code>X&lt;T&gt;</code> are implicitly convertible to <code>X&lt;T&gt;::type</code> . |

## 4.1.2 Binary type traits

[tr.meta.rqmts.binary]

- 1 In table 5, X is a class template that is a binary type trait and T and U are any arbitrary types.

Table 5: BinaryTypeTrait requirements

| expression                                         | return type                                       | requirement                                                                                                                                                                         |
|----------------------------------------------------|---------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <code>X&lt;T,U&gt;::value</code>                   | <code>bool</code>                                 | An integral constant expression that is true if T is related to U by the relation specified, and false otherwise.                                                                   |
| <code>X&lt;T,U&gt;::value_type</code>              | <code>bool</code>                                 | A type that is the type of <code>X&lt;T,U&gt;::value</code> , this is always <code>bool</code> for <code>BinaryTypeTraits</code> .                                                  |
| <code>X&lt;T,U&gt;::type</code>                    | <code>integral_constant&lt;bool, value&gt;</code> | A type for use in situations where a typename is more appropriate than a value. The class template <code>integral_constant</code> is declared in <code>&lt;type_traits&gt;</code> . |
| <code>X&lt;T,U&gt;::type t = X&lt;T,U&gt;()</code> |                                                   | Both lvalues of type <code>X&lt;T,U&gt;</code> const& and rvalues of type <code>X&lt;T,U&gt;</code> are implicitly convertible to <code>X&lt;T,U&gt;::type</code> .                 |

## 4.1.3 Transformation type traits

[tr.meta.rqmts.trans]

- 1 In table 6, X is a class template that is a transformation trait and T is any arbitrary type.

Table 6: TransformationTrait requirements

| expression                    | requirement                                                                     |
|-------------------------------|---------------------------------------------------------------------------------|
| <code>X&lt;T&gt;::type</code> | The result is a type that is the result of applying transformation X to type T. |

## 4.2 Header &lt;type\_traits&gt; synopsis

[tr.meta.type.synop]

```
namespace tr1{
```

```
// [4.3.1] helper class:
```

```

template <class T, T v> struct integral_constant;
typedef integral_constant<bool, true> true_type;
typedef integral_constant<bool, false> false_type;

// [4.3.2] Primary type categories:
template <class T> struct is_void;
template <class T> struct is_integral;
template <class T> struct is_floating_point;
template <class T> struct is_array;
template <class T> struct is_pointer;
template <class T> struct is_reference;
template <class T> struct is_member_object_pointer;
template <class T> struct is_member_function_pointer;
template <class T> struct is_enum;
template <class T> struct is_union;
template <class T> struct is_class;
template <class T> struct is_function;

// [4.3.3] composite type categories:
template <class T> struct is_arithmetic;
template <class T> struct is_fundamental;
template <class T> struct is_object;
template <class T> struct is_scalar;
template <class T> struct is_compound;
template <class T> struct is_member_pointer;

// [4.3.4] type properties:
template <class T> struct is_const;
template <class T> struct is_VOLATILE;
template <class T> struct is_pod;
template <class T> struct is_empty;
template <class T> struct is_polymorphic;
template <class T> struct is_abstract;
template <class T> struct has_trivial_constructor;
template <class T> struct has_trivial_copy;
template <class T> struct has_trivial_assign;
template <class T> struct has_trivial_destructor;
template <class T> struct has_nothrow_constructor;
template <class T> struct has_nothrow_copy;
template <class T> struct has_nothrow_assign;
template <class T> struct has_virtual_destructor;
template <class T> struct is_signed;
template <class T> struct is_unsigned;
template <class T> struct alignment_of;
template <class T> struct rank;
template <class T, unsigned I = 0> struct extent;

// [4.4] type relations:
template <class T, class U> struct is_same;
template <class From, class To> struct is_convertible;

```

```

template <class Base, class Derived> struct is_base_of;

// [4.5.1] const-volatile modifications:
template <class T> struct remove_const;
template <class T> struct remove_volatile;
template <class T> struct remove_cv;
template <class T> struct add_const;
template <class T> struct add_volatile;
template <class T> struct add_cv;

// [4.5.2] reference modifications:
template <class T> struct remove_reference;
template <class T> struct add_reference;

// [4.5.3] array modifications:
template <class T> struct remove_extent;
template <class T> struct remove_all_extents;

// [4.5.4] pointer modifications:
template <class T> struct remove_pointer;
template <class T> struct add_pointer;

// [4.5.5] Other transformations
template <class T> struct aligned_storage;

} // namespace tr1

```

### 4.3 Unary Type Traits

[tr.meta.unary]

- 1 This sub-clause contains templates that may be used to query the properties of a type at compile time.
- 2 All of the class templates defined in this clause satisfy the `UnaryTypeTrait` requirements.
- 3 For all of the class templates declared in this clause, all members declared `static const` shall be defined in such a way that they are usable as integral constant expressions.
- 4 For all of the class templates `X` declared in this clause, both rvalues of type `X const` and lvalues of type `X const&` shall be implicitly convertible to `X::type`. A traits class `X` shall inherit from `X::type`. [Note: For exposition only, the class templates `X` defined in this clause are shown with base classes that depend on names defined within the scope of `X`. —end note]
- 5 For all of the class templates `X` declared in this clause, instantiating that template with a template-argument that is a class template specialization, may result in the implicit instantiation of the template argument if and only if the semantics of `X` require that the argument must be a complete type.

#### 4.3.1 Helper classes

[tr.meta.unary.help]

```

template <class T, T v>
struct integral_constant
{
 static const T value = v;

```

```

 typedef T value_type;
 typedef integral_constant<T,v> type;
};

typedef integral_constant<bool, true> true_type;
typedef integral_constant<bool, false> false_type;

```

- 1 The class template `integral_constant` and its associated typedefs `true_type` and `false_type` are for use in situations where a type rather than a value is required.

### 4.3.2 Primary Type Categories

[tr.meta.unary.cat]

- 1 The primary type categories correspond to the descriptions given in section [basic.types] of the C++ standard.
- 2 For any given type `T`, exactly one of the primary type categories shall have its member `value` evaluate to `true`.
- 3 For any given type `T`, the result of applying one of these templates to `T`, and to *cv-qualified* `T` shall yield the same result.
- 4 Undefined behaviour results if any C++ program adds specializations for any of the class templates defined in this clause.

```

template <class T> struct is_void
: public integral_constant<value_type,value>
{
 static const bool value = implementation_defined;
 typedef bool value_type;
 typedef integral_constant<value_type,value> type;
};

5 value : defined to be true if T is void or a cv-qualified void. Otherwise defined to be false.

template <class T> struct is_integral
: public integral_constant<value_type,value>
{
 static const bool value = implementation_defined;
 typedef bool value_type;
 typedef integral_constant<value_type,value> type;
};

6 value: defined to be true if T is an integral type ([basic.fundamental]). Otherwise defined to be false.

template <class T> struct is_floating_point
: public integral_constant<value_type,value>
{
 static const bool value = implementation_defined;
 typedef bool value_type;
 typedef integral_constant<value_type,value> type;
};

7 value: defined to be true if T is a floating point type ([basic.fundamental]). Otherwise defined to be false.

template <class T> struct is_array
: public integral_constant<value_type,value>
{
 static const bool value = implementation_defined;
}

```

```

 typedef bool value_type;
 typedef integral_constant<value_type, value> type;
};

8 value: defined to be true if T is an array type ([basic.compound]). Otherwise defined to be false. [Note: class
 template array, described in clause 6.2 of this technical report, is not an array type. —end note]

template <class T> struct is_pointer
: public integral_constant<value_type, value>
{
 static const bool value = implementation_defined;
 typedef bool value_type;
 typedef integral_constant<value_type, value> type;
};

9 value : defined to be true if T is a pointer type ([basic.compound]), this includes all function pointer types, but
 not pointers to members or member functions. Otherwise defined to be false.

template <class T> struct is_reference
: public integral_constant<value_type, value>
{
 static const bool value = implementation_defined;
 typedef bool value_type;
 typedef integral_constant<value_type, value> type;
};

10 value : defined to be true if T is a reference type ([basic.compound]), this includes all reference to function
 types. Otherwise defined to be false.

template <class T> struct is_member_object_pointer
: public integral_constant<value_type, value>
{
 static const bool value = implementation_defined;
 typedef bool value_type;
 typedef integral_constant<value_type, value> type;
};

11 value : defined to be true if T is a pointer to a data member. Otherwise defined to be false.

template <class T> struct is_member_function_pointer
: public integral_constant<value_type, value>
{
 static const bool value = implementation_defined;
 typedef bool value_type;
 typedef integral_constant<value_type, value> type;
};

12 value : defined to be true if T is a pointer to a member function. Otherwise defined to be false.

template <class T> struct is_enum
: public integral_constant<value_type, value>
{

```

```

 static const bool value = implementation_defined;
 typedef bool value_type;
 typedef integral_constant<value_type, value> type;
};

13 value : defined to be true if T is an enumeration type ([basic.compound]). Otherwise defined to be false.

template <class T> struct is_union
: public integral_constant<value_type, value>
{
 static const bool value = implementation_defined;
 typedef bool value_type;
 typedef integral_constant<value_type, value> type;
};

14 value : defined to be true if T is a union type ([basic.compound]). Otherwise defined to be false.

template <class T> struct is_class
: public integral_constant<value_type, value>
{
 static const bool value = implementation_defined;
 typedef bool value_type;
 typedef integral_constant<value_type, value> type;
};

15 value : defined to be true if T is a class type ([basic.compound]), in this context unions are not considered to be
 class types. Otherwise defined to be false.

template <class T> struct is_function
: public integral_constant<value_type, value>
{
 static const bool value = implementation_defined;
 typedef bool value_type;
 typedef integral_constant<value_type, value> type;
};

16 value : defined to be true if T is a function type ([basic.compound]). Otherwise defined to be false.

```

### 4.3.3 Composite type traits

[tr.meta.unary.comp]

- 1 These templates provide convenient compositions of the primary type categories, corresponding to the descriptions given in section [basic.types].
- 2 For any given type T, the result of applying one of these templates to T, and to *cv-qualified* T shall yield the same result.
- 3 Undefined behaviour results if any C++ program adds specializations for any of the class templates defined in this clause.

```

template <class T> struct is_arithmetic
: public integral_constant<value_type, value>
{
 static const bool value =
 is_integral<T>::value || is_floating_point<T>::value;

```

```

 typedef bool value_type;
 typedef integral_constant<value_type, value> type;
};

4 value : defined to be true if T is an arithmetic type ([basic.fundamental]). Otherwise defined to be false.

template <class T> struct is_fundamental
 : public integral_constant<value_type, value>
{
 static const bool value =
 is_integral<T>::value
 || is_floating_point<T>::value
 || is_void<T>::value;
 typedef bool value_type;
 typedef integral_constant<value_type, value> type;
};

5 value : defined to be true if T is a fundamental type ([basic.fundamental]). Otherwise defined to be false.

template <class T> struct is_object
 : public integral_constant<value_type, value>
{
 static const bool value =
 !(is_function<T>::value
 || is_reference<T>::value
 || is_void<T>::value);
 typedef bool value_type;
 typedef integral_constant<value_type, value> type;
};

6 value : defined to be true if T is an object type ([basic.types]). Otherwise defined to be false.

template <class T> struct is_scalar
 : public integral_constant<value_type, value>
{
 static const bool value =
 is_arithmetic<T>::value
 || is_enum<T>::value
 || is_pointer<T>::value
 || is_member_pointer<T>::value;
 typedef bool value_type;
 typedef integral_constant<value_type, value> type;
};

7 value : defined to be true if T is a scalar type ([basic.types]). Otherwise defined to be false.

template <class T> struct is_compound
 : public integral_constant<value_type, value>
{
 static const bool value = !is_fundamental<T>::value;
 typedef bool value_type;
 typedef integral_constant<value_type, value> type;
};

```

```

};

8 value : defined to be true if T is a compound type ([basic.compound]). Otherwise defined to be false.

template <class T> struct is_member_pointer
 : public integral_constant<value_type, value>
{
 static const bool value =
 is_member_object_pointer<T>::value
 || is_member_function_pointer<T>::value;
 typedef bool value_type;
 typedef integral_constant<value_type, value> type;
};

9 value : defined to be true if T is a pointer to a member or member function. Otherwise defined to be false.

```

#### 4.3.4 Type properties

[tr.meta.unary.prop]

- 1 These templates provide access to some of the more important properties of types; they reveal information which is available to the compiler, but which would not otherwise be detectable in C++ code.
- 2 Except where specified, it is undefined whether any of these templates have any full or partial specialisations defined. It is permitted for the user to specialise any of these templates on a user-defined type, provided the semantics of the specialisation match those given for the template in its description.

```

template <class T> struct is_const
 : public integral_constant<value_type, value>
{
 static const bool value = implementation_defined;
 typedef bool value_type;
 typedef integral_constant<value_type, value> type;
};

3 value: defined to be true if T is const-qualified ([basic.type.qualifier]). Otherwise defined to be false.

template <class T> struct is_volatile
 : public integral_constant<value_type, value>
{
 static const bool value = implementation_defined;
 typedef bool value_type;
 typedef integral_constant<value_type, value> type;
};

4 value : defined to be true if T is volatile-qualified ([basic.type.qualifier]). Otherwise defined to be false.

template <class T> struct is_pod
 : public integral_constant<value_type, value>
{
 static const bool value = implementation_defined;
 typedef bool value_type;
 typedef integral_constant<value_type, value> type;
};

```

```

};

5 Preconditions: template argument T shall be a complete type.

6 value: defined to be true if T is a POD type ([basic.type]). Otherwise defined to be false.

template <class T> struct is_empty
 : public integral_constant<value_type, value>
{
 static const bool value = implementation_defined;
 typedef bool value_type;
 typedef integral_constant<value_type, value> type;
};

7 Preconditions: template argument T shall be a complete type.

8 value: defined to be true if T is an empty class (10). Otherwise defined to be false.

template <class T> struct is_polymorphic
 : public integral_constant<value_type, value>
{
 static const bool value = implementation_defined;
 typedef bool value_type;
 typedef integral_constant<value_type, value> type;
};

9 Preconditions: template argument T shall be a complete type.

10 value: defined to be true if T is a polymorphic class (10.3). Otherwise defined to be false.

template <class T> struct is_abstract
 : public integral_constant<value_type, value>
{
 static const bool value = implementation_defined;
 typedef bool value_type;
 typedef integral_constant<value_type, value> type;
};

11 Preconditions: template argument T shall be a complete type.

12 value: defined to be true if T is a abstract class (10.4). Otherwise defined to be false.

template <class T> struct has_trivial_constructor
 : public integral_constant<value_type, value>
{
 static const bool value = implementation_defined;
 typedef bool value_type;
 typedef integral_constant<value_type, value> type;
};

13 Preconditions: template argument T shall be a complete type.

14 value: defined to be true if the default constructor for T is trivial(12.1). Otherwise defined to be false.

```

```

template <class T> struct has_trivial_copy
 : public integral_constant<value_type, value>
{
 static const bool value = implementation_defined;
 typedef bool value_type;
 typedef integral_constant<value_type, value> type;
};

15 Preconditions: template argument T shall be a complete type.

16 value: defined to be true if the copy constructor for T is trivial (12.8). Otherwise defined to be false.

template <class T> struct has_trivial_assign
 : public integral_constant<value_type, value>
{
 static const bool value = implementation_defined;
 typedef bool value_type;
 typedef integral_constant<value_type, value> type;
};

17 Preconditions: template argument T shall be a complete type.

18 value: defined to be true if the assignment operator for T is trivial (12.8). Otherwise defined to be false.

template <class T> struct has_trivial_destructor
 : public integral_constant<value_type, value>
{
 static const bool value = implementation_defined;
 typedef bool value_type;
 typedef integral_constant<value_type, value> type;
};

19 Preconditions: template argument T shall be a complete type.

20 value: defined to be true if the destructor for T is trivial (12.4). Otherwise defined to be false.

template <class T> struct has_nothrow_constructor : public
integral_constant<value_type, value> { static const bool value =
implementation_defined; typedef bool value_type; typedef
integral_constant<value_type, value> type; };

21 Preconditions: template argument T shall be a complete type.

22 value: defined to be true if the default constructor for T has an empty exception specification, or can otherwise
be deduced never to throw an exception. Otherwise defined to be false.

template <class T> struct has_nothrow_copy
 : public integral_constant<value_type, value>
{
 static const bool value = implementation_defined;
 typedef bool value_type;
 typedef integral_constant<value_type, value> type;
};

```

23     *Preconditions:* template argument T shall be a complete type.

24     value: defined to be true if the copy constructor for T has an empty exception specification, or can otherwise be deduced never to throw an exception. Otherwise defined to be false .

```
template <class T> struct has_nothrow_assign
 : public integral_constant<value_type ,value>
{
 static const bool value = implementation_defined;
 typedef bool value_type;
 typedef integral_constant<value_type ,value> type;
};
```

25     *Preconditions:* template argument T shall be a complete type.

26     value: defined to be true if the assignment operator for T has an empty exception specification, or can otherwise be deduced never to throw an exception. Otherwise defined to be false .

```
template <class T> struct has_virtual_destructor
 : public integral_constant<bool,value>
{
 static const bool value = implementation_defined;
 typedef bool value_type;
 typedef integral_constant<bool,value> type;
};
```

27     value: true if type T has a virtual destructor (12.4) otherwise false. [Note: An implementation that cannot determine whether a type has a virtual destructor, e.g. a pure library implementation with no compiler support, should return false. —end note]

```
template <class T> struct is_signed
 : public integral_constant<value_type ,value>
{
 static const bool value = implementation_defined;
 typedef bool value_type;
 typedef integral_constant<value_type ,value> type;
};
```

28     value: defined to be true if T is a signed integral type ([basic.fundamental]). Otherwise defined to be false .

```
template <class T> struct is_unsigned
 : public integral_constant<value_type ,value>
{
 static const bool value = implementation_defined;
 typedef bool value_type;
 typedef integral_constant<value_type ,value> type;
};
```

29     value: defined to be true if T is an unsigned integral type ([basic.fundamental]). Otherwise defined to be false .

```
template <class T> struct alignment_of
 : public integral_constant<value_type ,value>
```

```

{
 static const std::size_t value = implementation_defined;
 typedef std::size_t value_type;
 typedef integral_constant<value_type, value> type;
};

30 value: An implementation-defined integer value representing the number of bytes of the alignment of objects of
 type T; an object of type T may be allocated at an address that is a multiple of its alignment ([basic.types]).
```

```

template <class T> struct rank
 : public integral_constant<value_type, value>
{
 static const std::size_t value = implementation defined;
 typedef std::size_t value_type;
 typedef integral_constant<value_type, value> type;
};

31 value: An implementation-defined integer value representing the rank of objects of type T (8.3.4). [Note: The
 term “rank” here is used to describe the number of dimensions of an array type. —end note]
```

32 [Example:

```

// the following assertions should hold:
assert(rank<int>::value == 0);
assert(rank<int[2]>::value == 1);
assert(rank<int[] [4]>::value == 2);

—end example]

template <class T, unsigned I = 0> struct extent
 : public integral_constant<value_type, value>
{
 static const std::size_t value = implementation defined;
 typedef std::size_t value_type;
 typedef integral_constant<value_type, value> type;
};

33 value: An implementation-defined integer value representing the extent (dimension) of the I'th bound of objects
 of type T (8.3.4). If the type T is not an array type, has rank of less than I, or if I == 0 and is of type “array
 of unknown bound of T,” then value shall evaluate to zero; otherwise value shall evaluate to the number of
 elements in the I'th array bound of T. [Note: The term “extent” here is used to describe the number of elements
 in an array type —end note]
```

34 [Example:

```

// the following assertions should hold:
assert(extent<int>::value == 0);
assert(extent<int[2]>::value == 2);
assert(extent<int[2][4]>::value == 2);
assert(extent<int[] [4]>::value == 0);
assert((extent<int, 1>::value) == 0);
assert((extent<int[2], 1>::value) == 0);
```

```
assert((extent<int[2][4], 1>::value) == 4);
assert((extent<int[][], 1>::value) == 4);
```

—end example]

## 4.4 Relationships between types

[tr.meta.rel]

- 1 All of the templates in this header satisfy the `BinaryTypeTrait` requirements.
- 2 For all of the class templates declared in this clause, all members declared `static const` shall be defined in such a way that they are usable as integral constant expressions.
- 3 For all of the class templates `X` declared in this clause, both rvalues of type `X const` and lvalues of type `X const&` shall be implicitly convertible to `X::type`. A traits class `X` shall inherit from `X::type`. [Note: For exposition only, the class templates `X` defined in this clause are shown with base classes that depend on names defined within the scope of `X`. —end note]

### 4.4.1 Type relationships

[tr.meta.rel.rel]

```
template <class T, class U> struct is_same
: public integral_constant<value_type, value>
{
 static const bool value = false;
 typedef bool value_type;
 typedef integral_constant<value_type, value> type;
};

template <class T> struct is_same<T, T>
: public integral_constant<value_type, value>
{
 static const bool value = true;
 typedef bool value_type;
 typedef integral_constant<value_type, value> type;
};
```

- 1 `value`: defined to be `true` if `T` and `U` are the same type. Otherwise defined to be `false`.

```
template <class From, class To> struct is_convertible
: public integral_constant<value_type, value>
{
 static const bool value = implementation_defined;
 typedef bool value_type;
 typedef integral_constant<value_type, value> type;
};
```

- 2 `value`: defined to be `true` only if an imaginary lvalue of type `From` is implicitly-convertible to type `To` (4.0). Otherwise defined to be `false`. Special conversions involving string-literals and null-pointer constants are not considered (4.2, 4.10 and 4.11). No function-parameter adjustments (8.3.5) are made to type `To` when determining whether `From` is convertible to `To`: this implies that if type `To` is a function type or an array type, then `value` must necessarily evaluate to `false`.

- 3 The expression `is_convertible<From,To>::value` is ill-formed if:
- Type `From`, is a void or incomplete type ([basic.types]).
  - Type `To`, is an incomplete, void or abstract type ([basic.types]).
  - The conversion is ambiguous. [Example: the conversion is ambiguous if type `From` has multiple base classes of type `To` ([class.member.lookup]). —end example]
  - Type `To` is of class type and the conversion would invoke a non-public constructor of `To` ([class.access] and [class.conv.ctor]).
  - Type `From` is of class type and the conversion would invoke a non-public conversion operator of `From` ([class.access] and [class.conv.fct]).

```
template <class Base, class Derived> struct is_base_of
 : public integral_constant<value_type, value>
{
 static const bool value = implementation_defined;
 typedef bool value_type;
 typedef integral_constant<value_type, value> type;
};
```

- 4 *Preconditions*: template arguments `Base` and `Derived` shall both be complete types.

- 5 `value`: defined to be `true` if type `Base` is a base class of type `Derived` ([class.derived]) or if `Base` and `Derived` are the same type. Otherwise defined to be `false`.

## 4.5 Transformations between types

[tr.meta.trans]

- 1 This sub-clause contains templates that may be used to transform one type to another following some predefined rule.
- 2 All of the templates in this header satisfy the TransformationTrait requirements.

### 4.5.1 Const-volatile modifications

[tr.meta.trans.cv]

```
template <class T> struct remove_const{
 typedef T type;
};
template <class T> struct remove_const<T const>{
 typedef T type;
};
```

- 1 `type` : defined to be a type that is the same as `T`, except that any top level const-qualifier has been removed. [Example: `remove_const<const volatile int>::type` evaluates to `volatile int`, whereas `remove_const<const int*>` is `const int*`. —end example]

```
template <class T> struct remove_volatile{
 typedef T type;
};
template <class T> struct remove_volatile<T volatile>{
 typedef T type;
};
```

- 2      type : defined to be a type that is the same as T, except that any top level volatile-qualifier has been removed. [Example: `remove_const<const volatile int>::type` evaluates to `const int`, whereas `remove_const<volatile int*>` is `volatile int*`. —end example]
- ```
template <class T> struct remove_cv{
    typedef typename remove_const<
        typename remove_volatile<T>::type
    >::type
    type;
};
```
- 3 type : defined to be a type that is the same as T, except that any top level cv-qualifiers have been removed. [Example: `remove_cv<const volatile int>::type` evaluates to `int`, whereas `remove_cv<const volatile int*>` is `const volatile int*`. —end example]
- ```
template <class T> struct add_const{
 typedef T const type;
};
```
- 4      type : if T is a reference, function, or top level const-qualified type, then the same type as T, otherwise T const.
- ```
template <class T> struct add_volatile{
    typedef T volatile type;
};
```
- 5 type: if T is a reference, function, or top level const-qualified type, then the same type as T, otherwise T volatile.
- ```
template <class T> struct add_cv{
 typedef typename add_const<
 typename add_volatile<T>::type
 >::type
 type;
};
```
- 6      type: the same type as `add_const< add_volatile<T>::type >::type`.

### 4.5.2 Reference modifications

[tr.meta.trans.ref]

- ```
template <class T> struct remove_reference{
    typedef T type;
};

template <class T> struct remove_reference<T&>{
    typedef T type;
};

1      type : defined to be a type that is the same as T, except any reference qualifier has been removed.

template <class T> struct add_reference{
    typedef T& type;
};

template <class T> struct add_reference<T&>{
```

```

    typedef T& type;
};

2      type : if T is a reference type, then T, otherwise T& .

```

4.5.3 Array modifications

[tr.meta.trans.arr]

```

template <class T> struct remove_extent{
    typedef T type;
};

template <class T, std::size_t N> struct remove_extent<T[N]>{
    typedef T type;
};

template <class T> struct remove_extent<T[]>{
    typedefs T type;
};

```

1 type: for a type ‘array of U’, the resulting type is U; for any other type V, the resulting type is V.

2 Note: for multidimensional arrays, only the first array dimension is removed. For a type ‘array of const U’, the resulting type is const U.

3 [example

```

// the following assertions should all hold:
assert((is_same<remove_extent<int>::type, int>::value));
assert((is_same<remove_extent<int[2]>::type, int>::value));
assert((is_same<remove_extent<int[2][3]>::type, int[3]>::value));
assert((is_same<remove_extent<int[]>::type, int[3]>::value));

```

—end example]

```

template <class T> struct remove_all_extents {
    typedef T type;
};

template <class T, std::size_t N> struct remove_all_extents<T[N]> {
    typedef typename remove_all_extents<T>::type type;
};

template <class T> struct remove_all_extents<T[]> {
    typedef typename remove_all_extents<T>::type type;
};

```

4 type: for a type ‘multi-dimensional array of U’, the resulting type is U; for any other type V, the resulting type is V.

5 [example

```

// the following assertions should all hold:
assert((is_same<remove_all_extents<int>::type, int>::value));
assert((is_same<remove_all_extents<int[2]>::type, int>::value));
assert((is_same<remove_all_extents<int[2][3]>::type, int>::value));
assert((is_same<remove_all_extents<int[]>::type, int>::value));

```

—end example]

4.5.4 Pointer modifications

[tr.meta.trans.ptr]

```
template <class T> struct remove_pointer{
    typedef T type;
};

template <class T> struct remove_pointer<T*>{
    typedef T type;
};

template <class T> struct remove_pointer<T* const>{
    typedef T type;
};

template <class T> struct remove_pointer<T* volatile>{
    typedef T type;
};

template <class T> struct remove_pointer<T* const volatile>{
    typedef T type;
};
```

1 type : defined to be a type that is the same as T, except any top level indirection has been removed. Note: pointers to members are left unchanged by remove_pointer.

```
template <class T> struct add_pointer{
    typedef typename remove_extent<
        typename remove_reference<T>::type
        >::type*
    type;
};
```

2 type: defined to be a type that is the same as remove_reference<T>::type* if T is a reference type, otherwise T*.

4.5.5 Other transformations

[tr.meta.trans.other]

```
template <std::size_t Len, std::size_t Align> struct aligned_storage{
    typedef unspecified type;
};
```

1 type: an implementation defined POD type with size *Len* and alignment *Align*, and suitable for use as uninitialized storage for any object of a type whose size is *Len* and whose alignment is *Align*.

4.6 Implementation requirements

[tr.meta.req]

- 1 The behaviour of all the class templates defined in <type_traits> shall conform to the specifications given, except where noted below.
- 2 [Note: The latitude granted to implementers in this clause is temporary, and is expected to be removed in future revisions of this document. —end note]

- 3 If there is no means by which the implementation can differentiate between class and union types, then the class templates `is_class` and `is_union` need not be provided.
- 4 If there is no means by which the implementation can detect polymorphic types, then the class template `is_polymorphic` need not be provided.
- 5 If there is no means by which the implementation can detect abstract types, then the class template `is_abstract` need not be provided.
- 6 It is unspecified under what circumstances, if any, `is_empty<T>::value` evaluates to `true`.
- 7 It is unspecified under what circumstances, if any, `is_pod<T>::value` evaluates to `true`, except that, for all types T:

```
is_pod<T>::value == is_pod<remove_extent<T>::type>::value
is_pod<T>::value == is_pod<T const volatile>::value
is_pod<T>::value >= (is_scalar<T>::value || is_void<T>::value)
```

- 8 It is unspecified under what circumstances, if any, `has_trivial_*<T>::value` evaluates to `true`, except that:

```
has_trivial_*<T>::value ==
    has_trivial_*<remove_extent<T>::type>::value
has_trivial_*<T>::value >=
    is_pod<T>::value
```

- 9 It is unspecified under what circumstances, if any, `has_nothrow_*<T>::value` evaluates to `true`.
- 10 There are trait templates whose semantics do not require their argument(s) to be completely defined, nor does such completeness in any way affect the exact definition of the traits class template specializations. However, in the absence of compiler support these traits cannot be implemented without causing implicit instantiation of their arguments; in particular: `is_class`, `is_enum`, and `is_scalar`. For these templates, it is unspecified whether their template argument(s) are implicitly instantiated when the traits class is itself instantiated.

5 Numerical facilities

[tr.num]

- 1 This clause describes components that C++ programs may use to perform numerical and seminumerical operations.
- 2 The following subclauses describe random number generators and mathematical special functions, as summarized in Table 7.

Table 7: Numerical library summary

Subclause	Header(s)
5.1 Random number generation	<random>
5.2 Mathematical special functions	<cmath> <math.h>

5.1 Random number generation

[tr.rand]

- 1 This subclause defines a facility for generating random numbers.

5.1.1 Requirements

[tr.rand.req]

- 1 In table 8, X denotes a uniform random number generator class returning objects of type T, u is a value of X, and v is a (possibly const) value of X.

Table 8: Uniform random number generator requirements

expression	return type	pre/post-condition	complexity
X::result_type	T	T is an arithmetic type [basic.fundamental]	compile-time
u()	T	—	amortized constant
v.min()	T	Returns a value that is less than or equal to all values potentially returned by operator(). The return value of this function shall not change during the lifetime of v.	constant

expression	return type	pre/post-condition	complexity
v.max()	T	If <code>std::numeric_limits<T>::is_integer</code> , returns a value that is greater than or equal to all values potentially returned by <code>operator()</code> , otherwise, returns a value that is strictly greater than all values potentially returned by <code>operator()</code> . In any case, the return value of this function shall not change during the lifetime of v.	constant

- 2 In table 9, X denotes a pseudo-random number engine class returning objects of type T, t is a value of T, u is a value of X, v is an lvalue of X, g is an lvalue of a zero-argument function object returning values of unsigned integral type, x and y are (possibly const) values of X, os is an lvalue of the type of some class template specialization `basic_ostream<charT, traits>`, and is is an lvalue of the type of some class template specialization `basic_istream<charT, traits>`, where `charT` and `traits` are constrained according to [lib.strings] and [lib.input.output].
- 3 A pseudo-random number engine x has a state `x(i)` at any given time. The specification of each pseudo-random number engines defines the size of its state in multiples of the size of its `result_type`, given as an integral constant expression.

Table 9: Pseudo-random number engine requirements (in addition to uniform random number generator, `CopyConstructible`, and `Assignable`)

expression	return type	pre/post-condition	complexity
X()	—	creates an engine with the same initial state as all other default-constructed engines of type X in the program.	$\mathcal{O}(\text{size of state})$
X(g)	—	creates an engine with the initial internal state given by the results of successive invocations of g. Throws what and when g throws.	$\mathcal{O}(\text{size of state})$
u.seed()	void	post: <code>u == X()</code>	$\mathcal{O}(\text{size of state})$
u.seed(g)	void	post: sets the internal state of u so that <code>u == X(g)</code> . If an invocation of g throws, that exception is rethrown, and further use of u (except destruction) is undefined until a seed member function has been executed without throwing an exception.	same as X(g)

expression	return type	pre/post-condition	complexity
<code>u()</code>	<code>T</code>	given the state $u(i)$ of the engine, computes $u(i+1)$, sets the state to $u(i+1)$, and returns some output dependent on $u(i+1)$	amortized constant
<code>x == y</code>	<code>bool</code>	Given the current state $x(i)$ of x and the current state $y(j)$ of y , returns true if $x(i+k)$ is equal to $y(j+k)$ for all integer $k \geq 0$, false otherwise.	$\mathcal{O}(\text{size of state})$
<code>x != y</code>	<code>bool</code>	$!(x == y)$	$\mathcal{O}(\text{size of state})$
<code>os << x</code>	reference to the type of <code>os</code>	writes the textual representation of the state $x(i)$ of x to <code>os</code> , with <code>os.flags</code> set to <code>ios_base::dec ios_base::fixed ios_base::left</code> and the fill character set to the space character. In the output, adjacent numbers are separated by one or more space characters. post: The <code>os.flags</code> and fill character are unchanged.	$\mathcal{O}(\text{size of state})$
<code>is >> v</code>	reference to the type of <code>is</code>	sets the state $v(i)$ of v as determined by reading its textual representation from <code>is</code> . pre: The textual representation was previously written using an <code>os</code> whose imbued locale and whose type's template specialization arguments <code>charT</code> and <code>traits</code> were the same as those of <code>is</code> . post: The <code>is.flags</code> are unchanged.	$\mathcal{O}(\text{size of state})$

- 4 Additional requirements: The complexity of both copy construction and assignment is $\mathcal{O}(\text{size of state})$.
- 5 For every pseudo-random number engine defined in this clause:
- the constructor template `<class Gen> X(Gen& g)` shall have the same effect as `X(static_cast<Gen>(g))` if `Gen` is a fundamental type.
 - The member function of the form template `<class Gen> void seed(Gen& g)` shall have the same effect as `X(static_cast<Gen>(g))` if `Gen` is a fundamental type.
- 6 [Note: The casts make `g` an rvalue, unsuitable for binding to a reference. —end note]
- 7 If a textual representation was written by `os << x` and that representation was read by `is >> v`, then `x == v`, provided that no intervening invocations of `x` or `v` have occurred.

- 8 In table 10, X denotes a random distribution class returning objects of type T, u is a value of X, x is a (possibly const) value of X, e is an lvalue of an arbitrary type that meets the requirements of a uniform random number generator, returning values of type U, os is an lvalue of the type of some class template specialization `basic_ostream<charT, traits>`, and is is an lvalue of the type of some class template specialization `basic_istream<charT, traits>`, where `charT` and `traits` are constrained according to [lib.strings] and [lib.input.output].

Table 10: Random distribution requirements (in addition to `CopyConstructible`, and `Assignable`)

expression	return type	pre/post-condition	complexity
<code>X::input_type</code>	U	—	compile-time
<code>u.reset()</code>	<code>void</code>	subsequent uses of u do not depend on values produced by e prior to invoking <code>reset</code> .	constant
<code>u(e)</code>	T	the sequence of numbers returned by successive invocations with the same object e is randomly distributed with some probability density function $p(x)$	amortized constant number of invocations of e
<code>os << x</code>	reference to the type of os	writes a textual representation for the parameters and additional internal data of the distribution x to os. post: The os. <code>fmtflags</code> and fill character are unchanged.	$\mathcal{O}(\text{size of state})$
<code>is >> u</code>	reference to the type os	restores the parameters and additional internal data of the distribution u. pre: is provides a textual representation that was previously written using an os whose imbued locale and whose type's template specialization arguments <code>charT</code> and <code>traits</code> were the same than those of is. post: The is. <code>fmtflags</code> are unchanged.	$\mathcal{O}(\text{size of state})$

- 9 Additional requirements: The sequence of numbers produced by repeated invocations of `x(e)` does not change whether or not `os << x` is invoked between any of the invocations `x(e)`. If a textual representation is written using `os << x` and that representation is restored into the same or a different object y of the same type using `is >> y`, repeated invocations of `y(e)` produce the same sequence of random numbers as would repeated invocations of `x(e)`.
- 10 In the following subclauses, a template parameter named `UniformRandomNumberGenerator` shall denote a type that satisfies all the requirements of a uniform random number generator. Moreover, a template parameter named `Distribution` shall denote a type that satisfies all the requirements of a random distribution.
- 11 The effect of instantiating a template that has a template type parameter named `RealType` is undefined unless that type is one of `float`, `double`, or `long double`.

- 12 The effect of instantiating a template that has a template type parameter named `IntType` is undefined unless that type is one of `short`, `int`, `long`, or their unsigned variants.
- 13 The effect of instantiating a template that has a template type parameter named `UIntType` is undefined unless that type is one of `unsigned short`, `unsigned int`, or `unsigned long`.

5.1.2 Header <random> synopsis

[tr.rand.synopsis]

```

namespace tr1 {
    // [5.1.3] Class template variate_generator
    template<class UniformRandomNumberGenerator,
              class Distribution>
    class variate_generator;

    // [5.1.4.1] Class template linear_congruential
    template<class IntType, IntType a, IntType c, IntType m>
    class linear_congruential;

    // [5.1.4.2] Class template mersenne_twister
    template<class UIntType, int w, int n, int m, int r,
              UIntType a, int u, int s,
              UIntType b, int t, UIntType c, int l>
    class mersenne_twister;

    // [5.1.4.3] Class template subtract_with_carry
    template<class IntType, IntType m, int s, int r>
    class subtract_with_carry;

    // [5.1.4.4] Class template subtract_with_carry_01
    template<class RealType, int w, int s, int r>
    class subtract_with_carry_01;

    // [5.1.4.5] Class template discard_block
    template<class UniformRandomNumberGenerator, int p, int r>
    class discard_block;

    // [5.1.4.6] Class template xor_combine
    template<class UniformRandomNumberGenerator1, int s1,
              class UniformRandomNumberGenerator2, int s2>
    class xor_combine;

    // [5.1.6] Class random_device
    class random_device;

    // [5.1.7.1] Class template uniform_int
    template<class IntType = int>
    class uniform_int;

    // [5.1.7.2] Class bernoulli_distribution

```

```

class bernoulli_distribution;

// [5.1.7.3] Class template geometric_distribution
template<class IntType = int, class RealType = double>
class geometric_distribution;

// [5.1.7.4] Class template poisson_distribution
template<class IntType = int, class RealType = double>
class poisson_distribution;

// [5.1.7.5] Class template binomial_distribution
template<class IntType = int, class RealType = double>
class binomial_distribution;

// [5.1.7.6] Class template uniform_real
template<class RealType = double>
class uniform_real;

// [5.1.7.7] Class template exponential_distribution
template<class RealType = double>
class exponential_distribution;

// [5.1.7.8] Class template normal_distribution
template<class RealType = double>
class normal_distribution;

// [5.1.7.9] Class template gamma_distribution
template<class RealType = double>
class gamma_distribution;

} // namespace tr1

```

5.1.3 Class template variate_generator

[tr.rand.var]

- 1 A variate_generator produces random numbers, drawing randomness from an underlying uniform random number generator and shaping the distribution of the numbers corresponding to a distribution function.

```

template<class Engine, class Distribution>
class variate_generator
{
public:
    typedef Engine engine_type;
    typedef implementation defined engine_value_type;
    typedef Distribution distribution_type;
    typedef typename Distribution::result_type result_type;

    variate_generator(engine_type eng, distribution_type d);

    result_type operator()();
    template<class T> result_type operator()(T value);

```

```

engine_value_type& engine();
const engine_value_type& engine() const;

distribution_type& distribution();
const distribution_type& distribution() const;

result_type min() const;
result_type max() const;
};

```

- 2 The template argument for the parameter Engine shall be of the form U , $U\&$, or $U*$, where U denotes a class that satisfies all the requirements of a uniform random number generator. The member `engine_value_type` shall name U .
- 3 Specializations of `variate_generator` satisfy the requirements of `CopyConstructible` and `Assignable`.
- 4 Except where specified otherwise, the complexity of all functions specified in this section is constant. No function described in this section except the constructor throws an exception.

`variate_generator(engine_type eng, distribution_type d)`

- 5 *Effects:* Constructs a `variate_generator` object with the associated uniform random number generator `eng` and the associated random distribution `d`.
- 6 *Complexity:* Sum of the complexities of the copy constructors of `engine_type` and `distribution_type`.
- 7 *Throws:* If and what the copy constructor of `Engine` or `Distribution` throws.

`result_type operator()()`

- 8 *Returns:* `distribution()(e)`
- 9 *Complexity:* Amortized constant.

- 10 *Notes:* The sequence of numbers produced by the uniform random number generator `e`, `se`, is obtained from the sequence of numbers produced by the associated uniform random number generator `eng`, `seng`, as follows: Consider the values of `numeric_limits<T>::is_integer` for T both `Distribution::input_type` and `engine_value_type::result_type`. If the values for both types are true, then `se` is identical to `seng`. Otherwise, if the values for both types are false, then the numbers in `seng` are divided by `engine().max() - engine().min()` to obtain the numbers in `se`. Otherwise, if the value for `engine_value_type::result_type` is true and the value for `Distribution::input_type` is false, then the numbers in `seng` are divided by `engine().max() - engine().min() + 1` to obtain the numbers in `se`. Otherwise, the mapping from `seng` to `se` is implementation-defined. In all cases, an implicit conversion from `engine_value_type::result_type` to `Distribution::input_type` is performed. If such a conversion does not exist, the program is ill-formed.

`template<class T> result_type operator()(T value)`

- 11 *Returns:* `distribution()(e, value)`. For the semantics of `e`, see the description of `operator()()`.
- 12 *Returns:* A reference to the associated uniform random number generator.

```

const engine_value_type& engine() const
13   Returns: A reference to the associated uniform random number generator.

distribution_type& distribution()

14   Returns: A reference to the associated random distribution.

const distribution_type& distribution() const
15   Returns: A reference to the associated random distribution.

result_type min() const
16   Precondition: distribution().min() is well-formed.

17   Returns: distribution().min()

result_type max() const
18   Precondition: distribution().max() is well-formed
19   Returns: distribution().max()

```

5.1.4 Random number engine class templates

[tr.rand.eng]

- 1 Except where specified otherwise, the complexity of all functions specified in the following sections is constant. No function described in this section, except the constructor and seed functions taking a zero-argument function object, throws an exception.
- 2 The class templates specified in this section satisfy all the requirements of a pseudo-random number engine (given in table 9), except where specified otherwise. Descriptions are provided here only for operations on the engines that are not described in one of these tables or for operations where there is additional semantic information.
- 3 All members declared `static const` in any of the following class templates shall be defined in such a way that they are usable as integral constant expressions.

5.1.4.1 Class template linear_congruential

[tr.rand.eng.lcong]

- 1 A `linear_congruential` engine produces random numbers using a linear function $x(i+1) := (a * x(i) + c) \bmod m$.

```

namespace tr1 {
    template<class UIntType, UIntType a, UIntType c, UIntType m>
    class linear_congruential
    {
    public:
        // types
        typedef UIntType result_type;

        // parameter values
        static const UIntType multiplier = a;
        static const UIntType increment = c;
        static const UIntType modulus = m;
    };
}

```

```
// constructors and member function
explicit linear_congruential(UIntType x0 = 1);
template<class Gen> linear_congruential(Gen& g);
void seed(UIntType x0 = 1);
template<class Gen> void seed(Gen& g);
result_type min() const;
result_type max() const;
result_type operator()();
};

}
```

- 2 The template parameter `UIntType` shall denote an unsigned integral type large enough to store values up to $(m-1)$. If the template parameter `m` is 0, the modulus `m` used throughout this section is `std::numeric_limits<UIntType>::max()` plus 1. [Note: The result is not representable as a value of type `UIntType`. —end note] Otherwise, the template parameters `a` and `c` shall be less than `m`.
- 3 The size of the state `x(i)` is 1. The textual representation is the value of `x(i)`.

`explicit linear_congruential(UIntType x0 = 1)`

- 4 *Effects:* Constructs a `linear_congruential` engine and invokes `seed(x0)`.

`void seed(UIntType x0 = 1)`

- 5 *Effects:* If $c \bmod m = 0$ and $x0 \bmod m = 0$, sets the state `x(i)` of the engine to $1 \bmod m$, else sets the state of the engine to $x0 \bmod m$.

`template<class Gen> linear_congruential(Gen& g)`

- 6 *Effects:* If $c \bmod m = 0$ and `g()` $\bmod m = 0$, sets the state `x(i)` of the engine to $1 \bmod m$, else sets the state of the engine to `g()` $\bmod m$.

- 7 *Complexity:* Exactly one invocation of `g`.

5.1.4.2 Class template `mersenne_twister`

[tr.rand.eng.mers]

- 1 A `mersenne_twister` engine produces random numbers `o(x(i))` using the following computation, performed modulo 2^w . `um` is a value with only the upper $w-r$ bits set in its binary representation. `lm` is a value with only its lower r bits set in its binary representation. `rshift` is a bitwise right shift with zero-valued bits appearing in the high bits of the result. `lshift` is a bitwise left shift with zero-valued bits appearing in the low bits of the result.

- $y(i) = (x(i-n) \text{ bitand } um) | (x(i-(n-1)) \text{ bitand } lm)$
- If the lowest bit of the binary representation of $y(i)$ is set, $x(i) = x(i-(n-m)) \text{ xor } (y(i) \text{ rshift } 1) \text{ xor } a$; otherwise $x(i) = x(i-(n-m)) \text{ xor } (y(i) \text{ rshift } 1)$.
- $z1(i) = x(i) \text{ xor } (x(i) \text{ rshift } u)$
- $z2(i) = z1(i) \text{ xor } ((z1(i) \text{ lshift } s) \text{ bitand } b)$
- $z3(i) = z2(i) \text{ xor } ((z2(i) \text{ lshift } t) \text{ bitand } c)$
- $o(x(i)) = z3(i) \text{ xor } (z3(i) \text{ rshift } 1)$

```

template<class UIntType, int w, int n, int m, int r,
         UIntType a, int u, int s,
         UIntType b, int t, UIntType c, int l>
class mersenne_twister
{
public:
    // types
    typedef UIntType result_type;

    // parameter values
    static const int word_size = w;
    static const int state_size = n;
    static const int shift_size = m;
    static const int mask_bits = r;
    static const UIntType parameter_a = a;
    static const int output_u = u;
    static const int output_s = s;
    static const UIntType output_b = b;
    static const int output_t = t;
    static const UIntType output_c = c;
    static const int output_l = l;

    // constructors and member function
    mersenne_twister();
    explicit mersenne_twister(unsigned long value);
    template<class Gen> mersenne_twister(Gen& g);
    void seed();
    void seed(unsigned long value);
    template<class Gen> void seed(Gen& g);
    result_type min() const;
    result_type max() const;
    result_type operator()();
};


```

- 2 The template parameter UIntType shall denote an unsigned integral type large enough to store values up to $2^w - 1$. Also, the following relations shall hold: $1 \leq m \leq n$. $0 \leq r, u, s, t, l \leq w$. $0 \leq a, b, c \leq 2^w - 1$.
- 3 The size of the state $x(i)$ is n . The textual representation is the values of $x(i-n), \dots, x(i-1)$, in that order.

`mersenne_twister()`

- 4 *Effects:* Constructs a `mersenne_twister` engine and invokes `seed()`.

`explicit mersenne_twister(unsigned long value)`

- 5 *Effects:* Constructs a `mersenne_twister` engine and invokes `seed(value)`.

`template<class Gen> mersenne_twister(Gen& g)`

- 6 *Effects:* Given the values $z_0 \dots z_{n-1}$ obtained by successive invocations of `g`, sets $x(-n) \dots x(-1)$ to $z_0 \bmod 2^w \dots z_{n-1} \bmod 2^w$.

7 *Complexity:* Exactly n invocations of g.

```
void seed()
```

8 *Effects:* Invokes seed(0).

```
void seed(unsigned long value)
```

9 *Effects:* If value == 0, sets value to 4357. In any case, with a linear congruential generator lcg(i) having parameters $m_{lcg} = 2^32$, $a_{lcg} = 69069$, $c_{lcg} = 0$, and $lcg(0) = \text{value}$, sets $x(-n) \dots x(-1)$ to $lcg(1) \dots lcg(n)$, respectively.

10 *Complexity:* $\mathcal{O}(n)$

```
template<class UIntType, int w, int n, int m, int r,
         UIntType a, int u, int s,
         UIntType b, int t, UIntType c, int l>
bool
operator==(const mersenne_twister<UIntType,
             w,n,m,r,a,u,s,b,t,c,l>& y,
             const mersenne_twister<UIntType,
             w,n,m,r,a,u,s,b,t,c,l>& x)
```

11 *Returns:* $x(i-n) == y(j-n)$ and ... and $x(i-1) == y(j-1)$

12 *Notes:* Assumes the next output of x is o(x(i)) and the next output of y is o(y(j)).

13 *Complexity:* $\mathcal{O}(n)$

5.1.4.3 Class template subtract_with_carry

[tr.rand.eng.sub]

1 A subtract_with_carry engine produces integer random numbers using the computation $x(i) = (x(i-s) - x(i-r) - \text{carry}(i-1)) \bmod m$ and setting $\text{carry}(i) = 1$ if $x(i-s) - x(i-r) - \text{carry}(i-1) < 0$, else $\text{carry}(i) = 0$.

```
template<class IntType, IntType m, int s, int r>
class subtract_with_carry
{
public:
    // types
    typedef IntType result_type;

    // parameter values
    static const IntType modulus = m;
    static const int long_lag = r;
    static const int short_lag = s;

    // constructors and member function
    subtract_with_carry();
    explicit subtract_with_carry(unsigned long value);
    template<class Gen> subtract_with_carry(Gen& g);
    void seed(unsigned long value = 19780503ul);
    template<class Gen> void seed(Gen& g);
```

```

    result_type min() const;
    result_type max() const;
    result_type operator()();
};


```

- 2 The template parameter `IntType` shall denote a signed integral type large enough to store values up to `m`. The following relation shall hold: $0 < s < r$. Let `w` the number of bits in the binary representation of `m`.
- 3 The size of the state is `r`. The textual representation is the values of $x(i-r), \dots, x(i-1)$, $\text{carry}(i-1)$, in that order.

`subtract_with_carry()`

- 4 *Effects:* Constructs a `subtract_with_carry` engine and invokes `seed()`.

```
explicit subtract_with_carry(unsigned long value)
```

- 5 *Effects:* Constructs a `subtract_with_carry` engine and invokes `seed(value)`.

```
template<class Gen> subtract_with_carry(Gen& g)
```

- 6 *Effects:* With $n = (w + 31)/32$ (rounded downward) and given the values $z_0 \dots z_{n*r-1}$ obtained by successive invocations of `g`, sets $x(-r) \dots x(-1)$ to $(z_0 \cdot 2^{32}) + \dots + z_{n-1} \cdot 2^{32(n-1)}) \bmod m \dots (z_{(r-1)n} \cdot 2^{32} + \dots + z_{(r-1)}) \cdot 2^{32(n-1)}) \bmod m$. If $x(-1) == 0$, sets `carry(-1) = 1`, else sets `carry(-1) = 0`.

- 7 *Complexity:* Exactly $r*n$ invocations of `g`.

```
void seed(unsigned long value = 19780503)
```

- 8 *Effects:* If `value == 0`, sets `value` to 19780503. In any case, with a linear congruential generator `lcg(i)` having parameters $m_{lcg} = 2147483563$, $a_{lcg} = 40014$, $c_{lcg} = 0$, and $lcg(0) = value$, sets $x(-r) \dots x(-1)$ to $lcg(1) \bmod m \dots lcg(r) \bmod m$, respectively. If $x(-1) == 0$, sets `carry(-1) = 1`, else sets `carry(-1) = 0`.

- 9 *Complexity:* $\mathcal{O}(r)$

```
template<class IntType, IntType m, int s, int r>
bool operator==(const subtract_with_carry<IntType, m, s, r> & x,
                  const subtract_with_carry<IntType, m, s, r> & y)
```

- 10 *Returns:* $x(i-r) == y(j-r)$ and ... and $x(i-1) == y(j-1)$.

- 11 *Notes:* Assumes the next output of `x` is `x(i)` and the next output of `y` is `y(j)`.

- 12 *Complexity:* $\mathcal{O}(r)$

5.1.4.4 Class template `subtract_with_carry_01`

[tr.rand.eng.sub1]

- 1 A `subtract_with_carry_01` engine produces floating-point random numbers using $x(i) = (x(i-s) - x(i-r) - \text{carry}(i-1)) \bmod 1$; and setting `carry(i) = 2^{-w}` if $x(i-s) - x(i-r) - \text{carry}(i-1) < 0$, else `carry(i) = 0`.

```
template<class RealType, int w, int s, int r>
class subtract_with_carry_01
{
```

```

public:
    // types
    typedef RealType result_type;

    // parameter values
    static const int word_size = w;
    static const int long_lag = r;
    static const int short_lag = s;

    // constructors and member function
    subtract_with_carry_01();
    explicit subtract_with_carry_01(unsigned long value);
    template<class Gen> subtract_with_carry_01(Gen& g);
    void seed(unsigned long value = 19780503);
    template<class Gen> void seed(Gen& g);
    result_type min() const;
    result_type max() const;
    result_type operator()();
};


```

- 2 The following relation shall hold: $0 < s < r$.
- 3 The size of the state is r . With $n = (w + 31)/32$ (rounded downward) and integer numbers $z[k, j]$ such that $x(i - k) * 2^w = z[k, 0] + z[k, 1] * 2^{32} + z[k, n - 1] * 2^{32}(n - 1)$, the textual representation is the values of $z[r, 0], \dots, z[r, n - 1], \dots, z[1, 0], \dots, z[1, n - 1]$, $\text{carry}(i - 1) * 2^w$, in that order. [Note: The algorithm ensures that only integer numbers representable in 32 bits are written. —end note]

`subtract_with_carry_01()`

- 4 *Effects:* Constructs a `subtract_with_carry_01` engine and invokes `seed()`.

`explicit subtract_with_carry_01(unsigned long value)`

- 5 *Effects:* Constructs a `subtract_with_carry_01` engine and invokes `seed(value)`.

`template<class Gen> subtract_with_carry_01(Gen& g)`

- 6 *Effects:* With $n = (w + 31)/32$ (rounded downward) and given the values $z_0 \dots z_{n-r-1}$ obtained by successive invocations of g , sets $x(-r) \dots x(-1)$ to $(z_0 \cdot 2^{32} + \dots + z_{n-1} \cdot 2^{32(n-1)}) \cdot 2^{-w} \bmod 1 \dots (z_{(r-1)n} \cdot 2^{32} + \dots + z_{r-1} \cdot 2^{32(n-1)}) \cdot 2^{-w} \bmod 1$. If $x(-1) == 0$, sets $\text{carry}(-1) = 2^{-w}$, else sets $\text{carry}(-1) = 0$.

- 7 *Complexity:* Exactly $r*n$ invocations of g .

`void seed(unsigned long value = 19780503)`

- 8 *Effects:* If $\text{value} == 0$, sets value to 19780503. In any case, with a linear congruential generator $\text{lcg}(i)$ having parameters $m_{\text{lcg}} = 2147483563$, $a_{\text{lcg}} = 40014$, $c_{\text{lcg}} = 0$, and $\text{lcg}(0) = \text{value}$, sets $x(-r) \dots x(-1)$ to $(\text{lcg}(1) \cdot 2^{-w}) \bmod 1 \dots (\text{lcg}(r) \cdot 2^{-w} \bmod 1$, respectively. If $x(-1) == 0$, sets $\text{carry}(-1) = 2^{-w}$, else sets $\text{carry}(-1) = 0$.

- 9 *Complexity:* $\mathcal{O}(n \cdot r)$.

`template<class RealType, int w, int s, int r>`

```

bool operator==(const subtract_with_carry<RealType, w, s, r> x,
                  const subtract_with_carry<RealType, w, s, r> y);

```

10 *Returns:* true, if and only if $x(i-r) == y(j-r)$ and ... and $x(i-1) == y(j-1)$.

11 *Complexity:* $\mathcal{O}(r)$

5.1.4.5 Class template `discard_block`

[tr.rand.eng.disc]

- 1 A `discard_block` engine produces random numbers from some base engine by discarding blocks of data.

```

template<class UniformRandomNumberGenerator, int p, int r>
class discard_block
{
public:
    // types
    typedef UniformRandomNumberGenerator base_type;
    typedef typename base_type::result_type result_type;

    // parameter values
    static const int block_size = p;
    static const int used_block = r;

    // constructors and member function
    discard_block();
    explicit discard_block(const base_type & rng);
    template<class Gen> discard_block(Gen& g);
    void seed();
    template<class Gen> void seed(Gen& g);
    const base_type& base() const;
    result_type min() const;
    result_type max() const;
    result_type operator()();
private:
    base_type b;                                // exposition only
    int n;                                       // exposition only
};

```

- 2 The template parameter `UniformRandomNumberGenerator` shall denote a class that satisfies all the requirements of a uniform random number generator, given in table 8 in clause 5.1.1. $0 \leq r \leq p$. The size of the state is the size of `b` plus 1. The textual representation is the textual representation of `b` followed by the value of `n`.

```

discard_block()

3   Effects: Constructs a discard_block engine. To construct the subobject b, invokes its default constructor. Sets n = 0.

explicit discard_block(const base_type & rng)

4   Effects: Constructs a discard_block engine. Initializes b with a copy of rng. Sets n = 0.

```

```

template<class Gen> discard_block(Gen)

5      Effects: Constructs a discard_block engine. To construct the subobject b, invokes the b(g) constructor. Sets n = 0.

void seed()

6      Effects: Invokes b.seed() and sets n = 0.

const base_type& base() const

7      Returns: b

result_type operator()()

8      Effects: If n >= r, invokes b (p-r) times, discards the values returned, and sets n = 0. In any case, then increments n and returns b().

```

5.1.4.6 Class template xor_combine

[tr.rand.eng.xor]

- 1 A `xor_combine` engine produces random numbers from two integer base engines by merging their random values with bitwise exclusive-or.

```

template<class UniformRandomNumberGenerator1, int s1,
         class UniformRandomNumberGenerator2, int s2>
class xor_combine
{
public:
    // types
    typedef UniformRandomNumberGenerator1 base1_type;
    typedef UniformRandomNumberGenerator2 base2_type;
    typedef see below result_type;

    // parameter values
    static const int shift1 = s1;
    static const int shift2 = s2;

    // constructors and member function
    xor_combine();
    xor_combine(const base1_type & rng1, const base2_type & rng2);
    template<class Gen> xor_combine(Gen& g);
    void seed();
    template<class Gen> void seed(Gen& g);
    const base1_type& base1() const;
    const base2_type& base2() const;
    result_type min() const;
    result_type max() const;
    result_type operator()();
private:
    base1_type b1;           // exposition only
    base2_type b2;           // exposition only

```

};

- 2 The template parameters `UniformRandomNumberGenerator1` and `UniformRandomNumberGenerator2` shall denote classes that satisfy all the requirements of a uniform random number generator, given in table 8 in clause 5.1.1. Both `UniformRandomNumberGenerator1::result_type` and `UniformRandomNumberGenerator2::result_type` shall denote (possibly different) unsigned integral types. The following relation shall hold: $0 \leq s1$ and $0 \leq s2$. The size of the state is the size of the state of `b1` plus the size of the state of `b2`. The textual representation is the textual representation of `b1` followed by the textual representation of `b2`.
- 3 The member `result_type` is defined to be either the type `UniformRandomNumberGenerator1 ::result_type` or the type `UniformRandomNumberGenerator2 ::result_type`, whichever one provides the most storage. (As defined in clause [basic.fundamental].)

`xor_combine()`

- 4 *Effects:* Constructs a `xor_combine` engine. To construct each of the subobjects `b1` and `b2`, invokes their respective default constructors.

`xor_combine(const base1_type & rng1, const base2_type & rng2)`

- 5 *Effects:* Constructs a `xor_combine` engine. Initializes `b1` with a copy of `rng1` and `b2` with a copy of `rng2`.

`template<class Gen> xor_combine(Gen& g)`

- 6 *Effects:* Constructs a `xor_combine` engine. To construct the subobject `b1`, invokes the `b1(g)` constructor. Then, to construct the subobject `b2`, invokes the `b2(g)` constructor.

`void seed()`

- 7 *Effects:* Invokes `b1.seed()` and `b2.seed()`.

`const base1_type& base1() const`

- 8 *Returns:* `b1`

`const base2_type& base2() const`

- 9 *Returns:* `b2`

`result_type operator()()`

- 10 *Returns:* $(b1() \ll s1) \wedge (b2() \ll s2)$.

- 11 *[Note:* Two shift values are provided for simplicity of interface. When using this class template, however, it is advisable for at most one of these values to be nonzero. If both `s1` and `s2` are nonzero then the low bits will always be zero. —end note]

5.1.5 Engines with predefined parameters

[`tr.rand.predef`]

```
typedef linear_congruential<implementation-defined,
                           16807, 0, 2147483647>
                           minstd_rand0;
```

```

typedef linear_congruential<implementation-defined,
                           48271, 0, 2147483647>
                           minstd_rand;

typedef mersenne_twister<implementation-defined,
                           32,624,397,31,0x9908b0df,11,7,0x9d2c5680,15,0xfc60000,18>
                           mt19937;

typedef subtract_with_carry_01<float, 24, 10, 24> ranlux_base_01;
typedef subtract_with_carry_01<double, 48, 10, 24> ranlux64_base_01;

typedef discard_block<subtract_with_carry<implementation-defined,
                           (1<<24), 10, 24>, 223, 24>
                           ranlux3;
typedef discard_block<subtract_with_carry<implementation-defined,
                           (1<<24), 10, 24>, 389, 24>
                           ranlux4;

typedef discard_block<subtract_with_carry_01<float, 24, 10, 24>, 223, 24>
                           ranlux3_01;
typedef discard_block<subtract_with_carry_01<float, 24, 10, 24>, 389, 24>
                           ranlux4_01;

```

- 1 For a default-constructed `minstd_rand0` object, $x(10000) = 1043618065$. For a default-constructed `minstd_rand` object, $x(10000) = 399268537$.
- 2 For a default-constructed `mt19937` object, $x(10000) = 3346425566$.
- 3 For a default-constructed `ranlux3` object, $x(10000) = 5957620$. For a default-constructed `ranlux4` object, $x(10000) = 8587295$. For a default-constructed `ranlux3_01` object, $x(10000) = 5957620 \cdot 2^{-24}$. For a default-constructed `ranlux4_01` object, $x(10000) = 8587295 \cdot 2^{-24}$.

5.1.6 Class random_device

[tr.rand.device]

- 1 A `random_device` produces non-deterministic random numbers. It satisfies all the requirements of a uniform random number generator (given in table 8 in clause 5.1.1). Descriptions are provided here only for operations on the engines that are not described in one of these tables or for operations where there is additional semantic information.
- 2 If implementation limitations prevent generating non-deterministic random numbers, the implementation can employ a pseudo-random number engine.

```

class random_device
{
public:
    // types
    typedef unsigned int result_type;

    // constructors, destructors and member functions
    explicit random_device(const std::string& token = implementation-defined);
    result_type min() const;
    result_type max() const;

```

```

    double entropy() const;
    result_type operator()();

private:
    random_device(const random_device& );
    void operator=(const random_device& );
};

explicit random_device(const std::string& token = implementation-defined);

3   Effects: Constructs a random_device non-deterministic random number engine. The semantics and default value
   of the token parameter are implementation-defined.1)

4   Throws: A value of some type derived from exception if the random_device could not be initialized.

result_type min() const
5   Returns: numeric_limits<result_type>::min()

result_type max() const
6   Returns: numeric_limits<result_type>::max()

double entropy() const
7   Returns: An entropy estimate for the random numbers returned by operator(), in the range min() to log2(max() +
   1). A deterministic random number generator (e.g. a pseudo-random number engine) has entropy 0.

8   Throws: Nothing.

result_type operator()()
9   Returns: A non-deterministic random value, uniformly distributed between min() and max(), inclusive. It is
   implementation-defined how these values are generated.

10  Throws: A value of some type derived from exception if a random number could not be obtained.

```

5.1.7 Random distribution class templates

[tr.rand.dist]

- 1 The class templates specified in this section satisfy all the requirements of a random distribution (given in tables in clause 5.1.1). Descriptions are provided here only for operations on the distributions that are not described in one of these tables or for operations where there is additional semantic information.
- 2 Given an object whose type is specified in this subclause, if the lifetime of the uniform random number generator referred to in the constructor invocation for that object has ended, any use of that object is undefined.
- 3 The algorithms for producing each of the specified distributions are implementation-defined.

5.1.7.1 Class template uniform_int

[tr.rand.dist.iunif]

- 1 A uniform_int random distribution produces integer random numbers x in the range $\min \leq x \leq \max$, with equal probability. \min and \max are the parameters of the distribution.

¹⁾ The parameter is intended to allow an implementation to differentiate between different sources of randomness.

- 2 A `uniform_int` random distribution satisfies all the requirements of a uniform random number generator (given in table 8 in clause 5.1.1).

```

template<class IntType = int>
class uniform_int
{
public:
    // types
    typedef IntType input_type;
    typedef IntType result_type;

    // constructors and member function
    explicit uniform_int(IntType min = 0, IntType max = 9);
    result_type min() const;
    result_type max() const;
    void reset();

    template<class UniformRandomNumberGenerator>
    result_type
    operator()(UniformRandomNumberGenerator& urng);
    template<class UniformRandomNumberGenerator>
    result_type
    operator()(UniformRandomNumberGenerator& urng, result_type n);
};

uniform_int(IntType min = 0, IntType max = 9)

```

3 *Requires:* $\min \leq \max$

4 *Effects:* Constructs a `uniform_int` object. `min` and `max` are the parameters of the distribution.

`result_type min() const`

5 *Returns:* The “`min`” parameter of the distribution.

`result_type max() const`

6 *Returns:* The “`max`” parameter of the distribution.

`result_type`
`operator()(UniformRandomNumberGenerator& urng, result_type n)`

7 *Returns:* A uniform random number x in the range $0 \leq x < n$. [Note: This allows a `variate_generator` object with a `uniform_int` distribution to be used with `std::random_shuffle`, see [lib.alg.random.shuffle]. —end note]

5.1.7.2 Class `bernoulli_distribution`

[tr.rand.dist.bern]

- 1 A `bernoulli_distribution` random distribution produces `bool` values distributed with probabilities $p(\text{true}) = p$ and $p(\text{false}) = 1-p$. p is the parameter of the distribution.

```

class bernoulli_distribution
{
public:
    // types
    typedef int input_type;
    typedef bool result_type;

    // constructors and member function
    explicit bernoulli_distribution(double p = 0.5);
    RealType p() const;
    void reset();
    template<class UniformRandomNumberGenerator>
    result_type operator()(UniformRandomNumberGenerator& urng);
};

bernoulli_distribution(double p = 0.5)

2      Requires:  $0 \leq p \leq 1$ 
3      Effects: Constructs a bernoulli_distribution object. p is the parameter of the distribution.

RealType p() const
4      Returns: The “p” parameter of the distribution.

```

5.1.7.3 Class template geometric_distribution

[tr.rand.dist.geom]

- 1 A geometric_distribution random distribution produces integer values $i > 1$ with $p(i) = (1 - p) \cdot p^{i-1}$. p is the parameter of the distribution.

```

template<class IntType = int, class RealType = double>
class geometric_distribution
{
public:
    // types
    typedef RealType input_type;
    typedef IntType result_type;

    // constructors and member function
    explicit geometric_distribution(const RealType& p = RealType(0.5));
    RealType p() const;
    void reset();
    template<class UniformRandomNumberGenerator>
    result_type operator()(UniformRandomNumberGenerator& urng);
};

geometric_distribution(const RealType& p = RealType(0.5))

2      Requires:  $0 < p < 1$ 
3      Effects: Constructs a geometric_distribution object; p is the parameter of the distribution.

```

```
RealType p() const
4      Returns: The “p” parameter of the distribution.
```

5.1.7.4 Class template poisson_distribution

[tr.rand.dist.pois]

- 1 A `poisson_distribution` random distribution produces integer values $i > 0$ with probability distribution

$$p(i) = \frac{\text{mean}^i}{i!} e^{-\text{mean}},$$

where *mean* is the parameter of the distribution.

```
template<class IntType = int, class RealType = double>
class poisson_distribution
{
public:
    // types
    typedef RealType input_type;
    typedef IntType result_type;

    // constructors and member function
    explicit poisson_distribution(const RealType& mean = RealType(1));
    RealType mean() const;
    void reset();
    template<class UniformRandomNumberGenerator>
    result_type operator()(UniformRandomNumberGenerator& urng);
};

poisson_distribution(const RealType& mean = RealType(1))
```

- 2 *Requires:* *mean* > 0

- 3 *Effects:* Constructs a `poisson_distribution` object; *mean* is the parameter of the distribution.

```
RealType mean() const
4      Returns: The mean parameter of the distribution.
```

5.1.7.5 Class template binomial_distribution

[tr.rand.dist.bin]

- 1 A `binomial_distribution` random distribution produces integer values $i > 0$ with

$$p(i) = \binom{n}{i} \cdot p^i \cdot (1-p)^{t-i},$$

where *t* and *p* are the parameters of the distribution.

```
template<class IntType = int, class RealType = double>
class binomial_distribution
{
```

```

public:
    // types
    typedef implementation-defined input_type;
    typedef IntType result_type;

    // constructors and member function
    explicit binomial_distribution(IntType t = 1,
                                    const RealType& p = RealType(0.5));
    IntType t() const;
    RealType p() const;
    void reset();
    template<class UniformRandomNumberGenerator>
    result_type operator()(UniformRandomNumberGenerator& urng);
};

binomial_distribution(IntType t = 1, const RealType& p = RealType(0.5))

2   Requires:  $0 \leq p \leq 1$  and  $t \geq 0$ .
3   Effects: Constructs a binomial_distribution object; t and p are the parameters of the distribution.
4   IntType t() const
5   Returns: The “t” parameter of the distribution.
6   RealType p() const
7   Returns: The “p” parameter of the distribution.

```

5.1.7.6 Class template uniform_real

[tr.rand.dist.runif]

- 1 A uniform_real random distribution produces floating-point random numbers x in the range $\min \leq x < \max$, with equal probability. \min and \max are the parameters of the distribution.
- 2 A uniform_real random distribution satisfies all the requirements of a uniform random number generator (given in table 8 in clause 5.1.1).

```

template<class RealType = double>
class uniform_real
{
public:
    // types
    typedef RealType input_type;
    typedef RealType result_type;

    // constructors and member function
    explicit uniform_real(RealType min = RealType(0),
                          RealType max = RealType(1));
    result_type min() const;
    result_type max() const;
    void reset();

```

```
template<class UniformRandomNumberGenerator>
result_type operator()(UniformRandomNumberGenerator& urng);
};
```

`uniform_real(RealType min = RealType(0), RealType max = RealType(1))`

3 *Requires:* $\min \leq \max$.

4 *Effects:* Constructs a `uniform_real` object; `min` and `max` are the parameters of the distribution.

5 `result_type min() const`

5 *Returns:* The “min” parameter of the distribution.

5 `result_type max() const`

6 *Returns:* The “max” parameter of the distribution.

5.1.7.7 Class template `exponential_distribution`

[tr.rand.dist.exp]

1 An `exponential_distribution` random distribution produces random numbers $x > 0$ distributed with probability density function

$$p(x) = \lambda e^{-\lambda x},$$

where λ is the parameter of the distribution.

```
template<class RealType = double>
class exponential_distribution
{
public:
    // types
    typedef RealType input_type;
    typedef RealType result_type;

    // constructors and member function
    explicit exponential_distribution(
        const result_type& lambda = result_type(1));
    RealType lambda() const;
    void reset();
    template<class UniformRandomNumberGenerator>
    result_type operator()(UniformRandomNumberGenerator& urng);
};
```

`exponential_distribution(const result_type& lambda = result_type(1))`

2 *Requires:* $\lambda > 0$.

3 *Effects:* Constructs an `exponential_distribution` object with `rng` as the reference to the underlying source of random numbers. `lambda` is the parameter for the distribution.

`RealType lambda() const`

- 4 *Returns:* The “ λ ” parameter of the distribution.

5.1.7.8 Class template normal_distribution

[tr.rand.dist.norm]

- 1 A `normal_distribution` random distribution produces random numbers x distributed with probability density function

$$p(x) = \frac{\sigma}{\sqrt{2\pi}} e^{-(x-\text{mean})^2/(2\sigma^2)},$$

where `mean` and σ are the parameters of the distribution.

```
template<class RealType = double>
class normal_distribution
{
public:
    // types
    typedef RealType input_type;
    typedef RealType result_type;

    // constructors and member functions
    explicit normal_distribution(const result_type& mean = 0,
                                const result_type& sigma = 1);
    RealType mean() const;
    RealType sigma() const;
    void reset();
    template<class UniformRandomNumberGenerator>
    result_type operator()(UniformRandomNumberGenerator& urng);
};

explicit normal_distribution(const result_type& mean = 0,
                            const result_type& sigma = 1);
```

- 2 *Requires:* $\sigma > 0$.

- 3 *Effects:* Constructs a `normal_distribution` object; `mean` and `sigma` are the parameters for the distribution.

`RealType mean() const`

Returns: The “`mean`” parameter of the distribution.

`RealType sigma() const`

- 4 *Returns:* The “ σ ” parameter of the distribution.

5.1.7.9 Class template gamma_distribution

[tr.rand.dist.gamma]

- 1 A `gamma_distribution` random distribution produces random numbers x distributed with probability density function

$$p(x) = \frac{1}{\Gamma(\alpha)} x^{\alpha-1} e^{-x},$$

where α is the parameter of the distribution.

```

template<class RealType = double>
class gamma_distribution
{
public:
    // types
    typedef RealType input_type;
    typedef RealType result_type;

    // constructors and member function
    explicit gamma_distribution(const result_type& alpha = result_type(1));
    RealType alpha() const;
    void reset();
    template<class UniformRandomNumberGenerator>
    result_type operator()(UniformRandomNumberGenerator& urng);
};

explicit gamma_distribution(const result_type& alpha = result_type(1));

```

2 *Requires:* $\alpha > 0$.

3 *Effects:* Constructs a `gamma_distribution` object; α is the parameter for the distribution.

`RealType alpha() const`

4 *Returns:* The “ α ” parameter of the distribution.

5.2 Mathematical special functions

[tr.num.sf]

5.2.1 Additions to header `<cmath>` synopsis

[tr.num.sf.cmath]

1 Table 11 summarizes the functions that are added to header `<cmath>`. The detailed signatures are given in the synopsis.

Table 11: Additions to header `<cmath>` synopsis

Type	Name(s)
Functions:	
assoc_laguerre	conf_hyperg
assoc_legendre	cyl_bessel_i
beta	cyl_bessel_j
comp_ellint_1	cyl_bessel_k
comp_ellint_2	cyl_neumann
comp_ellint_3	ellint_1
	ellint_2
	ellint_3
	expint
	hermite
	hyperg
	laguerre
	legendre
	riemann_zeta
	sph_bessel
	sph_legendre
	sph_neumann

2 Each of these functions is provided for arguments of type `float`, `double`, and `long double`. The signatures added to header `<cmath>` are:

```

namespace std {
namespace tr1 {
// [5.2.1.1] associated Laguerre polynomials:
double assoc_laguerre(unsigned n, unsigned m, double x);

```

```

float      assoc_laguerref(unsigned n, unsigned m, float x);
long double assoc_laguerrel(unsigned n, unsigned m, long double x);

// [5.2.1.2] associated Legendre functions:
double      assoc_legendre(unsigned l, unsigned m, double x);
float       assoc_legendref(unsigned l, unsigned m, float x);
long double assoc_legendrel(unsigned l, unsigned m, long double x);

// [5.2.1.3] beta function:
double      beta(double x, double y);
float       betaf(float x, float y);
long double betal(long double x, long double y);

// [5.2.1.4] (complete) elliptic integral of the first kind:
double      comp_ellint_1(double k);
float       comp_ellint_1f(float k);
long double comp_ellint_1l(long double k);

// [5.2.1.5] (complete) elliptic integral of the second kind:
double      comp_ellint_2(double k);
float       comp_ellint_2f(float k);
long double comp_ellint_2l(long double k);

// [5.2.1.6] (complete) elliptic integral of the third kind:
double      comp_ellint_3(double k, double nu);
float       comp_ellint_3f(float k, float nu);
long double comp_ellint_3l(long double k, long double nu);

// [5.2.1.7] confluent hypergeometric functions:
double      conf_hyperrg(double a, double c, double x);
float       conf_hyperrgf(float a, float c, float x);
long double conf_hypergl(long double a, long double c, long double x);

// [5.2.1.8] regular modified cylindrical Bessel functions:
double      cyl_bessel_i(double nu, double x);
float       cyl_bessel_if(float nu, float x);
long double cyl_bessel_il(long double nu, long double x);

// [5.2.1.9] cylindrical Bessel functions (of the first kind):
double      cyl_bessel_j(double nu, double x);
float       cyl_bessel_jf(float nu, float x);
long double cyl_bessel_jl(long double nu, long double x);

// [5.2.1.10] irregular modified cylindrical Bessel functions:
double      cyl_bessel_k(double nu, double x);
float       cyl_bessel_kf(float nu, float x);
long double cyl_bessel_kl(long double nu, long double x);

// [5.2.1.11] cylindrical Neumann functions;
// cylindrical Bessel functions (of the second kind):

```

```

double      cyl_neumann(double nu, double x);
float       cyl_neumannf(float nu, float x);
long double cyl_neumannl(long double nu, long double x);

// [5.2.1.12] (incomplete) elliptic integral of the first kind:
double      ellint_1(double k, double phi);
float       ellint_1f(float k, float phi);
long double ellint_1l(long double k, long double phi);

// [5.2.1.13] (incomplete) elliptic integral of the second kind:
double      ellint_2(double k, double phi);
float       ellint_2f(float k, float phi);
long double ellint_2l(long double k, long double phi);

// [5.2.1.14] (incomplete) elliptic integral of the third kind:
double      ellint_3(double k, double nu, double phi);
float       ellint_3f(float k, float nu, float phi);
long double ellint_3l(long double k, long double nu, long double phi);

// [5.2.1.15] exponential integral:
double      expint(double x);
float       expintf(float x);
long double expintl(long double x);

// [5.2.1.16] Hermite polynomials:
double      hermite(unsigned n, double x);
float       hermitef(unsigned n, float x);
long double hermitel(unsigned n, long double x);

// [5.2.1.17] hypergeometric functions:
double      hyperg(double a, double b, double c, double x);
float       hypergf(float a, float b, float c, float x);
long double hypergl(long double a, long double b, long double c,
                     long double x);

// [5.2.1.18] Laguerre polynomials:
double      laguerre(unsigned n, double x);
float       laguerref(unsigned n, float x);
long double laguerrel(unsigned n, long double x);

// [5.2.1.19] Legendre polynomials:
double      legendre(unsigned l, double x);
float       legendref(unsigned l, float x);
long double legendrel(unsigned l, long double x);

// [5.2.1.20] Riemann zeta function:
double      riemann_zeta(double);
float       riemann_zetaf(float);
long double riemann_zetal(long double);

```

```

// [5.2.1.21] spherical Bessel functions (of the first kind):
double      sph_bessel(unsigned n, double x);
float       sph_besself(unsigned n, float x);
long double sph_bessell(unsigned n, long double x);

// [5.2.1.22] spherical associated Legendre functions:
double      sph_legendre(unsigned l, unsigned m, double theta);
float       sph_legendref(unsigned l, unsigned m, float theta);
long double sph_legendrel(unsigned l, unsigned m, long double theta);

// [5.2.1.23] spherical Neumann functions;
// spherical Bessel functions (of the second kind):
double      sph_neumann(unsigned n, double x);
float       sph_neumannf(unsigned n, float x);
long double sph_neumannl(unsigned n, long double x);
} // namespace tr1
} // namespace std

```

- 3 Each of the functions declared above that has one or more double parameters (the double version) shall have two additional overloads:
 1. a version with each double parameter replaced with a float parameter (the float version), and
 2. a version with each double parameter replaced with a long double parameter (the long double version).
- 4 The return type of each such float version shall be float, and the return type of each such long double version shall be long double.
- 5 Moreover, each double version shall have sufficient additional overloads to determine which of the above three versions to actually call, by the following ordered set of rules:
 1. First, if any argument corresponding to a double parameter in the double version has type long double, the long double version is called.
 2. Otherwise, if any argument corresponding to a double parameter in the double version has type double or has an integer type, the double version is called.
 3. Otherwise, the float version is called.

5.2.1.1 associated Laguerre polynomials

[tr.num.sf.Lnm]

```

double      assoc_laguerre(unsigned n, unsigned m, double x);
float       assoc_laguerref(unsigned n, unsigned m, float x);
long double assoc_laguerrel(unsigned n, unsigned m, long double x);

```

- 1 *Effects:* These functions compute the associated Laguerre polynomials of their respective arguments n, m, and x.
- 2 *Returns:* The assoc_laguerre functions return

$$L_n^m(x) = e^x \frac{d^m}{dx^m} L_n(x).$$

5.2.1.2 associated Legendre functions

[tr.num.sf.Plm]

```
double      assoc_legendre(unsigned l, unsigned m, double x);
float       assoc_legendref(unsigned l, unsigned m, float x);
long double assoc_legendrel(unsigned l, unsigned m, long double x);
```

1 *Effects:* These functions compute the associated Legendre functions of their respective arguments l , m , and x . A domain error occurs if m is greater than l . A domain error may occur if the magnitude of x is greater than one.

2 *Returns:* The `assoc_legendre` functions return

$$P_l^m(x) = (1-x^2)^{m/2} \frac{d^m}{dx^m} P_l(x).$$

5.2.1.3 beta function

[tr.num.sf.beta]

```
double      beta(double x, double y);
float       betaf(float x, float y);
long double betal(long double x, long double y);
```

1 *Effects:* These functions compute the beta function of their respective arguments x and y . A domain error may occur (a) if either x or y is a negative integer, or (b) if either x or y is zero.

2 *Returns:* The beta functions return

$$\Beta(x,y) = \frac{\Gamma(x)\Gamma(y)}{\Gamma(x+y)}.$$

5.2.1.4 (complete) elliptic integral of the first kind

[tr.num.sf.ellK]

```
double      comp_ellint_1(double k);
float       comp_ellint_1f(float k);
long double comp_ellint_1l(long double k);
```

1 *Effects:* These functions compute the complete elliptic integral of the first kind of their respective arguments k . A domain error occurs if the magnitude of k is greater than one.

2 *Returns:* The `comp_ellint_1` functions return

$$K(k) = F(k, \pi/2) = \int_0^{\pi/2} \frac{d\theta}{\sqrt{1-k^2 \sin^2 \theta}}.$$

5.2.1.5 (complete) elliptic integral of the second kind

[tr.num.sf.ellEx]

```
double      comp_ellint_2(double k);
float       comp_ellint_2f(float k);
long double comp_ellint_2l(long double k);
```

1 *Effects:* These functions compute the complete elliptic integral of the second kind of their respective arguments k . A domain error occurs if the magnitude of k is greater than one.

- 2 *Returns:* The `comp_ellint_2` functions return

$$E(k, \pi/2) = \int_0^{\pi/2} \sqrt{1 - k^2 \sin^2 \theta} d\theta .$$

5.2.1.6 (complete) elliptic integral of the third kind

[tr.num.sf.ellPx]

```
double      comp_ellint_3(double k, double nu);
float       comp_ellint_3f(float k, float nu);
long double comp_ellint_3l(long double k, long double nu);
```

- 1 *Effects:* These functions compute the complete elliptic integral of the third kind of their respective arguments `k` and `nu`. A domain error occurs if the magnitude of `k` is greater than one.

- 2 *Returns:* The `comp_ellint_3` functions return

$$\Pi(v, k, \pi/2) = \int_0^{\pi/2} \frac{d\theta}{(1 - v \sin^2 \theta) \sqrt{1 - k^2 \sin^2 \theta}} .$$

5.2.1.7 confluent hypergeometric functions

[tr.num.sf.conhyp]

```
double      conf_hyperg(double a, double c, double x) ;
float       conf_hyperrg(float a, float c, float x) ;
long double conf_hyperrgl(long double a, long double c, long double x) ;
```

- 1 *Effects:* These functions compute the confluent hypergeometric functions of their respective arguments `a`, `c`, and `x`. A domain error occurs (a) if `c` is a negative integer, or (b) if `c` is zero.

- 2 *Returns:* The `conf_hyperrg` functions return

$$F(a; c; x) = \frac{\Gamma(c)}{\Gamma(a)} \sum_{n=0}^{\infty} \frac{\Gamma(a+n)}{\Gamma(c+n)} \frac{x^n}{n!} .$$

5.2.1.8 regular modified cylindrical Bessel functions

[tr.num.sf.I]

```
double      cyl_bessel_i(double nu, double x);
float       cyl_bessel_if(float nu, float x);
long double cyl_bessel_il(long double nu, long double x);
```

- 1 *Effects:* These functions compute the regular modified cylindrical Bessel functions of their respective arguments `nu` and `x`. A domain error may occur if `x` is less than zero.

- 2 *Returns:* The `cyl_bessel_i` functions return

$$I_v(x) = i^{-v} J_v(ix) = \sum_{k=0}^{\infty} \frac{(x/2)^{v+2k}}{k! \Gamma(v+k+1)} .$$

5.2.1.9 cylindrical Bessel functions (of the first kind)

[tr.num.sf.J]

```
double      cyl_bessel_j(double nu, double x);
float       cyl_bessel_jf(float nu, float x);
long double cyl_bessel_jl(long double nu, long double x);
```

1 *Effects:* These functions compute the cylindrical Bessel functions of the first kind of their respective arguments nu and x. A domain error may occur if x is less than zero.

2 *Returns:* The cyl_bessel_j functions return

$$J_v(x) = \sum_{k=0}^{\infty} \frac{(-1)^k (x/2)^{v+2k}}{k! \Gamma(v+k+1)}.$$

5.2.1.10 irregular modified cylindrical Bessel functions

[tr.num.sf.K]

```
double      cyl_bessel_k(double nu, double x);
float       cyl_bessel_kf(float nu, float x);
long double cyl_bessel_kl(long double nu, long double x);
```

1 *Effects:* These functions compute the irregular modified cylindrical Bessel functions of their respective arguments nu and x. A domain error may occur if x is less than zero.

2 *Returns:* The cyl_bessel_k functions return

$$K_v(x) = (\pi/2)i^{v+1}(J_v(ix) + iN_v(ix)) = \begin{cases} \frac{\pi}{2} \frac{I_{-v}(x) - I_v(x)}{\sin v\pi} & \text{for non-integral } v \\ \frac{\pi}{2} \lim_{\mu \rightarrow v} \frac{I_{-\mu}(x) - I_\mu(x)}{\sin \mu\pi} & \text{for integral } v \end{cases}.$$

5.2.1.11 cylindrical Neumann functions

[tr.num.sf.N]

```
double      cyl_neumann(double nu, double x);
float       cyl_neumannf(float nu, float x);
long double cyl_neumannl(long double nu, long double x);
```

1 *Effects:* These functions compute the cylindrical Neumann functions, also known as the cylindrical Bessel functions of the second kind, of their respective arguments nu and x. A domain error may occur if x is less than zero.

2 *Returns:* The cyl_neumann functions return

$$N_v(x) = \begin{cases} \frac{J_v(x) \cos v\pi - J_{-v}(x)}{\sin v\pi} & \text{for non-integral } v \\ \lim_{\mu \rightarrow v} \frac{J_\mu(x) \cos \mu\pi - J_{-\mu}(x)}{\sin \mu\pi} & \text{for integral } v \end{cases}.$$

5.2.1.12 (incomplete) elliptic integral of the first kind

[tr.num.sf.ellF]

```
double      ellint_1(double k, double phi);
float       ellint_1f(float k, float phi);
long double ellint_1l(long double k, long double phi);
```

1 *Effects:* These functions compute the incomplete elliptic integral of the first kind of their respective arguments k and ϕ . A domain error may occur if the magnitude of k is greater than one.

2 *Returns:* The `ellint_1` functions return

$$F(k, \phi) = \int_0^\phi \frac{d\theta}{\sqrt{1 - k^2 \sin^2 \theta}}.$$

5.2.1.13 (incomplete) elliptic integral of the second kind

[tr.num.sf.ellE]

```
double      ellint_2(double k, double phi);
float       ellint_2f(float k, float phi);
long double ellint_2l(long double k, long double phi);
```

1 *Effects:* These functions compute the incomplete elliptic integral of the second kind of their respective arguments k and ϕ . A domain error may occur if the magnitude of k is greater than one.

2 *Returns:* The `ellint_2` functions return

$$E(k, \phi) = \int_0^\phi \sqrt{1 - k^2 \sin^2 \theta} d\theta.$$

5.2.1.14 (incomplete) elliptic integral of the third kind

[tr.num.sf.ellP]

```
double      ellint_3(double k, double nu, double phi);
float       ellint_3f(float k, float nu, float phi);
long double ellint_3l(long double k, long double nu, long double phi);
```

1 *Effects:* These functions compute the incomplete elliptic integral of the third kind of their respective arguments k , ν , and ϕ . A domain error may occur if the magnitude of k is greater than one.

2 *Returns:* The `ellint_3` functions return

$$\Pi(\nu, k, \phi) = \int_0^\phi \frac{d\theta}{(1 - \nu \sin^2 \theta) \sqrt{1 - k^2 \sin^2 \theta}}.$$

5.2.1.15 exponential integral

[tr.num.sf.ei]

```
double      expint(double x);
float       expintf(float x);
long double expintl(long double x);
```

1 *Effects:* These functions compute the exponential integral of their respective arguments x .

2 *Returns:* The `expint` functions return

$$\text{Ei}(x) = - \int_{-x}^{\infty} \frac{e^{-t}}{t} dt .$$

5.2.1.16 Hermite polynomials

[tr.num.sf.Hn]

```
double      hermite(unsigned n, double x);
float       hermitef(unsigned n, float x);
long double hermitel(unsigned n, long double x);
```

1 *Effects:* These functions compute the Hermite polynomials of their respective arguments n and x .

2 *Returns:* The `hermite` functions return

$$H_n(x) = (-1)^n e^{x^2} \frac{d^n}{dx^n} e^{-x^2} .$$

5.2.1.17 hypergeometric functions

[tr.num.sf.hyper]

```
double      hyperg(double a, double b, double c, double x);
float       hypergf(float a, float b, float c, float x);
long double hypergl(long double a, long double b, long double c,
                     long double x);
```

1 *Effects:* These functions compute the hypergeometric functions of their respective arguments a , b , c , and x . A domain error may occur if the magnitude of x is greater than or equal to one.

2 *Returns:* The `hyperg` functions return

$$F(a, b; c; x) = \frac{\Gamma(c)}{\Gamma(a)\Gamma(b)} \sum_{n=0}^{\infty} \frac{\Gamma(a+n)\Gamma(b+n)}{\Gamma(c+n)} \frac{x^n}{n!} .$$

5.2.1.18 Laguerre polynomials

[tr.num.sf.Ln]

```
double      laguerre(unsigned n, double x);
float       laguerref(unsigned n, float x);
long double laguerrel(unsigned n, long double x);
```

1 *Effects:* These functions compute the Laguerre polynomials of their respective arguments n and x .

2 *Returns:* The `laguerre` functions return

$$L_n(x) = e^x \frac{d^n}{dx^n} (x^n e^{-x}) .$$

5.2.1.19 Legendre polynomials

[tr.num.sf.Pl]

```
double      legendre(unsigned l, double x);
float       legendref(unsigned l, float x);
long double legendrel(unsigned l, long double x);
```

1 *Effects:* These functions compute the Legendre polynomials of their respective arguments l and x . A domain error may occur if the magnitude of x is greater than one.

2 *Returns:* The `legendre` functions return

$$P_l(x) = \frac{1}{2^l l!} \frac{d^l}{dx^l} (x^2 - 1)^l.$$

5.2.1.20 Riemann zeta function

[tr.num.sf.riemannzeta]

```
double      riemann_zeta(double x);
float       riemann_zetaf(float x);
long double riemann_zetal(long double x);
```

1 *Effects:* These functions compute the Riemann zeta function of their respective arguments x . A domain error occurs if x is equal to one.

2 *Returns:* The `riemann_zeta` functions return

$$\zeta(x) = \begin{cases} \sum_{k=1}^{\infty} k^{-x} & \text{for } x > 1 \\ 2^x \pi^{x-1} \sin\left(\frac{\pi x}{2}\right) \Gamma(1-x) \zeta(1-x) & \text{for } x < 1 \end{cases}.$$

5.2.1.21 spherical Bessel functions (of the first kind)

[tr.num.sf.j]

```
double      sph_bessel(unsigned n, double x);
float       sph_besself(unsigned n, float x);
long double sph_bessell(unsigned n, long double x);
```

1 *Effects:* These functions compute the spherical Bessel functions of the first kind of their respective arguments n and x . A domain error may occur if x is less than zero.

2 *Returns:* The `sph_bessel` functions return

$$j_n(x) = (\pi/2x)^{1/2} J_{n+1/2}(x).$$

5.2.1.22 spherical associated Legendre functions

[tr.num.sf.Ylm]

```
double      sph_legendre(unsigned l, unsigned m, double theta);
float       sph_legendref(unsigned l, unsigned m, float theta);
long double sph_legendrel(unsigned l, unsigned m, long double theta);
```

1 *Effects:* These functions compute the spherical associated Legendre functions of their respective arguments l , m , and θ . A domain error occurs if the magnitude of m is greater than l .

2 *Returns:* The `sph_legendre` functions return

$$Y_l^m(\theta, 0)$$

where

$$Y_l^m(\theta, \phi) = (-1)^m \left[\frac{(2l+1)}{4\pi} \frac{(l-m)!}{(l+m)!} \right]^{1/2} P_l^m(\cos \theta) e^{im\phi}.$$

3 *[Note:* This formulation avoids any need to return non-real numbers. —end note]

5.2.1.23 spherical Neumann functions

[tr.num.sf.n]

```
double      sph_neumann(unsigned n, double x);
float       sph_neumannf(unsigned n, float x);
long double sph_neumannl(unsigned n, long double x);
```

1 *Effects:* These functions compute the spherical Neumann functions, also known as the spherical Bessel functions of the second kind, of their respective arguments n and x . A domain error may occur if x is less than zero.

2 *Returns:* The `sph_neumann` functions return

$$n_n(x) = (\pi/2x)^{1/2} N_{n+1/2}(x).$$

5.2.2 Additions to header <math.h> synopsis

[tr.num.sf.mathh]

1 The header <math.h> shall have sufficient additional using declarations to import into the global name space all of the function names declared in the previous section.

6 Containers

[tr.cont]

- 1 This clause describes components that C++ programs may use to organize collections of information.
- 2 The following subclauses describe tuples, fixed size arrays, and unordered associated containers, as summarized in Table 12.

Table 12: Container library summary

Subclause	Header(s)
6.1 Tuple types	<tuple>
6.2 Fixed size array	<array>
6.3 Unordered associative containers	<functional> <unordered_set> <unordered_map>

6.1 Tuple types

[tr.tuple]

- 1 6.1 describes the tuple library that provides a tuple type as the class template `tuple` that can be instantiated with any number of arguments. An implementation can set an upper limit for the number of arguments. The minimum value for this implementation quantity is defined in Annex A. Each template argument specifies the type of an element in the tuple. Consequently, tuples are heterogeneous, fixed-size collections of values.

6.1.1 Header <tuple> synopsis

[tr.tuple.synopsis]

```
// [6.1.2] Class template tuple
template <class T1 = implementation-defined,
          class T2 = implementation-defined,
          ...,
          class TM = implementation-defined> class tuple;

// [6.1.2.2] Tuple creation functions
template<class T1, class T2, ..., class TN>
tuple<V1, V2, ..., VN>
make_tuple(const T1&, const T2&, ..., const TN&);

template<class T1, class T2, ..., class TN>
tuple<T1&, T2&, ..., TN&> tie(T1&, T2&, ..., TN&);

// [6.1.2.3] Tuple helper classes
```

```
template <class T> class tuple_size;

template <int I, class T> class tuple_element;

// [6.1.2.4] Element access
template <int I, class T1, class T2, ..., class TN>
RI get(tuple<T1, T2, ..., TN>&);

template <int I, class T1, class T2, ..., class TN>
PI get(const tuple<T1, T2, ..., TN>&);

// [6.1.2.5] Equality and inequality comparisons
template<class T1, class T2, ..., class TM,
         class U1, class U2, ..., class UM>
bool operator==(const tuple<T1, T2, ..., TM>&,
                  const tuple<U1, U2, ..., UM>&);

template<class T1, class T2, ..., class TM,
         class U1, class U2, ..., class UM>
bool operator!=(const tuple<T1, T2, ..., TM>&,
                  const tuple<U1, U2, ..., UM>&);

// [6.1.2.6] Operator< and operator>
template<class T1, class T2, ..., class TM,
         class U1, class U2, ..., class UM>
bool operator<(const tuple<T1, T2, ..., TM>&,
                 const tuple<U1, U2, ..., UM>&);

template<class T1, class T2, ..., class TM,
         class U1, class U2, ..., class UM>
bool operator>(const tuple<T1, T2, ..., TM>&,
                 const tuple<U1, U2, ..., UM>&);

// [6.1.2.7] Operator<= and operator>=
template<class T1, class T2, ..., class TM,
         class U1, class U2, ..., class UM>
bool operator<=(const tuple<T1, T2, ..., TM>&,
                 const tuple<U1, U2, ..., UM>&);

template<class T1, class T2, ..., class TM,
         class U1, class U2, ..., class UM>
bool operator>=(const tuple<T1, T2, ..., TM>&,
                 const tuple<U1, U2, ..., UM>&);

// [6.1.2.8] I/O
template<class CharType, class CharTrait,
         class T1, class T2, ..., class TN>
basic_ostream<CharType, CharTrait>&
operator<<(basic_ostream<CharType, CharTrait>&,
            const tuple<T1, T2, ..., TN>&);
```

```

template<class CharType, class CharTrait,
         class T1, class T2, ..., class TN>
basic_istream<CharType, CharTrait>&
operator>>(basic_istream<CharType, CharTrait>&,
              tuple<T1, T2, ..., TN>&);

// [6.1.2.9] Formatting manipulators
tuple_manip1 tuple_open(char_type c);
tuple_manip2 tuple_close(char_type c);
tuple_manip3 tuple_delimiter(char_type c);

// [6.1.4] Interface to class template array
template <class T, size_t N> struct array;

template <class T, size_t N>           struct tuple_size<array<T, N> >;
template <int I, class T, size_t N> struct tuple_element<I, array<T, N> >;

template <int I, class T, size_t N>       T& get(      array<T, N>&);
template <int I, class T, size_t N> const T& get(const array<T, N>&)

```

6.1.2 Class template tuple

[tr.tuple.tuple]

- 1 M is used to denote the implementation-defined number of template type parameters to the tuple class template, and N is used to denote the number of template arguments specified in an instantiation.
- 2 [Example: Given the instantiation `tuple<int, float, char>`, N is 3. —end example]

```

template <class T1 = implementation-defined,
         class T2 = implementation-defined,
         ...,
         class TM = implementation-defined>
class tuple
{
public:
    tuple();
    explicit tuple(P1, P2, ..., PN); // iff N > 0

    tuple(const tuple&);

    template <class U1, class U2, ..., class UN>
    tuple(const tuple<U1, U2, ..., UN>&);

    // iff N == 2
    template <class U1, class U2>
    tuple(const pair<U1, U2>&);

    tuple& operator=(const tuple&);

    template <class U1, class U2, ..., class UN>
    tuple& operator=(const tuple<U1, U2, ..., UN>&);

```

```
// iff N == 2
template <class U1, class U2>
tuple& operator=(const pair<U1, U2>&);
};
```

6.1.2.1 Construction

[tr.tuple.cnstr]

`tuple();`

1 *Requires:* Each type T_i shall be default constructible.

2 *Effects:* Default initializes each element.

`tuple(P1, P2, ..., PN);`

3 Where, if T_i is a reference type then P_i is T_i , otherwise P_i is `const Ti&`.

4 *Requires:* Each type T_i shall be copy constructible.

5 *Effects:* Copy initializes each element with the value of the corresponding parameter.

`tuple(const tuple& u);`

6 *Requires:* Each type T_i shall be copy constructible.

7 *Effects:* Copy constructs each element of `*this` with the corresponding element of `u`.

```
template <class U1, class U2, ..., class UN>
tuple(const tuple<U1, U2, ..., UN>& u);
```

8 *Requires:* Each type T_i shall be constructible from the corresponding type U_i .

9 *Effects:* Constructs each element of `*this` with the corresponding element of `u`.

10 *Note:* In an implementation where one template definition serves for many different values for N , `enable_if` can be used to make the converting constructor and assignment operator exist only in the cases where the source and target have the same number of elements. Another way of achieving this is adding an extra integral template parameter which defaults to N (more precisely, a metafunction that computes N), and then defining the converting copy constructor and assignment only for tuples where the extra parameter in the source is N . —*end note*

`template <class U1, class U2> tuple(const pair<U1, U2>& u);`

11 *Requires:* T_1 shall be constructible from U_1 , T_2 shall be constructible from U_2 . $N == 2$.

12 *Effects:* Constructs the first element with `u.first` and the second element with `u.second`.

`tuple& operator=(const tuple& u);`

13 *Requires:* Each type T_i shall be assignable.

14 *Effects:* Assigns each element of `u` to the corresponding element of `*this`.

15 *Returns:* `*this`

```
template <class U1, class U2, ..., class UN>
tuple& operator=(const tuple<U1, U2, ..., UN>& u);
```

16 *Requires:* Each type T_i shall be assignable from the corresponding type U_i .

17 *Effects:* Assigns each element of u to the corresponding element of $*this$.

18 *Returns:* $*this$

```
template <class U1, class U2>
tuple& operator=(const pair<U1, U2>& u);
```

19 *Requires:* T_1 shall be assignable from U_1 , T_2 shall be assignable from U_2 . $N == 2$.

20 *Effects:* Assigns $u.first$ to the first element of $*this$ and $u.second$ to the second element of $*this$.

21 *Returns:* $*this$

22 *Note:* There are rare conditions where the converting copy constructor is a better match than the element-wise construction, even though the user might intend differently. An example of this is if one is constructing a one-element tuple where the element type is another tuple type T and if the parameter passed to the constructor is not of type T , but rather a tuple type that is convertible to T . The effect of the converting copy construction is most likely the same as the effect of the element-wise construction would have been. However, it is possible to compare the “nesting depths” of the source and target tuples and decide to select the element-wise constructor if the source nesting depth is smaller than the target nesting-depth. This can be accomplished using an `enable_if` template or other tools for constrained templates. —*end note*]

6.1.2.2 Tuple creation functions

[tr.tuple.helper]

```
template<class T1, class T2, ..., class TN>
tuple<V1, V2, ..., VN>
make_tuple(const T1& t1, const T2& t2, ..., const TN& tn);
```

1 where V_i is $X\&$, if the cv-unqualified type T_i is `reference_wrapper<X>`, otherwise V_i is T_i .

2 The `make_tuple` function template shall be implemented for each different number of arguments from 0 to the maximum number of allowed tuple elements.

3 *Returns:* $tuple<V1, V2, ..., VN>(t1, t2, ..., tn)$.

4 *[Example:*

```
int i; float j;
make_tuple(1, ref(i), cref(j))
```

creates a tuple of type

```
tuple<int, int&, const float&>
```

—end example]

```
template<class T1, class T2, ..., class TN>
tuple<T1&, T2&, ..., TN> tie(T1& t1, T2& t2, ..., TN& tn);
```

5 The `tie` function template shall be implemented for each different number of arguments from 0 to the maximum
number of allowed tuple elements.

6 *Returns:* `tuple<T1&, T2&, ..., TN&>(t1, t2, ..., tn)`

7 *[Example:* `tie` functions allow one to create tuples that unpack tuples into variables. `ignore` can be used for
elements that are not needed:

```
int i; std::string s;
tie(i, ignore, s) = make_tuple(42, 3.14, "C++");
// i == 42, s == "C++"
```

—end example]

6.1.2.3 Valid expressions for tuple types

[tr.tuple.expr]

`tuple_size<T>::value`

1 *Requires:* `T` is an instantiation of class template `tuple`.

2 *Type:* integral constant expression.

3 *Value:* Number of elements in `T`.

`tuple_element<I, T>::type`

4 *Requires:* $0 \leq I < N$. The program is ill-formed if `I` is out of bounds.

5 *Value:* The type of the `I`th element of `T`, where indexing is zero-based.

6.1.2.4 Element access

[tr.tuple.elem]

```
template <int I, class T1, class T2, ..., class TN>
RI get(tuple<T1, T2, ..., TN>& t);
```

1 *Requires:* $0 \leq I < N$. The program is ill-formed if `I` is out of bounds.

2 *Return type:* `RI`. If `TI` is a reference type, then `RI` is `TI`, otherwise `RI` is `TI&`.

3 *Returns:* A reference to the `I`th element of `t`, where indexing is zero-based.

```
template <int I, class T1, class T2, ..., class TN>
PI get(const tuple<T1, T2, ..., TN>& t);
```

4 *Requires:* $0 \leq I < N$. The program is ill-formed if `I` is out of bounds.

5 *Return type:* `PI`. If `TI` is a reference type, then `PI` is `TI`, otherwise `PI` is `const TI&`.

6 *Returns:* A const reference to the `I`th element of `t`, where indexing is zero-based.

7 *[Note:* Constness is shallow. If `TI` is some reference type `X&`, the return type is `X&`, not `const X&`. However, if
the element type is non-reference type `T`, the return type is `const T&`. This is consistent with how constness is
defined to work for member variables of reference type. —*end note.*]

- 8 [Note: The reason `get` is defined to be a nonmember function is that, if this functionality had been provided as a member function, invocations where the type depended on a template parameter would have required using the `template` keyword. —end note]

6.1.2.5 Equality and inequality comparisons

[tr.tuple.eq]

```
template<class T1, class T2, ..., class TM,
         class U1, class U2, ..., class UM>
bool operator==(const tuple<T1, T2, ..., TM>& t,
                  const tuple<U1, U2, ..., UM>& u);
```

- 1 *Requires:* `tuple_size<tuple<T1, T2, ..., TM>>::value == tuple_size<tuple<U1, U2, ..., UM>>::value == N`. For all i , where $0 \leq i < N$, `get<i>(t) == get<i>(u)` is a valid expression returning a type that is convertible to `bool`.

- 2 *Returns:* `true` iff `get<i>(t) == get<i>(u)` for all i . For any two zero-length tuples `e` and `f`, `e == f` returns `true`.

- 3 *Effects:* The elementary comparisons are performed in order from the zeroth index upwards. No comparisons or element accesses are performed after the first equality comparison that evaluates to `false`.

```
template<class T1, class T2, ..., class TM,
         class U1, class U2, ..., class UM>
bool operator!=(const tuple<T1, T2, ..., TM>& t,
                  const tuple<U1, U2, ..., UM>& u);
```

- 4 *Requires:* `tuple_size<tuple<T1, T2, ..., TM>>::value == tuple_size<tuple<U1, U2, ..., UM>>::value == N`. For all i , where $0 \leq i < N$, `get<i>(t) != get<i>(u)` is a valid expression returning a type that is convertible to `bool`.

- 5 *Returns:* `true` iff `get<i>(t) != get<i>(u)` for any i . For any two zero-length tuples `e` and `f`, `e != f` returns `false`.

- 6 *Effects:* The elementary comparisons are performed in order from the zeroth index upwards. No comparisons or element accesses are performed after the first inequality comparison that evaluates to `true`.

6.1.2.6 <, > comparisons

[tr.tuple.lt]

```
template<class T1, class T2, ..., class TN,
         class U1, class U2, ..., class UN>
bool operator<(const tuple<T1, T2, ..., TN>&,
                  const tuple<U1, U2, ..., UN>&);
```

```
template<class T1, class T2, ..., class TN,
         class U1, class U2, ..., class UN>
bool operator>(const tuple<T1, T2, ..., TN>&,
                  const tuple<U1, U2, ..., UN>&);
```

- 1 *Requires:* `tuple_size<tuple<T1, T2, ..., TM>>::value == tuple_size<tuple<U1, U2, ..., UM>>::value == N`. For all i , where $0 \leq i < N$, `get<i>(t) ⊕ get<i>(u)` is a valid expression returning a type that is convertible to `bool`, where \oplus is either `<` or `>`.
- 2 *Returns:* The result of a lexicographical comparison with \oplus between t and u , defined as: `(bool)(get<0>(t) ⊕ get<0>(u)) || !((bool)(get<0>(u) ⊕ get<0>(t)) && ttail ⊕ utail)`, where r_{tail} for some tuple r is a tuple containing all but the first element of r . For any two zero-length tuples e and f , $e ⊕ f$ returns `false`.

6.1.2.7 `<=` and `>=` comparisons

[tr.tuple.le]

```
template<class T1, class T2, ..., class TN,
         class U1, class U2, ..., class UN>
bool operator<=(const tuple<T1, T2, ..., TN>&,
                 const tuple<U1, U2, ..., UN>&);

template<class T1, class T2, ..., class TN,
         class U1, class U2, ..., class UN>
bool operator>=(const tuple<T1, T2, ..., TN>&,
                 const tuple<U1, U2, ..., UN>&);
```

- 1 *Requires:* `tuple_size<tuple<T1, T2, ..., TM>>::value == tuple_size<tuple<U1, U2, ..., UM>>::value == N`. For all i , where $0 \leq i < N$, `get<i>(t) ⊕ get<i>(u)` is a valid expression returning a type that is convertible to `bool`, where \oplus is either `<=` or `>=`.
- 2 *Returns:* The result of a lexicographical comparison with \oplus between t and u , defined as: `(bool)(get<0>(t) ⊕ get<0>(u)) && (!((bool)(get<0>(u) ⊕ get<0>(t)) || ttail ⊕ utail)`, where r_{tail} for some tuple r is a tuple containing all but the first element of r . For any two zero-length tuples e and f , $e ⊕ f$ returns `true`.
- 3 *Notes:* The above definitions for comparison operators do not impose the requirement that t_{tail} (or u_{tail}) shall be constructed. It may be even impossible, as t (or u) is not required to be copy constructible. Also, all comparison operators are short circuited to not perform element accesses beyond what is required to determine the result of the comparison.

6.1.2.8 Input and output

[tr.tuple.io]

```
template<class CharType, class CharTrait,
         class T1, class T2, ..., class TN>
basic_ostream<CharType, CharTrait>&
operator<<(basic_ostream<CharType, CharTrait>& os,
            const tuple<T1, T2, ..., TN>& t);
```

- 1 *Requires:* For all $i = 0, 1, \dots, N-1$ in $os \ll get<i>(t)$ is a valid expression.
- 2 *Effects:* Inserts t into os as $Lt_0dt_1d\dots dt_nR$, where L is the opening, d the delimiter and R the closing character set by tuple formatting manipulators. Each element t_i is output by invoking $os \ll get<i>(t)$. A zero-element tuple is output as LR and a one-element tuple is output as Lt_0R .
- 3 *Returns:* os

```
template<class CharType, class CharTrait,
         class T1, class T2, ..., class TN>
basic_istream<CharType, CharTrait>&
operator>>(basic_istream<CharType, CharTrait>& is,
             tuple<T1, T2, ..., TN>& t);
```

4 *Requires:* For all $i = 0, 1, \dots, N-1$ in `is >> get<i>(t)` is a valid expression.

5 *Effects:* Extracts a tuple of the form $Lt_0dt_1d\dots dt_nR$, where L is the opening, d the delimiter and R the closing character set by tuple formatting manipulators. Each element t_i is extracted by invoking `is >> get<i>(t)`. A zero-element tuple expects to extract LR from the stream and one-element tuple expects to extract Lt_0R . If bad input is encountered, calls `is.set_state(ios::failbit)` (which may throw `ios::failure` (27.4.4.3)).

6 *Returns:* `is`

7 *Notes:* It is not guaranteed that a tuple written to a stream can be extracted back to a tuple of the same type.

6.1.2.9 Tuple formatting manipulators

[tr.tuple.form]

1 The library defines the following three stream manipulator functions. The types designated `tuple_manip1`, `tuple_manip2` and `tuple_manip3` are implementation-specified.

```
tuple_manip1 tuple_open(char_type c);
tuple_manip2 tuple_close(char_type c);
tuple_manip3 tuple_delimiter(char_type c);
```

2 *Returns:* Each of these functions returns an object `s` of unspecified type such that if `out` is an instance of `basic_ostream<charT,traits>`, `in` is an instance of `basic_istream<charT,traits>` and `char_type` equals `charT`, then the expression `out << s` (respectively `in >> s`) sets `c` to be the opening, closing, or delimiter character (depending on the manipulator function called) to be used when writing tuples into `out` (respectively extracting tuples from `in`).

3 *Notes:* It is unspecified whether an implementation supports these manipulators for streams with `sizeof(charT) > sizeof(long)`. If an implementation does not support these manipulators for such streams, the expressions `out << s` and `in >> s`, where `out` and `in` are such streams, are ill-formed.

4 *[Note:* The constraint stated in the above **Notes** section allows an implementation where the delimiter characters are stored in space allocated by `xalloc`, which allocates an array of `longs`. A more general alternative is to store pointers to the delimiter characters in the `xalloc`-allocated array, and register a callback function (with `ios::base::register_callback`) for the stream to take care of deallocating the memory. If this approach is taken, the delimiters could be chosen to be strings instead of single characters. This might be worthwhile, such as to allow delimiters like ", ". —end note]

6.1.3 Pairs

[tr.tuple.pairs]

1 This is an *impure* extension (as defined in section 1.2) to the standard library class template `std::pair`.

```
template<class T1, class T2>
struct tuple_size<pair<T1, T2> > {
    static const int value = 2;
```

```

};

template<class T1, class T2>
struct tuple_element<0, pair<T1, T2> > {
    typedef T1 type;
};

template<class T1, class T2>
struct tuple_element<1, pair<T1, T2> > {
    typedef T2 type;
};

template<int I, class T1, class T2>
P& get(pair<T1, T2>&);

template<int I, class T1, class T2>
const P& get(const pair<T1, T2>&);

```

2 *Return type:* If I is 0 then P is T1, if I is 1 then P is T2, otherwise the program is ill-formed.

3 *Returns:* If I == 0 returns p.first, otherwise returns p.second.

6.1.4 Tuple interface to array

[tr.tuple.arr]

```
tuple_size<array<T, N> >::value
```

1 *Return type:* integral constant expression.

2 *Value:* N

```
tuple_element<I, array<T, N> >::type
```

3 *Requires:* 0 <= I < N. The program is ill-formed if I is out of bounds.

4 *value:* The type T.

```
template <int I, class T, size_t N> T& get(array<T, N>& a);
```

5 *Requires:* 0 <= I < N. The program is ill-formed if I is out of bounds.

6 *Returns:* A reference to the Ith element of a, where indexing is zero-based.

```
template <int I, class T, size_t N> const T& get(const array<T, N>& a);
```

7 *Requires:* 0 <= I < N. The program is ill-formed if I is out of bounds.

8 *Return type:* const T&.

9 *Returns:* A const reference to the Ith element of a, where indexing is zero-based.

6.2 Fixed size array

[tr.array]

6.2.1 Header <array> synopsis

[tr.array.syn]

```

namespace tr1 {
    // [6.2.2] Class template array
    template <class T, size_t N > struct array;

    // Array comparisons
    template <class T, size_t N >
    bool operator==
        (const array<T,N>& x, const array<T,N>& y);
    template <class T, size_t N >
    bool operator<
        (const array<T,N>& x, const array<T,N>& y);
    template <class T, size_t N >
    bool operator!=
        (const array<T,N>& x, const array<T,N>& y);
    template <class T, size_t N >
    bool operator>
        (const array<T,N>& x, const array<T,N>& y);
    template <class T, size_t N >
    bool operator>=
        (const array<T,N>& x, const array<T,N>& y);
    template <class T, size_t N >
    bool operator<=
        (const array<T,N>& x, const array<T,N>& y);

    // [6.2.2.2] Specialized algorithms
    template <class T, size_t N >
    void swap(array<T,N>& x, array<T,N>& y);
}

```

6.2.2 Class template array

[tr.array.array]

- 1 The header `<array>` defines a class template for storing fixed-size sequences of objects. An `array` supports random access iterators. An instance of `array<T, N>` stores `N` elements of type `T`, so that `size() == N` is an invariant. The elements of an `array` are stored contiguously, meaning that if `a` is an `array<T, N>` then it obeys the identity `&a[n] == &a[0] + n` for all `0 <= n < N`.
- 2 An `array` is an aggregate ([dcl.init.aggr]) that can be initialized with the syntax

```
array a = { initializer-list };
```

where *initializer-list* is a comma separated list of up to `N` elements of type convertible-to-`T`.

- 3 Unless specified otherwise, all `array` operations are as described in [lib.container.requirements]. Descriptions are provided here only for operations on `array` that are not described in this clause or for operations where there is additional semantic information.
- 4 The effect of calling `front()` or `back()` for a zero-sized array is implementation defined.

```

namespace tr1 {
    template <class T, size_t N >
    struct array {

```

```

// types:
typedef T & reference;
typedef const T & const_reference;
typedef implementation defined iterator;
typedef implementation defined const_iterator;
typedef size_t size_type;
typedef ptrdiff_t difference_type;
typedef T value_type;
typedef std::reverse_iterator<iterator> reverse_iterator;
typedef std::reverse_iterator<const_iterator> const_reverse_iterator;

T     elems[N];           // Exposition only

// No explicit construct/copy/destroy for aggregate type

void assign(const T& u);
void swap( array<T, N> &);

// iterators:
iterator begin();
const_iterator begin() const;
iterator end();
const_iterator end() const;
reverse_iterator rbegin();
const_reverse_iterator rbegin() const;
reverse_iterator rend();
const_reverse_iterator rend() const;

// capacity:
size_type size() const;
size_type max_size() const;
bool empty() const;

// element access:
reference operator[](size_type n);
const_reference operator[](size_type n) const;
const_reference at(size_type n) const;
reference at(size_type n);
reference front();
const_reference front() const;
reference back();
const_reference back() const;

T * data();
const T * data() const;
};

template <class T, size_t N>
bool operator==(const array<T,N>& x,

```

```

        const array<T,N>& y);
template <class T, size_t N>
bool operator< (const array<T,N>& x,
                 const array<T,N>& y);
template <class T, size_t N>
bool operator!=(const array<T,N>& x,
                  const array<T,N>& y);
template <class T, size_t N>
bool operator> (const array<T,N>& x,
                  const array<T,N>& y);
template <class T, size_t N>
bool operator>=(const array<T,N>& x,
                   const array<T,N>& y);
template <class T, size_t N>
bool operator<=(const array<T,N>& x,
                   const array<T,N>& y);

// specialized algorithms:
template <class T, size_t N>
void swap(array<T,N>& x, array<T,N>& y);
}

```

- 5 [Note: The member variable `elems` is shown for exposition only, to emphasize that `array` is a class aggregate. The name `elems` is not part of `array`'s interface. —end note]

6.2.2.1 array constructors, copy, and assignment

[tr.array.cons]

- 1 **Initialization:** The conditions for an aggregate ([dcl.init.aggr]) must be met. Class `array` relies on the implicitly-declared special member functions ([class.ctor], [class.dtor], and [class.copy]) to conform to the container requirements table in [lib.container.requirements].

6.2.2.2 array specialized algorithms

[tr.array.special]

```

template <class T, size_t N>
void swap(array<T,N>& x, array<T,N>& y);

```

- 1 *Effects:*

```
swap_ranges(x.begin(), x.end(), y.begin());
```

6.2.2.3 array size

[tr.array.size]

```

template <class T, size_t N>
size_type array<T,N>::size();

```

- 1 *Returns:* `N`

6.2.2.4 Zero sized arrays

[tr.array.zero]

- 1 `array` shall provide support for the special case `N == 0`.

- 2 In the case that $N == 0$:
- `elems` is not required.
 - `begin() == end() == unique value.`

6.3 Unordered associative containers

[tr.hash]

6.3.1 Unordered associative container requirements

[tr.unord.req]

- 1 Unordered associative containers provide an ability for fast retrieval of data based on keys. The worst-case complexity for most operations is linear, but the average case is much faster. The library provides four basic kinds of unordered associative containers: `unordered_set`, `unordered_map`, `unordered_multiset`, and `unordered_multimap`.
- 2 Unordered associative containers conform to the requirements for Containers ([lib.container.requirements]), except that the expressions in table 13 are not required to be valid, where a and b denote values of a type X , and X is an unordered associative container class:

Table 13: Container requirements that are not supported by unordered associative containers

unsupported expressions
$a == b$
$a != b$
$a < b$
$a > b$
$a <= b$
$a >= b$

- 3 Each unordered associative container is parameterized by `Key`, by a function object `Hash` that acts as a hash function for values of type `Key`, and on a binary predicate `Pred` that induces an equivalence relation on values of type `Key`. Additionally, `unordered_map` and `unordered_multimap` associate an arbitrary *mapped type* T with the `Key`.
- 4 A hash function is a function object that takes a single argument of type `Key` and returns a value of type `std::size_t` in the range $[0, \text{std}::\text{numeric_limits}[\text{std}::\text{size_t}]::\text{max}()]$.
- 5 Two values k_1 and k_2 of type `Key` are considered equal if the container's equality function object returns true when passed those values. If k_1 and k_2 are equal, the hash function shall return the same value for both.
- 6 An unordered associative container supports *unique keys* if it may contain at most one element for each key. Otherwise, it supports *equivalent keys*. `unordered_set` and `unordered_map` support unique keys. `unordered_multiset` and `unordered_multimap` support equivalent keys. In containers that support equivalent keys, elements with equivalent keys are adjacent to each other.
- 7 For `unordered_set` and `unordered_multiset` the value type is the same as the key type. For `unordered_map` and `unordered_multimap` it is equal to `std::pair<const Key, T>`.
- 8 The elements of an unordered associative container are organized into *buckets*. Keys with the same hash code appear in the same bucket. The number of buckets is automatically increased as elements are added to an unordered associative

container, so that the average number of elements per bucket is kept below a bound. Rehashing invalidates iterators, changes ordering between elements, and changes which buckets elements appear in, but does not invalidate pointers or references to elements.

- 9 In table 14: X is an unordered associative container class, a is an object of type X, b is a possibly const object of type X, a_uniq is an object of type X when X supports unique keys, a_eq is an object of type X when X supports equivalent keys, i and j are input iterators that refer to value_type, [i, j) is a valid range, p and q2 are valid iterators to a, q and q1 are valid dereferenceable iterators to a, [q1, q2) is a valid range in a, r and r1 are valid dereferenceable const iterators to a, r2 is a valid const iterator to a, [r1, r2) is a valid range in a, t is a value of type X::value_type, k is a value of type key_type, hf is a possibly const value of type hasher, eq is a possibly const value of type key_equal, n is a value of type size_type, and z is a value of type float.

Table 14: Unordered associative container requirements (in addition to container)

expression	return type	assertion/notepre/post-condition	complexity
X::key_type	Key	Key is Assignable and CopyConstructible	compile time
X::hasher	Hash	Hash is a unary function object that takes an argument of type Key and returns a value of type std::size_t.	compile time
X::key_equal	Pred	Pred is a binary predicate that takes two arguments of type Key. Pred is an equivalence relation.	compile time
X::local_iterator	An iterator type whose category, value type, difference type, and pointer and reference types are the same as X::iterator's.	A local_iterator object may be used to iterate through a single bucket, but may not be used to iterate across buckets.	compile time
X::const_local_iterator	An iterator type whose category, value type, difference type, and pointer and reference types are the same as X::const_iterator's.	A const_local_iterator object may be used to iterate through a single bucket, but may not be used to iterate across buckets.	compile time
X(n, hf, eq) X a(n, hf, eq)	X	Constructs an empty container with $\mathcal{O}(n)$ at least n buckets, using hf as the hash function and eq as the key equality predicate.	
X(n, hf) X a(n, hf)	X	Constructs an empty container with $\mathcal{O}(n)$ at least n buckets, using hf as the hash function and key_equal() as the key equality predicate.	

expression	return type	assertion/notepre/post-condition	complexity
<code>X(n)</code> <code>X a(n)</code>	<code>X</code>	Constructs an empty container with at least n buckets, using <code>hasher()</code> as the hash function and <code>key_equal()</code> as the key equality predicate.	$\mathcal{O}(n)$
<code>X()</code> <code>tcodeX a</code>	<code>X</code>	Constructs an empty container with an unspecified number of buckets, using <code>hasher()</code> as the hash function and <code>key_equal</code> as the key equality predicate.	constant
<code>X(i, j, n, hf, eq)</code> <code>X a(i, j, n, hf, eq)</code>	<code>X</code>	Constructs an empty container with at least n buckets, using <code>hf</code> as the hash function and <code>eq</code> as the key equality predicate, and inserts elements from $[i, j]$ into it.	Average case $\mathcal{O}(N)$ (N is <code>distance(i, j)</code>), worst case $\mathcal{O}(N^2)$
<code>X(i, j, n, hf)</code> <code>X a(i, j, n, hf)</code>	<code>X</code>	Constructs an empty container with at least n buckets, using <code>hf</code> as the hash function and <code>key_equal()</code> as the key equality predicate, and inserts elements from $[i, j]$ into it.	Average case $\mathcal{O}(N)$ (N is <code>distance(i, j)</code>), worst case $\mathcal{O}(N^2)$
<code>X(i, j, n)</code> <code>X a(i, j, n)</code>	<code>X</code>	Constructs an empty container with at least n buckets, using <code>hasher()</code> as the hash function and <code>key_equal()</code> as the key equality predicate, and inserts elements from $[i, j]$ into it.	Average case $\mathcal{O}(N)$ (N is <code>distance(i, j)</code>), worst case $\mathcal{O}(N^2)$
<code>X(i, j)</code> <code>X a(i, j)</code>	<code>X</code>	Constructs an empty container with an unspecified number of buckets, using <code>hasher()</code> as the hash function and <code>key_equal</code> as the key equality predicate, and inserts elements from $[i, j]$ into it.	Average case $\mathcal{O}(N)$ (N is <code>distance(i, j)</code>), worst case $\mathcal{O}(N^2)$
<code>X(b)</code> <code>X a(b)</code>	<code>X</code>	Copy constructor. In addition to the contained elements, the hash function, predicate, and maximum load factor are copied.	Average case linear in <code>b.size()</code> , worst case quadratic.
<code>a = b</code>	<code>X</code>	Copy assignment operator. In addition to the contained elements, the hash function, predicate, and maximum load factor are copied.	Average case linear in <code>b.size()</code> , worst case quadratic.
<code>b.hash_function()</code>	<code>hasher</code>	Returns the hash function out of which <code>b</code> was constructed.	constant

expression	return type	assertion/notepre/post-condition	complexity
<code>b.key_eq()</code>	<code>key_equal</code>	Returns the key equality function out of which <code>b</code> was constructed.	constant
<code>a_uniq.insert(t)</code>	<code>pair<iterator, bool></code>	Inserts <code>t</code> if and only if there is no element in the container with key equivalent to the key of <code>t</code> . The <code>bool</code> component of the returned pair indicates whether the insertion takes place, and the <code>iterator</code> component points to the element with key equivalent to the key of <code>t</code> .	Average case $\mathcal{O}(1)$, worst case $\mathcal{O}(a_{-}\text{uniq}.\text{size}())$.
<code>a_eq.insert(t)</code>	<code>iterator</code>	Inserts <code>t</code> , and returns an iterator pointing to the newly inserted element.	Average case $\mathcal{O}(1)$, worst case $\mathcal{O}(a_{-}\text{uniq}.\text{size}())$.
<code>a.insert(r, t)</code>	<code>iterator</code>	Equivalent to <code>a.insert(t)</code> . Return value is an iterator pointing to the element with the key equivalent to that of <code>t</code> . The const iterator <code>r</code> is a hint pointing to where the search should start. Implementations are permitted to ignore the hint.	Average case $\mathcal{O}(1)$, worst case $\mathcal{O}(a_{-}\text{uniq}.\text{size}())$.
<code>a.insert(i, j)</code>	<code>void</code>	Pre: <code>i</code> and <code>j</code> are not iterators in <code>a</code> . Equivalent to <code>a.insert(t)</code> for each element in $[i, j]$.	Average case $\mathcal{O}(N)$, where N is <code>distance(i, j)</code> . Worst case $\mathcal{O}(N * a.\text{size}())$.
<code>a.erase(k)</code>	<code>size_type</code>	Erases all elements with key equivalent to <code>k</code> . Returns the number of elements erased.	Average case $\mathcal{O}(a.\text{count}(k))$. Worst case $\mathcal{O}(a.\text{size}())$.
<code>a.erase(r)</code>	<code>void</code>	Erases the element pointed to by <code>r</code> .	Average case $\mathcal{O}(1)$, worst case $\mathcal{O}(a.\text{size}())$.
<code>a.erase(r1, r2)</code>	<code>void</code>	Erases all elements in the range $[r1, r2]$.	Average case $\mathcal{O}(N)$, where N is <code>distance(r1, r2)</code> , worst case $\mathcal{O}(a.\text{size}())$.
<code>a.clear()</code>	<code>void</code>	Erases all elements in the container. Post: <code>a.size() == 0</code>	Linear.

expression	return type	assertion/notepre/post-condition	complexity
b.find(k)	iterator; const_iterator for const b.	Returns an iterator pointing to an element with key equivalent to k, or b.end() if no such element exists.	Average case $\mathcal{O}(1)$, worst case $\mathcal{O}(b.size())$.
b.count(k)	size_type	Returns the number of elements with key equivalent to k.	Average case $\mathcal{O}(1)$, worst case $\mathcal{O}(b.size())$.
b.equal_range(k)	pair<iterator, iterator>; pair<const_iterator, const_iterator> for const b.	Returns a range containing all elements with keys equivalent to k. Returns make_pair(b.end(), b.end()) if no such elements exist.	Average case $\mathcal{O}(b.count(k))$. Worst case $\mathcal{O}(b.size())$.
b.bucket_count()	size_type	Returns the number of buckets that b contains.	Constant
b.max_bucket_count()	size_type	Returns an upper bound on the number of buckets that b might ever contain.	Constant
b.bucket(k)	size_type	Returns the index of the bucket in which elements with keys equivalent to k would be found, if any such element existed. Post: the return value is in the range [0, b.bucket_count()).	Constant
b.bucket_size(n)	size_type	Pre: n is in the range [0, b.bucket_count()). Returns the number of elements in the n^{th} bucket.	$\mathcal{O}(b.bucket_size(n))$
b.begin(n)	local_iterator; const_local_iterator for const b.	Pre: n is in the range [0, b.bucket_count()). Note: [b.begin(n), b.end(n)) is a valid range containing all of the elements in the n^{th} bucket.	Constant
b.end(n)	local_iterator; const_local_iterator for const b.	Pre: n is in the range [0, b.bucket_count()).	Constant
b.load_factor()	float	Returns the average number of elements per bucket.	Constant
b.max_load_factor()	float	Returns a number that the container attempts to keep the load factor less than or equal to. The container automatically increases the number of buckets as necessary to keep the load factor below this number. Post: return value is positive.	Constant

expression	return type	assertion/notepre/post-condition	complexity
a.max_load_factor(z)	void	Pre: z is positive. Changes the container's maximum load factor, using z as a hint.	Constant
a.rehash(n)	void	Post: a.bucket_count() > a.size() / a.max_load_factor() and a.bucket_count() >= n.	Average case linear in a.size(), worst case quadratic.

- 10 Unordered associative containers are not required to support the expressions `a == b` or `a != b`. [Note: This is because the container requirements define operator equality in terms of equality of ranges. Since the elements of an unordered associative container appear in an arbitrary order, range equality is not a useful operation. —end note]
- 11 The iterator types `iterator` and `const_iterator` of an unordered associative container are of at least the forward iterator category. For unordered associative containers where the key type and value type are the same, both `iterator` and `const_iterator` are `const` iterators.
- 12 The insert members shall not affect the validity of references to container elements, but may invalidate all iterators to the container. The erase members shall invalidate only iterators and references to the erased elements.
- 13 The insert members shall not affect the validity of iterators if $(N+n) < z * B$, where N is the container's size, n is the number of elements inserted, B is the container's bucket count, and z is the container's maximum load factor.

6.3.1.1 Exception safety guarantees

[tr.unord.req.exception]

- 1 For unordered associative containers, no `clear()` function throws an exception. No `erase()` function throws an exception unless that exception is thrown by the container's Hash or Pred object (if any).
- 2 For unordered associative containers, if an exception is thrown by an `insert()` function while inserting a single element other than by the container's hash function, the `insert()` function has no effects.
- 3 For unordered associative containers, no `swap` function throws an exception unless that exception is thrown by the copy constructor or copy assignment operator of the container's Hash or Pred object (if any).
- 4 For unordered associative containers, if an exception is thrown from within a `rehash()` function other than by the container's hash function or comparison function, the `rehash()` function has no effect.

6.3.2 Additions to header <functional> synopsis

[tr.unord.fun.syn]

```
namespace tr1 {
    // [6.3.3] Hash function base template
    template <class T> struct hash;

    // Hash function specializations
    template <> struct hash<bool>;
    template <> struct hash<char>;
    template <> struct hash<signed char>;
    template <> struct hash<unsigned char>;
    template <> struct hash<wchar_t>;
    template <> struct hash<short>;
```

```

template <> struct hash<int>;
template <> struct hash<long>;
template <> struct hash<unsigned short>;
template <> struct hash<unsigned int>;
template <> struct hash<unsigned long>;

template <> struct hash<float>;
template <> struct hash<double>;
template <> struct hash<long double>;

template<class T>
struct hash<T*>

template <class charT, class traits, class Allocator>
struct hash<std::basic_string<charT, traits, Allocator> >;
}

```

6.3.3 Class template hash

[tr.unord.hash]

- 1 The function object `hash` is used as the default hash function by the *unordered associative containers*. This class template is only required to be instantiable for integer types ([basic.fundamental]), floating point types ([basic.fundamental]), pointer types ([dcl.ptr]), and (for any valid set of `charT`, `traits`, and `Alloc` such that `charT` is an integer type) `std::basic_string<charT, traits, Alloc>`.

```

template <class T>
struct hash : public std::unary_function<T, std::size_t>
{
    std::size_t operator()(T val) const;
};

```

- 2 The return value of `operator()` is unspecified, except that equal arguments yield the same result. `operator()` shall not throw exceptions.

6.3.4 Unordered associative container classes

[tr.unord.unord]

6.3.4.1 Header <unordered_set> synopsis

[tr.unord.syn.set]

```

namespace tr1 {
    // [6.3.4.3] Class template unordered_set
    template <class Value,
              class Hash = hash<Value>,
              class Pred = std::equal_to<Value>,
              class Alloc = std::allocator<Value> >
    class unordered_set;

    // [6.3.4.5] Class template unordered_multiset
    template <class Value,
              class Hash = hash<Value>,
              class Pred = std::equal_to<Value>,
              class Alloc = std::allocator<Value> >
    class unordered_multiset;
}

```

```
}
```

6.3.4.2 Header <unordered_map> synopsis

[tr.unord.syn.map]

```
namespace tr1 {
    // [6.3.4.4] Class template unordered_map
    template <class Key,
              class T,
              class Hash = hash<Key>,
              class Pred = std::equal_to<Key>,
              class Alloc = std::allocator<std::pair<const Key, T>>>
    class unordered_map;

    // [6.3.4.6] Class template unordered_multimap
    template <class Key,
              class T,
              class Hash = hash<Key>,
              class Pred = std::equal_to<Key>,
              class Alloc = std::allocator<std::pair<const Key, T>>>
    class unordered_multimap;
}
```

6.3.4.3 Class template unordered_set

[tr.unord.set]

- 1 An `unordered_set` is a kind of unordered associative container that supports unique keys (an `unordered_set` contains at most one of each key value) and in which the elements' keys are the elements themselves.
- 2 An `unordered_set` satisfies all of the requirements of a container and of an unordered associative container. It provides the operations described in the preceding requirements table for unique keys; that is, an `unordered_set` supports the `a_uniq` operations in that table, not the `a_eq` operations. For a `unordered_set<Value>` the `key` type and the `value` type are both `Value`. The `iterator` and `const_iterator` types are both `const iterator` types. It is unspecified whether or not they are the same type.
- 3 This section only describes operations on `unordered_set` that are not described in one of the requirement tables, or for which there is additional semantic information.

```
template <class Value,
          class Hash = hash<Value>,
          class Pred = std::equal_to<Value>,
          class Alloc = std::allocator<Value>>
class unordered_set
{
public:
    // types
    typedef Value                                key_type;
    typedef Value                                value_type;
    typedef Hash                                 hasher;
    typedef Pred                                key_equal;
    typedef Alloc                               allocator_type;
    typedef typename allocator_type::pointer     pointer;
    typedef typename allocator_type::const_pointer const_pointer;
```

```

typedef typename allocator_type::reference reference;
typedef typename allocator_type::const_reference const_reference;
typedef implementation-defined size_type;
typedef implementation-defined difference_type;

typedef implementation-defined iterator;
typedef implementation-defined const_iterator;
typedef implementation-defined local_iterator;
typedef implementation-defined const_local_iterator;

// construct/destroy/copy
explicit unordered_set(size_type n = implementation-defined,
                      const hasher& hf = hasher(),
                      const key_equal& eql = key_equal(),
                      const allocator_type& a = allocator_type());
template <class InputIterator>
unordered_set(InputIterator f, InputIterator l,
              size_type n = implementation-defined,
              const hasher& hf = hasher(),
              const key_equal& eql = key_equal(),
              const allocator_type& a = allocator_type());
unordered_set(const unordered_set&);
~unordered_set();
unordered_set& operator=(const unordered_set&);
allocator_type get_allocator() const;

// size and capacity
bool empty() const;
size_type size() const;
size_type max_size() const;

// iterators
iterator begin();
const_iterator begin() const;
iterator end();
const_iterator end() const;

// modifiers
std::pair<iterator, bool> insert(const value_type& obj);
iterator insert(const_iterator hint, const value_type& obj);
template <class InputIterator>
void insert(InputIterator first, InputIterator last);

void erase(const_iterator position);
size_type erase(const key_type& k);
void erase(const_iterator first, const_iterator last);
void clear();

void swap(unordered_set&);

```

```

// observers
hasher hash_function() const;
key_equal key_eq() const;

// lookup
iterator      find(const key_type& k);
const_iterator find(const key_type& k) const;
size_type count(const key_type& k) const;
std::pair<iterator, iterator>
    equal_range(const key_type& k);
std::pair<const_iterator, const_iterator>
    equal_range(const key_type& k) const;

// bucket interface
size_type bucket_count() const;
size_type max_bucket_count() const;
size_type bucket_size(size_type n) const;
size_type bucket(const key_type& k) const;
local_iterator begin(size_type n);
const_local_iterator begin(size_type n) const;
local_iterator end(size_type n);
const_local_iterator end(size_type n) const;

// hash policy
float load_factor() const;
float max_load_factor() const;
void max_load_factor(float z);
void rehash(size_type n);
};

template <class Value, class Hash, class Pred, class Alloc>
void swap(unordered_set<Value, Hash, Pred, Alloc>& x,
          unordered_set<Value, Hash, Pred, Alloc>& y);

```

6.3.4.3.1 unordered_set constructors

[tr.unord.set.cnstr]

```

explicit unordered_set(size_type n = implementation-defined,
                      const hasher& hf = hasher(),
                      const key_equal& eql = key_equal(),
                      const allocator_type& a = allocator_type());

```

1 *Effects:* Constructs an empty unordered_set using the specified hash function, key equality function, and allocator, and using at least *n* buckets. If *n* is not provided, the number of buckets is implementation defined. *max_load_factor()* is 1.0.

2 *Complexity:* Constant.

```

template <class InputIterator>
unordered_set(InputIterator f, InputIterator l,

```

```

size_type n = implementation-defined,
const hasher& hf = hasher(),
const key_equal& eql = key_equal(),
const allocator_type& a = allocator_type());

```

- 3 *Effects:* Constructs an empty `unordered_set` using the specified hash function, key equality function, and allocator, and using at least `n` buckets. (If `n` is not provided, the number of buckets is implementation defined.) Then inserts elements from the range $[f, l]$. `max_load_factor()` is 1.0.

- 4 *Complexity:* Average case linear, worst case quadratic.

6.3.4.3.2 `unordered_set swap`

[tr.unord.set.swap]

```

template <class Value, class Hash, class Pred, class Alloc>
void swap(unordered_set<Value, Hash, Pred, Alloc>& x,
          unordered_set<Value, Hash, Pred, Alloc>& y);

```

- 1 *Effects:* `x.swap(y)`.

6.3.4.4 Class template `unordered_map`

[tr.unord.map]

- 1 An `unordered_map` is a kind of unordered associative container that supports unique keys (an `unordered_map` contains at most one of each key value) and that associates values of another type `mapped_type` with the keys.
- 2 An `unordered_map` satisfies all of the requirements of a container and of a unordered associative container. It provides the operations described in the preceding requirements table for unique keys; that is, an `unordered_map` supports the `a_uniq` operations in that table, not the `a_eq` operations. For a `unordered_map<Key, T>` the key type is `Key`, the mapped type is `T`, and the value type is `std::pair<const Key, T>`.
- 3 This section only describes operations on `unordered_map` that are not described in one of the requirement tables, or for which there is additional semantic information.

```

template <class Key,
         class T,
         class Hash = hash<Key>,
         class Pred = std::equal_to<Key>,
         class Alloc = std::allocator<std::pair<const Key, T> > >
class unordered_map
{
public:
    // types
    typedef Key                                key_type;
    typedef std::pair<const Key, T>              value_type;
    typedef T                                  mapped_type;
    typedef Hash                               hasher;
    typedef Pred                             key_equal;
    typedef Alloc                            allocator_type;
    typedef typename allocator_type::pointer   pointer;
    typedef typename allocator_type::const_pointer const_pointer;
    typedef typename allocator_type::reference reference;

```

```

typedef typename allocator_type::const_reference const_reference;
typedef implementation-defined size_type;
typedef implementation-defined difference_type;

typedef implementation-defined iterator;
typedef implementation-defined const_iterator;
typedef implementation-defined local_iterator;
typedef implementation-defined const_local_iterator;

// construct/destroy/copy
explicit unordered_map(size_type n = implementation-defined,
                      const hasher& hf = hasher(),
                      const key_equal& eql = key_equal(),
                      const allocator_type& a = allocator_type());
template <class InputIterator>
unordered_map(InputIterator f, InputIterator l,
              size_type n = implementation-defined,
              const hasher& hf = hasher(),
              const key_equal& eql = key_equal(),
              const allocator_type& a = allocator_type());
unordered_map(const unordered_map&);
~unordered_map();
unordered_map& operator=(const unordered_map&);

allocator_type get_allocator() const;

// size and capacity
bool empty() const;
size_type size() const;
size_type max_size() const;

// iterators
iterator begin();
const_iterator begin() const;
iterator end();
const_iterator end() const;

// modifiers
std::pair<iterator, bool> insert(const value_type& obj);
iterator insert(const_iterator hint, const value_type& obj);
template <class InputIterator>
void insert(InputIterator first, InputIterator last);

void erase(const_iterator position);
size_type erase(const key_type& k);
void erase(const_iterator first, const_iterator last);
void clear();

void swap(unordered_map&);

// observers

```

```

hasher hash_function() const;
key_equal key_eq() const;

// lookup
iterator find(const key_type& k);
const_iterator find(const key_type& k) const;
size_type count(const key_type& k) const;
std::pair<iterator, iterator>
    equal_range(const key_type& k);
std::pair<const_iterator, const_iterator>
    equal_range(const key_type& k) const;

mapped_type& operator[](const key_type& k);

// bucket interface
size_type bucket_count() const;
size_type max_bucket_count() const;
size_type bucket_size(size_type n);
size_type bucket(const key_type& k) const;
local_iterator begin(size_type n) const;
const_local_iterator begin(size_type n) const;
local_iterator end(size_type n);
const_local_iterator end(size_type n) const;

// hash policy
float load_factor() const;
float max_load_factor() const;
void max_load_factor(float z);
void rehash(size_type n);
};

template <class Key, class T, class Hash, class Pred, class Alloc>
void swap(unordered_map<Key, T, Hash, Pred, Alloc>& x,
          unordered_map<Key, T, Hash, Pred, Alloc>& y);

```

6.3.4.4.1 unordered_map constructors

[tr.unord.map.cnstr]

```

explicit unordered_map(size_type n = implementation-defined,
                      const hasher& hf = hasher(),
                      const key_equal& eql = key_equal(),
                      const allocator_type& a = allocator_type());

```

1 *Effects:* Constructs an empty unordered_map using the specified hash function, key equality function, and allocator, and using at least *n* buckets. If *n* is not provided, the number of buckets is implementation defined. *max_load_factor()* is 1.0.

2 *Complexity:* Constant.

```

template <class InputIterator>
unordered_map(InputIterator f, InputIterator l,

```

```

size_type n = implementation-defined,
const hasher& hf = hasher(),
const key_equal& eql = key_equal(),
const allocator_type& a = allocator_type());
```

- 3 *Effects:* Constructs an empty `unordered_map` using the specified hash function, key equality function, and allocator, and using at least `n` buckets. (If `n` is not provided, the number of buckets is implementation defined.) Then inserts elements from the range $[f, l]$. `max_load_factor()` is 1.0.

- 4 *Complexity:* Average case linear, worst case quadratic.

6.3.4.4.2 `unordered_map` element access

[tr.unord.map.elem]

```
mapped_type& operator[](const key_type& k);
```

- 1 *Effects:* If the `unordered_map` does not already contain an element whose key is equivalent to `k`, inserts the value `std::pair<const key_type, mapped_type>(k, mapped_type())`.
- 2 *Returns:* A reference to `x.second`, where `x` is the (unique) element whose key is equivalent to `k`.

6.3.4.4.3 `unordered_map` swap

[tr.unord.map.swap]

```

template <class Value, class Hash, class Pred, class Alloc>
void swap(unordered_map<Value, Hash, Pred, Alloc>& x,
          unordered_map<Value, Hash, Pred, Alloc>& y);
```

- 1 *Effects:* `x.swap(y)`.

6.3.4.5 Class template `unordered_multiset`

[tr.unord.multiset]

- 1 An `unordered_multiset` is a kind of unordered associative container that supports equivalent keys (an `unordered_multiset` may contain multiple copies of the same key value) and in which the elements' keys are the elements themselves.
- 2 An `unordered_multiset` satisfies all of the requirements of a container and of a unordered associative container. It provides the operations described in the preceding requirements table for equivalent keys; that is, an `unordered_multiset` supports the `a_eq` operations in that table, not the `a_uniq` operations. For an `unordered_multiset<Value>` the `key_type` and the `value_type` are both `Value`. The `iterator` and `const_iterator` types are both `const iterator` types. It is unspecified whether or not they are the same type.
- 3 This section only describes operations on `unordered_multiset` that are not described in one of the requirement tables, or for which there is additional semantic information.

```

template <class Value,
          class Hash = hash<Value>,
          class Pred = std::equal_to<Value>,
          class Alloc = std::allocator<Value> >
class unordered_multiset
{
```

```

public:
    // types
    typedef Value                                key_type;
    typedef Value                                value_type;
    typedef Hash                                 hasher;
    typedef Pred                                key_equal;
    typedef Alloc                               allocator_type;
    typedef typename allocator_type::pointer      pointer;
    typedef typename allocator_type::const_pointer const_pointer;
    typedef typename allocator_type::reference    reference;
    typedef typename allocator_type::const_reference const_reference;
    typedef implementation-defined               size_type;
    typedef implementation-defined               difference_type;

    typedef implementation-defined              iterator;
    typedef implementation-defined              const_iterator;
    typedef implementation-defined              local_iterator;
    typedef implementation-defined              const_local_iterator;

// construct/destroy/copy
explicit unordered_multiset(size_type n = implementation-defined,
                             const hasher& hf = hasher(),
                             const key_equal& eql = key_equal(),
                             const allocator_type& a = allocator_type());
template <class InputIterator>
unordered_multiset(InputIterator f, InputIterator l,
                  size_type n = implementation-defined,
                  const hasher& hf = hasher(),
                  const key_equal& eql = key_equal(),
                  const allocator_type& a = allocator_type());
unordered_multiset(const unordered_multiset&);
~unordered_multiset();
unordered_multiset& operator=(const unordered_multiset&);

allocator_type get_allocator() const;

// size and capacity
bool empty() const;
size_type size() const;
size_type max_size() const;

// iterators
iterator begin();
const_iterator begin() const;
iterator end();
const_iterator end() const;

// modifiers
iterator insert(const value_type& obj);
iterator insert(const_iterator hint, const value_type& obj);

```

```

template <class InputIterator>
void insert(InputIterator first, InputIterator last);

void erase(const_iterator position);
size_type erase(const key_type& k);
void erase(const_iterator first, const_iterator last);
void clear();

void swap(unordered_multiset&);

// observers
hasher hash_function() const;
key_equal key_eq() const;

// lookup
iterator find(const key_type& k);
const_iterator find(const key_type& k) const;
size_type count(const key_type& k) const;
std::pair<iterator, iterator>
    equal_range(const key_type& k);
std::pair<const_iterator, const_iterator>
    equal_range(const key_type& k) const;

// bucket interface
size_type bucket_count() const;
size_type max_bucket_count() const;
size_type bucket_size(size_type n);
size_type bucket(const key_type& k) const;
local_iterator begin(size_type n) const;
const_local_iterator begin(size_type n) const;
local_iterator end(size_type n);
const_local_iterator end(size_type n) const;

// hash policy
float load_factor() const;
float max_load_factor() const;
void max_load_factor(float z);
void rehash(size_type n);
};

template <class Value, class Hash, class Pred, class Alloc>
void swap(unordered_multiset<Value, Hash, Pred, Alloc>& x,
          unordered_multiset<Value, Hash, Pred, Alloc>& y);
}

```

6.3.4.5.1 unordered_multiset constructors

[tr.unord.multiset.cnstr]

```

explicit unordered_multiset(size_type n = implementation-defined,
                           const hasher& hf = hasher(),
                           const key_equal& eql = key_equal(),
                           
```

```
const allocator_type& a = allocator_type();
```

- 1 *Effects:* Constructs an empty `unordered_multiset` using the specified hash function, key equality function, and allocator, and using at least n buckets. If n is not provided, the number of buckets is implementation defined. `max_load_factor()` is 1.0.

- 2 *Complexity:* Constant.

```
template <class InputIterator>
unordered_multiset(InputIterator f, InputIterator l,
                  size_type n = implementation-defined,
                  const hasher& hf = hasher(),
                  const key_equal& eql = key_equal(),
                  const allocator_type& a = allocator_type());
```

- 3 *Effects:* Constructs an empty `unordered_multiset` using the specified hash function, key equality function, and allocator, and using at least n buckets. (If n is not provided, the number of buckets is implementation defined.) Then inserts elements from the range $[f, l]$. `max_load_factor()` is 1.0.

- 4 *Complexity:* Average case linear, worst case quadratic.

6.3.4.5.2 `unordered_multiset swap`

[\[tr.unord.multiset.swap\]](#)

```
template <class Value, class Hash, class Pred, class Alloc>
void swap(unordered_multiset<Value, Hash, Pred, Alloc>& x,
          unordered_multiset<Value, Hash, Pred, Alloc>& y);

pnumEffects: x.swap(y);
```

6.3.4.6 Class template `unordered_multimap`

[\[tr.unord.multimap\]](#)

- 1 An `unordered_multimap` is a kind of unordered associative container that supports equivalent keys (an `unordered_multimap` may contain multiple copies of each key value) and that associates values of another type `mapped_type` with the keys.
- 2 An `unordered_multimap` satisfies all of the requirements of a container and of an unordered associative container. It provides the operations described in the preceding requirements table for equivalent keys; that is, an `unordered_multimap` supports the `a_eq` operations in that table, not the `a_uniq` operations. For an `unordered_multimap<Key, T>` the key type is `Key`, the mapped type is `T`, and the value type is `std::pair<const Key, T>`.
- 3 This section only describes operations on `unordered_multimap` that are not described in one of the requirement tables, or for which there is additional semantic information.

```
template <class Key,
         class T,
         class Hash = hash<Key>,
         class Pred = std::equal_to<Key>,
         class Alloc = std::allocator<std::pair<const Key, T>>>
class unordered_multimap
{
```

```

public:
    // types
    typedef Key                                key_type;
    typedef std::pair<const Key, T>              value_type;
    typedef T                                   mapped_type;
    typedef Hash                               hasher;
    typedef Pred                               key_equal;
    typedef Alloc                             allocator_type;
    typedef typename allocator_type::pointer   pointer;
    typedef typename allocator_type::const_pointer const_pointer;
    typedef typename allocator_type::reference  reference;
    typedef typename allocator_type::const_reference const_reference;
    typedef implementation-defined           size_type;
    typedef implementation-defined           difference_type;

    typedef implementation-defined          iterator;
    typedef implementation-defined          const_iterator;
    typedef implementation-defined          local_iterator;
    typedef implementation-defined          const_local_iterator;

    // construct/destroy/copy
    explicit unordered_multimap(size_type n = implementation-defined,
                                 const hasher& hf = hasher(),
                                 const key_equal& eql = key_equal(),
                                 const allocator_type& a = allocator_type());
    template <class InputIterator>
    unordered_multimap(InputIterator f, InputIterator l,
                      size_type n = implementation-defined,
                      const hasher& hf = hasher(),
                      const key_equal& eql = key_equal(),
                      const allocator_type& a = allocator_type());
    unordered_multimap(const unordered_multimap&);
    ~unordered_multimap();
    unordered_multimap& operator=(const unordered_multimap&);

    allocator_type get_allocator() const;

    // size and capacity
    bool empty() const;
    size_type size() const;
    size_type max_size() const;

    // iterators
    iterator begin();
    const_iterator begin() const;
    iterator end();
    const_iterator end() const;

    // modifiers
    iterator insert(const value_type& obj);
    iterator insert(const_iterator hint, const value_type& obj);

```

```

template <class InputIterator>
void insert(InputIterator first, InputIterator last);

void erase(const_iterator position);
size_type erase(const key_type& k);
void erase(const_iterator first, const_iterator last);
void clear();

void swap(unordered_multimap&);

// observers
hasher hash_function() const;
key_equal key_eq() const;

// lookup
iterator find(const key_type& k);
const_iterator find(const key_type& k) const;
size_type count(const key_type& k) const;
std::pair<iterator, iterator>
    equal_range(const key_type& k);
std::pair<const_iterator, const_iterator>
    equal_range(const key_type& k) const;

// bucket interface
size_type bucket_count() const;
size_type max_bucket_count() const;
size_type bucket_size(size_type n);
size_type bucket(const key_type& k) const;
local_iterator begin(size_type n) const;
const_local_iterator begin(size_type n) const;
local_iterator end(size_type n);
const_local_iterator end(size_type n) const;

// hash policy
float load_factor() const;
float max_load_factor() const;
void max_load_factor(float z);
void rehash(size_type n);
};

template <class Key, class T, class Hash, class Pred, class Alloc>
void swap(unordered_multimap<Key, T, Hash, Pred, Alloc>& x,
          unordered_multimap<Key, T, Hash, Pred, Alloc>& y);

```

6.3.4.6.1 unordered_multimap constructors

[tr.unord.multimap.cnstr]

```

explicit unordered_multimap(size_type n = implementation-defined,
                           const hasher& hf = hasher(),
                           const key_equal& eql = key_equal(),
                           const allocator_type& a = allocator_type());

```

1 *Effects:* Constructs an empty `unordered_multimap` using the specified hash function, key equality function, and allocator, and using at least n buckets. If n is not provided, the number of buckets is implementation defined. `max_load_factor()` is 1.0.

2 *Complexity:* Constant.

```
template <class InputIterator>
unordered_multimap(InputIterator f, InputIterator l,
                   size_type n = implementation-defined,
                   const hasher& hf = hasher(),
                   const key_equal& eql = key_equal(),
                   const allocator_type& a = allocator_type());
```

3 *Effects:* Constructs an empty `unordered_multimap` using the specified hash function, key equality function, and allocator, and using at least n buckets. (If n is not provided, the number of buckets is implementation defined.) Then inserts elements from the range $[f, l)$. `max_load_factor()` is 1.0.

4 *Complexity:* Average case linear, worst case quadratic.

6.3.4.6.2 `unordered_multimap swap`

[\[tr.unord.multimap.swap\]](#)

```
template <class Value, class Hash, class Pred, class Alloc>
void swap(unordered_multimap<Value, Hash, Pred, Alloc>& x,
          unordered_multimap<Value, Hash, Pred, Alloc>& y);
```

1 *Effects:* `x.swap(y)`.

7 Regular expressions

[tr.re]

- 1 This clause describes components that C++ programs may use to perform operations involving regular expression matching and searching.

7.1 Definitions

[tr.re.def]

- 1 The following definitions shall apply to this clause:
- 2 *Collating element*: A sequence of one or more characters within the current locale that collate as if they were a single character.
- 3 *Finite state machine*: An unspecified data structure that is used to represent a regular expression, and which permits efficient matches against the regular expression to be obtained.
- 4 *Format specifier*: A sequence of one or more characters that is to be replaced with some part of a regular expression match.
- 5 *Matched*: A sequence of zero or more characters shall be said to be matched by a regular expression when the characters in the sequence correspond to a sequence of characters defined by the pattern.
- 6 *Partial match*: A match that is obtained by matching one or more characters at the end of a character-container sequence, but only a prefix of the regular expression.
- 7 *Primary equivalence class*: A set of one or more characters which share the same primary sort key: that is the sort key weighting that depends only upon character shape, and not accentuation, case, or locale specific tailorings.
- 8 *Regular expression*: A pattern that selects specific strings from a set of character strings.
- 9 *Sub-expression*: A subset of a regular expression that has been marked by parenthesis.

7.2 Requirements

[tr.re.req]

- 1 This subclause defines requirements on classes representing regular expression traits. [Note: The class template `regex_traits<charT>`, defined in clause 7.7, satisfies these requirements. —end note]
- 2 The class template `basic_regex`, defined in clause 7.8, needs a set of related types and functions to complete the definition of its semantics. These types and functions are provided as a set of member typedefs and functions in the template parameter `traits` used by the `basic_regex` class template. This subclause defines the semantics guaranteed by these members.
- 3 To specialize the `basic_regex` template to generate a regular expression class to handle a particular character container type `CharT`, that and its related regular expression traits class `Traits` is passed as a pair of parameters to the `basic_regex` template as formal parameters `charT` and `Traits`.

- 4 In Table 15 X denotes a traits class defining types and functions for the character container type `charT`; u is an object of type X; v is an object of type `const X`; p is a value of type `const charT*`; I1 and I2 are Input Iterators; F1 and F2 are forward iterators; c is a value of type `const charT`; s is an object of type `X::string_type`; cs is an object of type `const X::string_type`; b is a value of type `bool`; I is a value of type `int`; and loc is an object of type `X::locale_type`.

Table 15: regular expression traits class requirements

expression	Return Type	Assertion / Note / Pre / Post condition
<code>X::char_type</code>	<code>charT</code>	The character container type used in the implementation of class template <code>basic_regex</code> .
<code>X::size_type</code>		An unsigned integer type, capable of holding the length of a null-terminated string of <code>charTs</code> .
<code>X::string_type</code>	<code>std::basic_string<charT></code>	
<code>X::locale_type</code>	Implementation defined	A copy constructible type that represents the locale used by the traits class.
<code>X::char_class_type</code>	Implementation defined	A bitmask type representing a particular character classification. Multiple values of this type can be bitwise-or'ed together to obtain a new valid value.
<code>X::length(p)</code>	<code>X::size_type</code>	Yields the smallest i such that <code>p[i] == 0</code> . Complexity is linear in i .
<code>v.translate(c)</code>	<code>X::char_type</code>	Returns a character such that for any character d that is to be considered equivalent to c then <code>v.translate(c) == v.translate(d)</code> .
<code>v.translate_nocase(c)</code>	<code>X::char_type</code>	For all characters C that are to be considered equivalent to c when comparisons are to be performed without regard to case, then <code>v.translate_nocase(c) == v.translate_nocase(C)</code> .
<code>v.transform(F1, F2)</code>	<code>X::string_type</code>	Returns a sort key for the character sequence designated by the iterator range [F1, F2) such that if the character sequence [G1, G2) sorts before the character sequence [H1, H2) then <code>v.transform(G1, G2) < v.transform(H1, H2)</code> .
<code>v.transform_primary(F1, F2)</code>	<code>X::string_type</code>	Returns a sort key for the character sequence designated by the iterator range [F1, F2) such that if the character sequence [G1, G2) sorts before the character sequence [H1, H2) when character case is not considered then <code>v.transform_primary(G1, G2) < v.transform_primary(H1, H2)</code> .

expression	Return Type	Assertion / Note / Pre / Post condition
v.lookup_classname(F1, F2)	X::char_class_- type	Converts the character sequence designated by the iterator range [F1,F2] into a bitmask type that can subsequently be passed to <code>isctype</code> . Values returned from <code>lookup_classname</code> can be safely bitwise or'ed together. Returns 0 if the character sequence is not the name of a character class recognized by X. The value returned shall be independent of the case of the characters in the sequence.
v.lookup_collatename(F1, F2)	X::string_type	Returns a sequence of characters that represents the collating element consisting of the character sequence designated by the iterator range [F1, F2]. Returns an empty string if the character sequence is not a valid collating element.
v.isctype(c, v.lookup_classname (F1, F2))	bool	Returns true if character c is a member of the character class designated by the iterator range [F1, F2], false otherwise.
v.value(c, I)	int	Returns the value represented by the digit c in base I if the character c is a valid digit in base I; otherwise returns -1. [Note: the value of I will only be 8, 10, or 16. —end note]
u.imbue(loc)	X::locale_type	Imbues u with the locale loc and returns the previous locale used by u if any.
v.getloc()	X::locale_type	Returns the current locale used by v, if any.

- 5 The header <regex> defines the class template `regex_traits` which shall be capable of being specialized for character container types `char` and `wchar_t`, and which satisfies the requirements for a regular expression traits class. Class template `regex_traits` is described in clause 7.7.

7.3 Regular expressions summary

[tr.re.sum]

- 1 The header <regex> defines a basic regular expression class template and its traits that can handle all char-like (lib.strings) template arguments.
- 2 The header <regex> defines a class template that holds the result of a regular expression match.
- 3 The header <regex> defines a series of algorithms that allow an iterator sequence to be operated upon by a regular expression.
- 4 The header <regex> defines two specific template classes, `regex` and `wregex`, and their special traits.
- 5 The header <regex> also defines two iterator types for enumerating regular expression matches.

7.4 Header <regex> synopsis

[tr.re.syn]

```
namespace std {
namespace tr1 {
```

```

// [7.5] Regex constants
namespace regex_constants {
    typedef bitmask_type syntax_option_type;
    typedef bitmask_type match_flag_type;
    typedef implementation-defined error_type;
} // namespace regex_constants

// [7.6] Class regex_error
class regex_error;

// [7.7] Class template regex_traits
template <class charT>
struct regex_traits;

// [7.8] Class template basic_regex
template <class charT,
           class traits = regex_traits<charT> >
class basic_regex;

typedef basic_regex<char> regex;
typedef basic_regex<wchar_t> wregex;

// [7.8.7] basic_regex swap
template <class charT, class traits>
void swap(basic_regex<charT, traits>& e1,
          basic_regex<charT, traits>& e2);

// [7.9] Class template sub_match
template <class BidirectionalIterator>
class sub_match;
typedef sub_match<const char*> csub_match;
typedef sub_match<const wchar_t*> wcsub_match;
typedef sub_match<string::const_iterator> ssub_match;
typedef sub_match<wstring::const_iterator> wssub_match;

// [7.9.2] sub_match non-member operators
template <class BiIter>
bool operator==(const sub_match<BiIter>& lhs, const sub_match<BiIter>& rhs);
template <class BiIter>
bool operator!=(const sub_match<BiIter>& lhs, const sub_match<BiIter>& rhs);
template <class BiIter>
bool operator<(const sub_match<BiIter>& lhs, const sub_match<BiIter>& rhs);
template <class BiIter>
bool operator<=(const sub_match<BiIter>& lhs, const sub_match<BiIter>& rhs);
template <class BiIter>
bool operator>=(const sub_match<BiIter>& lhs, const sub_match<BiIter>& rhs);
template <class BiIter>
bool operator>(const sub_match<BiIter>& lhs, const sub_match<BiIter>& rhs);

```

```

template <class BiIter, class traits, class Alloc>
bool operator==(const std::basic_string<iterator_traits<BiIter>::value_type,
                  traits, Alloc>& lhs,
                  const sub_match<BiIter>& rhs);
template <class BiIter, class traits, class Alloc>
bool operator!=(const std::basic_string<iterator_traits<BiIter>::value_type,
                  traits, Alloc>& lhs,
                  const sub_match<BiIter>& rhs);
template <class BiIter, class traits, class Alloc>
bool operator<(const std::basic_string<iterator_traits<BiIter>::value_type,
                  traits, Alloc>& lhs,
                  const sub_match<BiIter>& rhs);
template <class BiIter, class traits, class Alloc>
bool operator>(const std::basic_string<iterator_traits<BiIter>::value_type,
                  traits, Alloc>& lhs,
                  const sub_match<BiIter>& rhs);
template <class BiIter, class traits, class Alloc>
bool operator>=(const std::basic_string<iterator_traits<BiIter>::value_type,
                  traits, Alloc>& lhs,
                  const sub_match<BiIter>& rhs);
template <class BiIter, class traits, class Alloc>
bool operator<=(const std::basic_string<iterator_traits<BiIter>::value_type,
                  traits, Alloc>& lhs,
                  const sub_match<BiIter>& rhs);

template <class BiIter, class traits, class Alloc>
bool operator==(const sub_match<BiIter>& lhs,
                  const std::basic_string<iterator_traits<BiIter>::value_type,
                  traits, Alloc>& rhs);
template <class BiIter, class traits, class Alloc>
bool operator!=(const sub_match<BiIter>& lhs,
                  const std::basic_string<iterator_traits<BiIter>::value_type,
                  traits, Alloc>& rhs);
template <class BiIter, class traits, class Alloc>
bool operator<(const sub_match<BiIter>& lhs,
                  const std::basic_string<iterator_traits<BiIter>::value_type,
                  traits, Alloc>& rhs);
template <class BiIter, class traits, class Alloc>
bool operator>(const sub_match<BiIter>& lhs,
                  const std::basic_string<iterator_traits<BiIter>::value_type,
                  traits, Alloc>& rhs);
template <class BiIter, class traits, class Alloc>
bool operator>=(const sub_match<BiIter>& lhs,
                  const std::basic_string<iterator_traits<BiIter>::value_type,
                  traits, Alloc>& rhs);
template <class BiIter, class traits, class Alloc>
bool operator<=(const sub_match<BiIter>& lhs,
                  const std::basic_string<iterator_traits<BiIter>::value_type,
                  traits, Alloc>& rhs);

```

```

template <class BiIter>
bool operator==(typename iterator_traits<BiIter>::value_type const* lhs,
                  const sub_match<BiIter>& rhs);
template <class BiIter>
bool operator!=(typename iterator_traits<BiIter>::value_type const* lhs,
                  const sub_match<BiIter>& rhs);
template <class BiIter>
bool operator<(typename iterator_traits<BiIter>::value_type const* lhs,
                  const sub_match<BiIter>& rhs);
template <class BiIter>
bool operator>(typename iterator_traits<BiIter>::value_type const* lhs,
                  const sub_match<BiIter>& rhs);
template <class BiIter>
bool operator>=(typename iterator_traits<BiIter>::value_type const* lhs,
                  const sub_match<BiIter>& rhs);
template <class BiIter>
bool operator<=(typename iterator_traits<BiIter>::value_type const* lhs,
                  const sub_match<BiIter>& rhs);

template <class BiIter>
bool operator==(const sub_match<BiIter>& lhs,
                  typename iterator_traits<BiIter>::value_type const* rhs);
template <class BiIter>
bool operator!=(const sub_match<BiIter>& lhs,
                  typename iterator_traits<BiIter>::value_type const* rhs);
template <class BiIter>
bool operator<(const sub_match<BiIter>& lhs,
                  typename iterator_traits<BiIter>::value_type const* rhs);
template <class BiIter>
bool operator>(const sub_match<BiIter>& lhs,
                  typename iterator_traits<BiIter>::value_type const* rhs);
template <class BiIter>
bool operator>=(const sub_match<BiIter>& lhs,
                  typename iterator_traits<BiIter>::value_type const* rhs);
template <class BiIter>
bool operator<=(const sub_match<BiIter>& lhs,
                  typename iterator_traits<BiIter>::value_type const* rhs);

template <class BiIter>
bool operator==(typename iterator_traits<BiIter>::value_type const& lhs,
                  const sub_match<BiIter>& rhs);
template <class BiIter>
bool operator!=(typename iterator_traits<BiIter>::value_type const& lhs,
                  const sub_match<BiIter>& rhs);
template <class BiIter>
bool operator<(typename iterator_traits<BiIter>::value_type const& lhs,
                  const sub_match<BiIter>& rhs);
template <class BiIter>
bool operator>(typename iterator_traits<BiIter>::value_type const& lhs,
                  const sub_match<BiIter>& rhs);

```

```

template <class BiIter>
bool operator>=(typename iterator_traits<BiIter>::value_type const& lhs,
                 const sub_match<BiIter>& rhs);
template <class BiIter>
bool operator<=(typename iterator_traits<BiIter>::value_type const& lhs,
                 const sub_match<BiIter>& rhs);

template <class BiIter>
bool operator==(const sub_match<BiIter>& lhs,
                  typename iterator_traits<BiIter>::value_type const& rhs);
template <class BiIter>
bool operator!=(const sub_match<BiIter>& lhs,
                  typename iterator_traits<BiIter>::value_type const& rhs);
template <class BiIter>
bool operator<(const sub_match<BiIter>& lhs,
                  typename iterator_traits<BiIter>::value_type const& rhs);
template <class BiIter>
bool operator>(const sub_match<BiIter>& lhs,
                  typename iterator_traits<BiIter>::value_type const& rhs);
template <class BiIter>
bool operator>=(const sub_match<BiIter>& lhs,
                  typename iterator_traits<BiIter>::value_type const& rhs);
template <class BiIter>
bool operator<=(const sub_match<BiIter>& lhs,
                  typename iterator_traits<BiIter>::value_type const& rhs);

template <class charT, class traits, class BiIter>
basic_ostream<charT, traits>&
operator<<(basic_ostream<charT, traits>& os, const sub_match<BiIter>& m);

// [7.10] Class template match_results
template <class BidirectionalIterator,
          class Allocator = allocator<
              typename iterator_traits<BidirectionalIterator>::value_type > >
class match_results;

typedef match_results<const char*> cmatch;
typedef match_results<const wchar_t*> wcmatch;
typedef match_results<string::const_iterator> smatch;
typedef match_results<wstring::const_iterator> wsmatch;

// match_result comparisons
template <class BidirectionalIterator, class Allocator>
bool operator == (const match_results<BidirectionalIterator, Allocator>& m1,
                  const match_results<BidirectionalIterator, Allocator>& m2);
template <class BidirectionalIterator, class Allocator>
bool operator != (const match_results<BidirectionalIterator, Allocator>& m1,
                  const match_results<BidirectionalIterator, Allocator>& m2);

// match_result I/O

```

```

template <class charT, class traits,
         class BidirectionalIterator, class Allocator>
basic_ostream<charT, traits>&
operator << (basic_ostream<charT, traits>& os,
              const match_results<BidirectionalIterator, Allocator>& m);

// [7.10.6] match_result swap
template <class BidirectionalIterator, class Allocator>
void swap(match_results<BidirectionalIterator, Allocator>& m1,
          match_results<BidirectionalIterator, Allocator>& m2);

// [7.11.2] Function template regex_match
template <class BidirectionalIterator, class Allocator,
          class charT, class traits>
bool regex_match(BidirectionalIterator first, BidirectionalIterator last,
                 match_results<BidirectionalIterator, Allocator>& m,
                 const basic_regex<charT, traits>& e,
                 regex_constants::match_flag_type flags
                 = regex_constants::match_default);
template <class BidirectionalIterator,
          class charT, class traits>
bool regex_match(BidirectionalIterator first, BidirectionalIterator last,
                 const basic_regex<charT, traits>& e,
                 regex_constants::match_flag_type flags
                 = regex_constants::match_default);
template <class charT, class Allocator, class traits>
bool regex_match(const charT* str, match_results<const charT*, Allocator>& m,
                 const basic_regex<charT, traits>& e,
                 regex_constants::match_flag_type flags
                 = regex_constants::match_default);
template <class ST, class SA, class Allocator,
          class charT, class traits>
bool regex_match(const basic_string<charT, ST, SA>& s,
                 match_results<typename basic_string<charT, ST, SA>
                               ::const_iterator,
                               Allocator>& m,
                 const basic_regex<charT, traits>& e,
                 regex_constants::match_flag_type flags
                 = regex_constants::match_default);
template <class charT, class traits>
bool regex_match(const charT* str,
                 const basic_regex<charT, traits>& e,
                 regex_constants::match_flag_type flags
                 = regex_constants::match_default);
template <class ST, class SA, class charT, class traits>
bool regex_match(const basic_string<charT, ST, SA>& s,
                 const basic_regex<charT, traits>& e,
                 regex_constants::match_flag_type flags
                 = regex_constants::match_default);

```

```

// [7.11.3] Function template regex_search
template <class BidirectionalIterator, class Allocator,
          class charT, class traits>
bool regex_search(BidirectionalIterator first, BidirectionalIterator last,
                  match_results<BidirectionalIterator, Allocator>& m,
                  const basic_regex<charT, traits>& e,
                  regex_constants::match_flag_type flags
                  = regex_constants::match_default);
template <class BidirectionalIterator,
          class charT, class traits>
bool regex_search(BidirectionalIterator first, BidirectionalIterator last,
                  const basic_regex<charT, traits>& e,
                  regex_constants::match_flag_type flags
                  = regex_constants::match_default);
template <class charT, class Allocator, class traits>
bool regex_search(const charT* str,
                  match_results<const charT*, Allocator>& m,
                  const basic_regex<charT, traits>& e,
                  regex_constants::match_flag_type flags
                  = regex_constants::match_default);
template <class charT, class traits>
bool regex_search(const charT* str
                  const basic_regex<charT, traits>& e,
                  regex_constants::match_flag_type flags
                  = regex_constants::match_default);
template <class ST, class SA,
          class charT, class traits>
bool regex_search(const basic_string<charT, ST, SA>& s,
                  const basic_regex<charT, traits>& e,
                  regex_constants::match_flag_type flags
                  = regex_constants::match_default);
template <class ST, class SA, class Allocator,
          class charT, class traits>
bool regex_search(const basic_string<charT, ST, SA>& s,
                  match_results<typename basic_string<charT, ST, SA>
                               ::const_iterator,
                               Allocator>& m,
                  const basic_regex<charT, traits>& e,
                  regex_constants::match_flag_type flags
                  = regex_constants::match_default);

// [7.11.4] Function template regex_replace
template <class OutputIterator, class BidirectionalIterator,
          class traits, class charT>
OutputIterator regex_replace(OutputIterator out,
                            BidirectionalIterator first,
                            BidirectionalIterator last,
                            const basic_regex<charT, traits>& e,
                            const basic_string<charT>& fmt,
                            regex_constants::match_flag_type flags

```

```

        = regex_constants::match_default);
template <class traits, class charT>
basic_string<charT> regex_replace(const basic_string<charT>& s,
                                   const basic_regex<charT, traits>& e,
                                   const basic_string<charT>& fmt,
                                   regex_constants::match_flag_type flags
                                   = regex_constants::match_default);

// [7.12.1] Class template regex_iterator
template <class BidirectionalIterator,
           class charT = iterator_traits<BidirectionalIterator>::value_type,
           class traits = regex_traits<charT> >
class regex_iterator;
typedef regex_iterator<const char*> cregex_iterator;
typedef regex_iterator<const wchar_t*> wcregex_iterator;
typedef regex_iterator<string::const_iterator> sregex_iterator;
typedef regex_iterator<wstring::const_iterator> wsregex_iterator;

// [7.12.2] Class template regex_token_iterator
template <class BidirectionalIterator,
           class charT = iterator_traits<BidirectionalIterator>::value_type,
           class traits = regex_traits<charT> >
class regex_token_iterator;
typedef regex_token_iterator<const char*> cregex_token_iterator;
typedef regex_token_iterator<const wchar_t*> wcregex_token_iterator;
typedef regex_token_iterator<string::const_iterator> sregex_token_iterator;
typedef regex_token_iterator<wstring::const_iterator> wcregex_token_iterator;

} // namespace tr1
} // namespace std

```

7.5 Namespace `tr1::regex_constants`

[tr.re.const]

- 1 The namespace `tr1::regex_constants` acts as a repository for the symbolic constants used by the regular expression library. This namespace provides three types, `syntax_option_type`, `match_flag_type`, and `error_type`, along with a series of constants of these types.

7.5.1 Bitmask Type `syntax_option_type`

[tr.re.synopt]

```

namespace tr1 { namespace regex_constants {

typedef bitmask_type syntax_option_type;
// these flags are required:
static const syntax_option_type icase;
static const syntax_option_type nosubs;
static const syntax_option_type optimize;
static const syntax_option_type collate;
static const syntax_option_type ECMAScript;
// these flags are optional; if the functionality is supported
// then the flags shall take these names.

```

```

static const syntax_option_type basic;
static const syntax_option_type extended;
static const syntax_option_type awk;
static const syntax_option_type grep;
static const syntax_option_type egrep;

} // namespace regex_constants
} // namespace tr1

```

- 1 The type `syntax_option_type` is an implementation defined bitmask type (§17.3.2.1.2). Setting its elements has the effects listed in table 16. A valid value of type `syntax_option_type` shall have exactly one of the elements `ECMAScript`, `basic`, `extended`, `awk`, `grep`, `egrep`, `set`.

Table 16: `syntax_option_type` effects

Element	Effect(s) if set
<code>icase</code>	Specifies that matching of regular expressions against a character container sequence shall be performed without regard to case.
<code>nosubs</code>	Specifies that when a regular expression is matched against a character container sequence, then no sub-expression matches are to be stored in the supplied <code>match_results</code> structure.
<code>optimize</code>	Specifies that the regular expression engine should pay more attention to the speed with which regular expressions are matched, and less to the speed with which regular expression objects are constructed. Otherwise it has no detectable effect on the program output.
<code>collate</code>	Specifies that character ranges of the form “[a-b]” should be locale sensitive.
<code>ECMAScript</code>	Specifies that the grammar recognized by the regular expression engine uses its normal semantics: that is the same as that given in the ECMA-262 [7].
<code>basic</code>	Specifies that the grammar recognized by the regular expression engine is the same as that used by POSIX basic regular expressions [11] in IEEE Std 1003.1-2001, Portable Operating System Interface (POSIX), Base Definitions and Headers, Section 9, Regular Expressions .
<code>extended</code>	Specifies that the grammar recognized by the regular expression engine is the same as that used by POSIX extended regular expressions [11] in IEEE Std 1003.1-2001, Portable Operating System Interface (POSIX), Base Definitions and Headers, Section 9, Regular Expressions .
<code>awk</code>	Specifies that the grammar recognized by the regular expression engine is the same as that used by POSIX utility <code>awk</code> in IEEE Std 1003.1-2001 [11].
<code>grep</code>	Specifies that the grammar recognized by the regular expression engine is the same as that used by POSIX utility <code>grep</code> in IEEE Std 1003.1-2001 [11].
<code>egrep</code>	Specifies that the grammar recognized by the regular expression engine is the same as that used by POSIX utility <code>grep</code> when given the <code>-E</code> option in IEEE Std 1003.1-2001 [11].

7.5.2 Bitmask Type `regex_constants::match_flag_type`

[tr.re.matchflag]

```

namespace tr1 { namespace regex_constants{

typedef bitmask_type regex_constants::match_flag_type;

static const regex_constants::match_flag_type match_default = 0;
static const regex_constants::match_flag_type match_not_bol;
static const regex_constants::match_flag_type match_not_eol;
static const regex_constants::match_flag_type match_not_bow;
static const regex_constants::match_flag_type match_not_eow;
static const regex_constants::match_flag_type match_any;
static const regex_constants::match_flag_type match_not_null;
static const regex_constants::match_flag_type match_continuous;
static const regex_constants::match_flag_type match_partial;
static const regex_constants::match_flag_type match_prev_avail;
static const regex_constants::match_flag_type format_default = 0;
static const regex_constants::match_flag_type format_sed;
static const regex_constants::match_flag_type format_perl;
static const regex_constants::match_flag_type format_no_copy;
static const regex_constants::match_flag_type format_first_only;

} // namespace regex_constants
} // namespace tr1

```

- 1 The type `regex_constants::match_flag_type` is an implementation defined bitmask type (§17.3.2.1.2). Matching a regular expression against a sequence of characters [first, last) proceeds according to the normal rules of ECMA-262 [7], modified according to the effects listed in table 17 for any bitmask elements set.

7.5.3 Implementation defined `error_type`

[tr.re.err]

```

namespace tr1 { namespace regex_constants {

typedef implementation_defined error_type;

static const error_type error_collate;
static const error_type error_ctype;
static const error_type error_escape;
static const error_type error_backref;
static const error_type error_brack;
static const error_type error_paren;
static const error_type error_brace;
static const error_type error_badbrace;
static const error_type error_range;
static const error_type error_space;
static const error_type error_badrepeat;
static const error_type error_complexity;
static const error_type error_stack;

} // namespace regex_constants
} // namespace tr1

```

Table 17: `regex_constants::match_flag_type` effects when obtaining a match against a character container sequence `[first, last)`.

Element	Effect(s) if set
<code>match_not_bol</code>	The first character in the sequence <code>[first, last)</code> is treated as though it is not at the beginning of a line, so the character " <code>^</code> " in the regular expression shall not match <code>[first, first)</code> .
<code>match_not_eol</code>	The last character in the sequence <code>[first, last)</code> is treated as though it is not at the end of a line, so the character " <code>\$</code> " in the regular expression shall not match <code>[last, last)</code> .
<code>match_not_bow</code>	The expression " <code>\b</code> " is not matched against the sub-sequence <code>[first, first)</code> .
<code>match_not_eow</code>	The expression " <code>\B</code> " should not be matched against the sub-sequence <code>[last, last)</code> .
<code>match_any</code>	If more than one match is possible then any match is an acceptable result.
<code>match_not_null</code>	The expression does not match an empty sequence.
<code>match_continuous</code>	The expression only matches a sub-sequence that begins at <code>first</code> .
<code>match_partial</code>	If no match is found, then it is acceptable to return a match <code>[from, last)</code> where <code>from!=last</code> , if there exists some sequence of characters <code>[from,to)</code> of which <code>[from,last)</code> is a prefix, and which would result in a full match.
<code>match_prev_avail</code>	- <code>first</code> is a valid iterator position. When this flag is set then the flags <code>match_not_bol</code> and <code>match_not_bow</code> are ignored by the regular expression algorithms 7.11 and iterators 7.12.
<code>format_default</code>	When a regular expression match is to be replaced by a new string, the new string is constructed using the rules used by the ECMAScript replace function in ECMA-262 [7], part 15.4.11 <code>String.prototype.replace</code> . In addition, during search and replace operations all non-overlapping occurrences of the regular expression are located and replaced, and sections of the input that did not match the expression, are copied unchanged to the output string.
<code>format_sed</code>	When a regular expression match is to be replaced by a new string, the new string is constructed using the rules used by the POSIX sed utility in IEEE Std 1003.1-2001 [11].
<code>format_perl</code>	When a regular expression match is to be replaced by a new string, the new string is constructed using an implementation defined superset of the rules used by the ECMAScript replace function in ECMA-262 [7], part 15.4.11 <code>String.prototype.replace</code> .
<code>format_no_copy</code>	During a search and replace operation, sections of the character container sequence being searched that do match the regular expression are not copied to the output string.
<code>format_first_only</code>	When specified during a search and replace operation, only the first occurrence of the regular expression is replaced.

- 1 The type `error_type` is an implementation defined enumeration type (§17.3.2.1.2). Values of type `error_type` represent the error conditions as described in table 18:

Table 18: `error_type` values in the C locale

Value	Error condition
<code>error_collate</code>	The expression contained an invalid collating element name.
<code>error_ctype</code>	The expression contained an invalid character class name.
<code>error_escape</code>	The expression contained an invalid escaped character, or a trailing escape.
<code>error_backref</code>	The expression contained an invalid backreference.
<code>error_brack</code>	The expression contained mismatched [and].
<code>error_paren</code>	The expression contained mismatched (and).
<code>error_brace</code>	The expression contained mismatched { and }
<code>error_badbrace</code>	The expression contained an invalid range in a {} expression.
<code>error_range</code>	The expression contained an invalid character range, for example [b-a].
<code>error_space</code>	There was insufficient memory to convert the expression into a finite state machine.
<code>error_badrepeat</code>	One of *?+{ was not preceded by a valid regular expression.
<code>error_complexity</code>	The complexity of an attempted match against a regular expression exceeded a pre-set level.
<code>error_stack</code>	There was insufficient memory to determine whether the regular expression could match the specified character sequence.

7.6 Class regex_error

[tr.re.badexp]

```
class regex_error : public std::runtime_error
{
public:
    explicit regex_error(regex_constants::error_type ecode);
    regex_constants::error_type code() const;
};
```

- 1 The class `regex_error` defines the type of objects thrown as exceptions to report errors from the regular expression library.

2 *Effects:* Constructs an object of class `regex_error`.

3 *Postcondition:* `ecode == code()`

4 *Returns:* The error code that was passed to the constructor.

7.7 Class template regex_traits

[tr.re.traits]

```

template <class charT>
struct regex_traits
{
public:
    typedef charT           char_type;
    typedef std::size_t      size_type;
    typedef std::basic_string<char_type> string_type;
    typedef std::locale      locale_type;
    typedef bitmask_type    char_class_type;

    regex_traits();
    static size_type length(const char_type* p);
    charT translate(charT c) const;
    charT translate_nocase(charT c) const;
    template <class ForwardIterator>
        string_type transform(ForwardIterator first,
                              ForwardIterator last) const;
    template <class ForwardIterator>
        string_type transform_primary(ForwardIterator first,
                                       ForwardIterator last) const;
    template <class ForwardIterator>
        char_class_type lookup_classname(ForwardIterator first,
                                         ForwardIterator last) const;
    template <class ForwardIterator>
        string_type lookup_collatename(ForwardIterator first,
                                       ForwardIterator last) const;
    bool isctype(charT c, char_class_type f) const;
    int value(charT ch, int radix) const;
    locale_type imbue(locale_type l);
    locale_type getloc() const;
};

```

- 1 The class template `regex_traits` is capable of being specialized for the types `char` and `wchar_t` and satisfies the requirements for a regular expression traits class (7.2).

```
typedef bitmask_type           char_class_type;
```

- 2 The type `char_class_type` is used to represent a character classification and is capable of holding an implementation specific set returned by `lookup_classname`.

```

static size_type length(const char_type* p);

3     Returns: char_traits<charT>::length(p);

charT translate(charT c) const;

4     Returns: (c).

charT translate_nocase(charT c) const;

5     Returns: use_facet<ctype<charT>>(getloc()).tolower(c).

```

```
template <class ForwardIterator>
string_type transform(ForwardIterator first,
    ForwardIterator last) const;
```

6 *Effects:*

```
        string_type str(first, last);
        return use_facet<collate<charT>>(getloc()).transform(
            &str.begin(), &str.end());
```

```
template <class ForwardIterator>
string_type transform_primary(ForwardIterator first,
    ForwardIterator last) const;
```

7 *Effects:* if `typeid(use_facet<collate<charT>>)` == `typeid(collate_byname<charT>)` and the form of the sort key returned by `collate_byname<charT> ::transform(first, last)` is known and can be converted into a primary sort key then returns that key, otherwise returns an empty string.

```
template <class ForwardIterator>
char_class_type lookup_classname(ForwardIterator first,
    ForwardIterator last) const;
```

8 *Returns:* an unspecified value that represents the character classification named by the character sequence designated by the iterator range `[first, last]`. The value returned shall be independent of the case of the characters in the character sequence. If the name is not recognized then returns a value that compares equal to 0.

9 *Notes:* For `regex_traits<char>`, at least the names "d", "w", "s", "alnum", "alpha", "blank", "cntrl", "digit", "graph", "lower", "print", "punct", "space", "upper" and "xdigit" shall be recognized. For `regex_traits<wchar_t>`, at least the names L"d", L"w", L"s", L"alnum", L"alpha", L"blank", L"cntrl", L"digit", L"graph", L"lower", L"print", L"punct", L"space", L"upper" and L"xdigit" shall be recognized.

```
template <class ForwardIterator>
string_type lookup_collatename(ForwardIterator first,
    ForwardIterator last) const;
```

10 *Returns:* a sequence of one or more characters that represents the collating element consisting of the character sequence designated by the iterator range `[first, last]`. Returns an empty string if the character sequence is not a valid collating element.

```
bool isctype(charT c, char_class_type f) const;
```

11 *Effects:* Determines if the character `c` is a member of the character classification represented by `f`.

12 *Returns:* Converts `f` into a value `m` of type `std::ctype_base::mask` in an unspecified manner, and returns `true` if `use_facet<ctype<charT>>(getloc()).is(c, m)` is `true`. Otherwise returns `true` if `f` bitwise or'ed with the result of calling `lookup_classname` with an iterator pair that designates the character sequence "w" is not equal to 0 and `c == '_'`, or if `f` bitwise or'ed with the result of calling `lookup_classname` with an iterator pair that designates the character sequence "blank" is not equal to 0 and `c` is one of an implementation-defined subset of the characters for which `isspace(c, getloc())` returns `true`, otherwise returns `false`.

```
int value(charT ch, int radix) const;
```

- 13 *Precondition:* The value of *radix* shall be 8, 10, or 16.
- 14 *Returns:* the value represented by the digit *ch* in base *radix* if the character *ch* is a valid digit in base *radix*; otherwise returns -1.
- ```
locale_type imbue(locale_type loc);
```
- 15     *Effects:* Imbues *this* with a copy of the locale *loc*. [Note: calling *imbue* with a different locale than the one currently in use invalidates all cached data held by *this*. — *end note*]
- 16     *Returns:* if no locale has been previously imbued then a copy of the global locale in effect at the time of construction of *this*, otherwise a copy of the last argument passed to *imbue*.
- 17     *Postcondition:* *getloc()* == *loc*.
- ```
locale_type getloc() const;
```
- 18 *Returns:* if no locale has been imbued then a copy of the global locale in effect at the time of construction of *this*, otherwise a copy of the last argument passed to *imbue*.

7.8 Class template basic_regex

[tr.re.regex]

- 1 For a char-like type *charT*, the class template *basic_regex* describes objects that represent a regular expression constructed from a sequence of *charTs*. In the rest of this clause, *charT* denotes such a given char-like type. Storage for the regular expression is allocated and freed as necessary by the member functions of class *basic_regex*.
- 2 Objects of type specialization of *basic_regex* are responsible for converting the sequence of *charT* objects to an internal representation. It is not specified what form this representation takes, nor how it is accessed by algorithms that operate on regular expressions. [Note: implementations will typically declare some function template as friends of *basic_regex* to achieve this — *end note*]
- 3 indexgrammar!regular expression The regular expression grammar recognized by class template *basic_regex* is described in clause 7.13.
- 4 The functions described in this clause report errors by throwing exceptions of type *regex_error*.

```
template <class charT,
          class traits = regex_traits<charT> >
class basic_regex
{
public:
    // types:
    typedef           charT           value_type;
    typedef           regex_constants::syntax_option_type flag_type;
    typedef typename traits::locale_type      locale_type;

    // constants:
    static const regex_constants::syntax_option_type icase
        = regex_constants::icase;
    static const regex_constants::syntax_option_type nosubs
        = regex_constants::nosubs;
    static const regex_constants::syntax_option_type optimize
```

```
= regex_constants::optimize;
static const regex_constants::syntax_option_type collate
= regex_constants::collate;
static const regex_constants::syntax_option_type ECMAScript
= regex_constants::ECMAScript;
// these flags are optional, if the functionality is supported
// then the flags shall take these names.
static const regex_constants::syntax_option_type basic
= regex_constants::basic;
static const regex_constants::syntax_option_type extended
= regex_constants::extended;
static const regex_constants::syntax_option_type awk
= regex_constants::awk;
static const regex_constants::syntax_option_type grep
= regex_constants::grep;
static const regex_constants::syntax_option_type egrep
= regex_constants::egrep;

// construct/copy/destroy:
basic_regex();
explicit basic_regex(const charT* p,
flag_type f = regex_constants::ECMAScript);
basic_regex(const charT* p, size_type len, flag_type f);
basic_regex(const basic_regex&);

template <class ST, class SA>
explicit basic_regex(const basic_string<charT, ST, SA>& p,
flag_type f = regex_constants::ECMAScript);
template <class InputIterator>
basic_regex(InputIterator first, inputIterator last,
flag_type f = regex_constants::ECMAScript);

~basic_regex();
basic_regex& operator=(const basic_regex&);
basic_regex& operator=(const charT* ptr);
template <class ST, class SA>
basic_regex& operator=(const basic_string<charT, ST, SA>& p);

// capacity:
bool empty() const;
unsigned mark_count() const;

//
// modifiers:
basic_regex& assign(const basic_regex& that);
basic_regex& assign(const charT* ptr,
flag_type f = regex_constants::ECMAScript);
basic_regex& assign(const charT* p, size_type len, flag_type f);
template <class string_traits, class A>
basic_regex& assign(
const basic_string<charT, string_traits, A>& s,
```

```

    flag_type f = regex_constants::ECMAScript);
template <class InputIterator>
basic_regex& assign(InputIterator first, InputIterator last,
                    flag_type f = regex_constants::ECMAScript);

// const operations:
flag_type flags() const;
// locale:
locale_type imbue(locale_type loc);
locale_type getloc() const;
// swap
void swap(basic_regex&) throw();
};

```

7.8.1 basic_regex constants

[tr.re.regex.const]

```

static const regex_constants::syntax_option_type icase
    = regex_constants::icase;
static const regex_constants::syntax_option_type nosubs
    = regex_constants::nosubs;
static const regex_constants::syntax_option_type optimize
    = regex_constants::optimize;
static const regex_constants::syntax_option_type collate
    = regex_constants::collate;
static const regex_constants::syntax_option_type ECMAScript
    = regex_constants::ECMAScript;
// these flags are optional, if the functionality is supported
// then the flags shall take these names.
static const regex_constants::syntax_option_type basic
    = regex_constants::basic;
static const regex_constants::syntax_option_type extended
    = regex_constants::extended;
static const regex_constants::syntax_option_type awk
    = regex_constants::awk;
static const regex_constants::syntax_option_type grep
    = regex_constants::grep;
static const regex_constants::syntax_option_type egrep
    = regex_constants::egrep;

```

- 1 The static constant members are provided as synonyms for the constants declared in namespace `regex_constants`; for each constant of type `syntax_option_type` declared in namespace `regex_constants` a constant with the same name, type and value shall be declared within the scope of `basic_regex`.

7.8.2 basic_regex constructors

[tr.re.regex.construct]

```
basic_regex();
```

- 1 *Effects:* Constructs an object of class `basic_regex`. The postconditions of this function are indicated in Table 19.

```
basic_regex(const charT* p, flag_type f = regex_constants::ECMAScript);
```

Table 19: `basic_regex()` effects

Element	Value
<code>empty()</code>	<code>true</code>

2 *Requires:* p shall not be a null pointer.

3 *Throws:* `regex_error` if p is not a valid regular expression.

4 *Effects:* Constructs an object of class `basic_regex`; the object's internal finite state machine is constructed from the regular expression contained in the array of `charT` of length `char_traits<charT>::length(p)` whose first element is designated by p , and interpreted according to the flags f . The postconditions of this function are indicated in Table 20.

Table 20: `basic_regex(const charT* p, flag_type f)` effects

Element	Value
<code>empty()</code>	<code>false</code>
<code>flags()</code>	f
<code>mark_count()</code>	The number of marked sub-expressions within the expression.

`basic_regex(const charT* p, size_type len, flag_type f);`

5 *Requires:* p shall not be a null pointer.

6 *Throws:* `regex_error` if p is not a valid regular expression.

7 *Effects:* Constructs an object of class `basic_regex`; the object's internal finite state machine is constructed from the regular expression contained in the sequence of characters $[p, p+len)$, and interpreted according the flags specified in f . The postconditions of this function are indicated in Table 21

Table 21: `basic_regex(const charT* p1, size_type len, flag_type f)` effects

Element	Value
<code>empty()</code>	<code>false</code>
<code>flags()</code>	f
<code>mark_count()</code>	The number of marked sub-expressions within the expression.

`basic_regex(const basic_regex& e);`

8 *Effects:* Constructs an object of class `basic_regex` as a copy of the object e . The postconditions of this function are indicated in Table 22

```
template <class ST, class SA>
basic_regex(const basic_string<charT, ST, SA>& s,
            flag_type f = regex_constants::ECMAScript);
```

Table 22: `basic_regex(const basic_regex& e)` effects

Element	Value
<code>empty()</code>	<code>e.empty()</code>
<code>flags()</code>	<code>e.flags()</code>
<code>mark_count()</code>	<code>e.mark_count()</code>

9 *Throws:* `regex_error` if `s` is not a valid regular expression.

10 *Effects:* Constructs an object of class `basic_regex`; the object's internal finite state machine is constructed from the regular expression contained in the string `s`, and interpreted according to the flags specified in `f`. The postconditions of this function are indicated in Table 23

Table 23: `basic_regex(const basic_string&)` effects

Element	Value
<code>empty()</code>	<code>false</code>
<code>flags()</code>	<code>f</code>
<code>mark_count()</code>	The number of marked sub-expressions within the expression.

```
template <class ForwardIterator>
basic_regex(ForwardIterator first, ForwardIterator last,
            flag_type f = regex_constants::ECMAScript);
```

11 *Throws:* `regex_error` if the sequence [`first, last`] is not a valid regular expression.

12 *Effects:* Constructs an object of class `basic_regex`; the object's internal finite state machine is constructed from the regular expression contained in the sequence of characters [`first, last`), and interpreted according to the flags specified in `f`. The postconditions of this function are indicated in Table 24.

Table 24: `basic_regex(ForwardIterator first, ForwardIterator last, flag_type f, const Allocator&)` effects

Element	Value
<code>empty()</code>	<code>false</code>
<code>flags()</code>	<code>f</code>
<code>mark_count()</code>	The number of marked sub-expressions within the expression.

```
basic_regex& operator=(const basic_regex& e);
```

13 *Effects:* Returns the result of `assign(e.str(), e.flags())`.

```
basic_regex& operator=(const charT* ptr);
```

14 *Requires:* `ptr` shall not be a null pointer.

15 *Effects:* Returns the result of `assign(ptr)`.

```
template <class ST, class SA>
basic_regex& operator=(const basic_string<charT, ST, SA>& p);
```

- 16 *Effects:* Returns the result of `assign(p)`.

7.8.3 basic_regex capacity

[tr.re.regex.cap]

```
bool empty() const;
```

- 1 *Effects:* Returns true if the object does not contain a valid regular expression, otherwise false.

```
unsigned mark_count() const;
```

- 2 *Effects:* Returns the number of marked sub-expressions within the regular expression.

7.8.4 basic_regex assign

[tr.re.regex.assign]

```
basic_regex& assign(const basic_regex& that);
```

- 1 *Effects:* Returns `assign(that.str(), that.flags())`.

```
basic_regex& assign(const charT* ptr,
                    flag_type f = regex_constants::ECMAScript);
```

- 2 *Effects:* Returns `assign(string_type(ptr), f)`.

```
basic_regex& assign(const charT* ptr, size_t len,
                    flag_type f = regex_constants::ECMAScript);
```

- 3 *Effects:* Returns `assign(string_type(ptr, len), f)`.

```
template <class string_traits, class A>
basic_regex& assign(const basic_string<charT, string_traits, A>& s,
                   flag_type f = regex_constants::ECMAScript);
```

- 4 *Throws:* `regex_error` if `s` is not a valid regular expression.

- 5 *Returns:* `*this`.

- 6 *Effects:* Assigns the regular expression contained in the string `s`, interpreted according the flags specified in `f`. The postconditions of this function are indicated in Table 25.

Table 25: `basic_regex& assign(const basic_string<charT, string_traits, A>& s, flag_type f)` effects

Element	Value
<code>empty()</code>	<code>false</code>
<code>flags()</code>	<code>f</code>
<code>mark_count()</code>	The number of marked sub-expressions within the expression.

```
template <class InputIterator>
basic_regex& assign(InputIterator first, InputIterator last,
                    flag_type f = regex_constants::ECMAScript);
```

7 *Requires:* The type InputIterator corresponds to the Input Iterator requirements (§24.1.1).

8 *Effects:* Returns `assign(string_type(first, last), f)`.

7.8.5 basic_regex constant operations

[tr.re.regex.operations]

```
flag_type flags() const;
```

1 *Effects:* Returns a copy of the regular expression syntax flags that were passed to the object's constructor, or the last call to `assign`.

7.8.6 basic_regex locale

[tr.re.regex.locale]

```
locale_type imbue(locale_type loc);
```

1 *Effects:* Returns the result of `traits_inst.imbue(loc)` where `traits_inst` is a (default initialized) instance of the template type argument `traits` stored within the object. Calls to `imbue` invalidate any currently contained regular expression.

2 *Postcondition:* `empty() == true`.

```
locale_type getloc() const;
```

3 *Effects:* Returns the result of `traits_inst.getloc()` where `traits_inst` is a (default initialized) instance of the template parameter `traits` stored within the object.

7.8.7 basic_regex swap

[tr.re.regex.swap]

```
void swap(basic_regex& e) throw();
```

1 *Effects:* Swaps the contents of the two regular expressions.

2 *Postcondition:* `*this` contains the regular expression that was in `e`, `e` contains the regular expression that was in `*this`.

3 *Complexity:* constant time.

7.8.8 basic_regex non-member functions

[tr.re.regex.nonmemb]

7.8.8.1 basic_regex non-member swap

[tr.re.regex.nmswap]

```
template <class charT, class traits>
void swap(basic_regex<charT, traits>& lhs,
          basic_regex<charT, traits>& rhs);
```

1 *Effects:* Calls `lhs.swap(rhs)`.

7.9 Class template `sub_match`**[tr.re.submatch]**

- 1 Class template `sub_match` denotes the sequence of characters matched by a particular marked sub-expression.

```
template <class BidirectionalIterator>
class sub_match
    : public std::pair<BidirectionalIterator, BidirectionalIterator>
{
public:
    typedef typename iterator_traits<BidirectionalIterator>::value_type
        value_type;
    typedef typename iterator_traits<BidirectionalIterator>::difference_type
        difference_type;
    typedef BidirectionalIterator
        iterator;

    bool matched;

    difference_type length() const;
    operator basic_string<value_type>() const;
    basic_string<value_type> str() const;

    int compare(const sub_match& s) const;
    int compare(const basic_string<value_type>& s) const;
    int compare(const value_type* s) const;
};
```

7.9.1 `sub_match` members**[tr.re.submatch.members]**

- 1 `difference_type length();`
Returns: (matched ? `distance(first, second)` : 0).
- 2 `operator basic_string<value_type>() const;`
Returns: (matched ? `basic_string<value_type>(first, second)` : `basic_string<value_type>()`).
- 3 `basic_string<value_type> str() const;`
Returns: (matched ? `basic_string<value_type>(first, second)` : `basic_string<value_type>()`).
- 4 `int compare(const sub_match& s) const;`
Returns: `str().compare(s.str())`.
- 5 `int compare(const basic_string<value_type>& s) const;`
Returns: `str().compare(s)`.
- `int compare(const value_type* s) const;`

6 *Returns:* str().compare(s).

7.9.2 sub_match non-member operators

[tr.re.submatch.op]

```
template <class BiIter>
bool operator==(const sub_match<BiIter>& lhs, const sub_match<BiIter>& rhs);
```

1 *Returns:* lhs.compare(rhs) == 0.

```
template <class BiIter>
bool operator!=(const sub_match<BiIter>& lhs, const sub_match<BiIter>& rhs);
```

2 *Returns:* lhs.compare(rhs) != 0.

```
template <class BiIter>
bool operator<(const sub_match<BiIter>& lhs, const sub_match<BiIter>& rhs);
```

3 *Returns:* lhs.compare(rhs) < 0.

```
template <class BiIter>
bool operator<=(const sub_match<BiIter>& lhs, const sub_match<BiIter>& rhs);
```

4 *Returns:* lhs.compare(rhs) <= 0.

```
template <class BiIter>
bool operator>=(const sub_match<BiIter>& lhs, const sub_match<BiIter>& rhs);
```

5 *Returns:* lhs.compare(rhs) >= 0.

```
template <class BiIter>
bool operator>(const sub_match<BiIter>& lhs, const sub_match<BiIter>& rhs);
```

6 *Returns:* lhs.compare(rhs) > 0.

```
template <class BiIter, class traits, class Allocator>
bool operator==(const basic_string<iterator_traits<BiIter>::value_type,
                  traits, Allocator>& lhs,
                  const sub_match<BiIter>& rhs);
```

7 *Returns:* lhs == rhs.str().

```
template <class BiIter, class traits, class Allocator>
bool operator!=(const basic_string<iterator_traits<BiIter>::value_type,
                  traits, Allocator>& lhs,
                  const sub_match<BiIter>& rhs);
```

8 *Returns:* lhs != rhs.str().

```
template <class BiIter, class traits, class Allocator>
bool operator<(const basic_string<iterator_traits<BiIter>::value_type,
                  traits, Allocator>& lhs,
                  const sub_match<BiIter>& rhs);
```

```
9     Returns: lhs < rhs.str().  
  
template <class BiIter, class traits, class Allocator>  
bool operator<>(const basic_string<iterator_traits<BiIter>::value_type,  
                     traits, Allocator>& lhs,  
                     const sub_match<BiIter>& rhs);  
  
10    Returns: lhs > rhs.str().  
  
template <class BiIter, class traits, class Allocator>  
bool operator>=(const basic_string<iterator_traits<BiIter>::value_type,  
                   traits, Allocator>& lhs,  
                   const sub_match<BiIter>& rhs);  
  
11    Returns: lhs >= rhs.str().  
  
template <class BiIter, class traits, class Allocator>  
bool operator<=(const basic_string<iterator_traits<BiIter>::value_type,  
                   traits, Allocator>& lhs,  
                   const sub_match<BiIter>& rhs);  
  
12    Returns: lhs <= rhs.str().  
  
template <class BiIter, class traits, class Allocator>  
bool operator==(const sub_match<BiIter>& lhs,  
                  const basic_string<iterator_traits<BiIter>::value_type,  
                  traits, Allocator>& rhs);  
  
13    Returns: lhs.str() == rhs.  
  
template <class BiIter, class traits, class Allocator>  
bool operator!=(const sub_match<BiIter>& lhs,  
                  const basic_string<iterator_traits<BiIter>::value_type,  
                  traits, Allocator>& rhs);  
  
14    Returns: lhs.str() != rhs.  
  
template <class BiIter, class traits, class Allocator>  
bool operator<<(const sub_match<BiIter>& lhs,  
                  const basic_string<iterator_traits<BiIter>::value_type,  
                  traits, Allocator>& rhs);  
  
15    Returns: lhs.str() < rhs.  
  
template <class BiIter, class traits, class Allocator>  
bool operator>(const sub_match<BiIter>& lhs,  
                 const basic_string<iterator_traits<BiIter>::value_type,  
                 traits, Allocator>& rhs);  
  
16    Returns: lhs.str() > rhs.  
  
template <class BiIter, class traits, class Allocator>  
bool operator>=(const sub_match<BiIter>& lhs,  
                  const basic_string<iterator_traits<BiIter>::value_type,
```

```

                                traits, Allocator>& rhs);

17   Returns: lhs.str() >= rhs.

template <class BiIter, class traits, class Allocator>
bool operator<=(const sub_match<BiIter>& lhs,
                  const basic_string<iterator_traits<BiIter>::value_type,
                  traits, Allocator>& rhs);

18   Returns: lhs.str() <= rhs.

template <class BiIter>
bool operator==(typename iterator_traits<BiIter>::value_type const* lhs,
                  const sub_match<BiIter>& rhs);

19   Returns: lhs == rhs.str().

template <class BiIter>
bool operator!=(typename iterator_traits<BiIter>::value_type const* lhs,
                  const sub_match<BiIter>& rhs);

20   Returns: lhs != rhs.str().

template <class BiIter>
bool operator<(typename iterator_traits<BiIter>::value_type const* lhs,
                  const sub_match<BiIter>& rhs);

21   Returns: lhs < rhs.str().

template <class BiIter>
bool operator>(typename iterator_traits<BiIter>::value_type const* lhs,
                  const sub_match<BiIter>& rhs);

22   Returns: lhs > rhs.str().

template <class BiIter>
bool operator>=(typename iterator_traits<BiIter>::value_type const* lhs,
                  const sub_match<BiIter>& rhs);

23   Returns: lhs >= rhs.str().

template <class BiIter>
bool operator<=(typename iterator_traits<BiIter>::value_type const* lhs,
                  const sub_match<BiIter>& rhs);

24   Returns: lhs <= rhs.str().

template <class BiIter>
bool operator==(const sub_match<BiIter>& lhs,
                  typename iterator_traits<BiIter>::value_type const* rhs);

25   Returns: lhs.str() == rhs.

template <class BiIter>
bool operator!=(const sub_match<BiIter>& lhs,

```

```
        typename iterator_traits<BiIter>::value_type const* rhs);  
26     Returns: lhs.str() != rhs.  
  
template <class BiIter>  
bool operator<(const sub_match<BiIter>& lhs,  
                  typename iterator_traits<BiIter>::value_type const* rhs);  
27     Returns: lhs.str() < rhs.  
  
template <class BiIter>  
bool operator>(const sub_match<BiIter>& lhs,  
                 typename iterator_traits<BiIter>::value_type const* rhs);  
28     Returns: lhs.str() > rhs.  
  
template <class BiIter>  
bool operator>=(const sub_match<BiIter>& lhs,  
                  typename iterator_traits<BiIter>::value_type const* rhs);  
29     Returns: lhs.str() >= rhs.  
  
template <class BiIter>  
bool operator<=(const sub_match<BiIter>& lhs,  
                  typename iterator_traits<BiIter>::value_type const* rhs);  
30     Returns: lhs.str() <= rhs.  
  
template <class BiIter>  
bool operator==(typename iterator_traits<BiIter>::value_type const& lhs,  
                  const sub_match<BiIter>& rhs);  
31     Returns: lhs == rhs.str().  
  
template <class BiIter>  
bool operator!=(typename iterator_traits<BiIter>::value_type const& lhs,  
                  const sub_match<BiIter>& rhs);  
32     Returns: lhs != rhs.str().  
  
template <class BiIter>  
bool operator<(typename iterator_traits<BiIter>::value_type const& lhs,  
                  const sub_match<BiIter>& rhs);  
33     Returns: lhs < rhs.str().  
  
template <class BiIter>  
bool operator>(typename iterator_traits<BiIter>::value_type const& lhs,  
                  const sub_match<BiIter>& rhs);  
34     Returns: lhs > rhs.str().  
  
template <class BiIter>  
bool operator>=(typename iterator_traits<BiIter>::value_type const& lhs,  
                  const sub_match<BiIter>& rhs);
```

```

35     Returns: lhs >= rhs.str().

template <class BiIter>
bool operator<=(typename iterator_traits<BiIter>::value_type const& lhs,
                 const sub_match<BiIter>& rhs);

36     Returns: lhs <= rhs.str().

template <class BiIter>
bool operator==(const sub_match<BiIter>& lhs,
                  typename iterator_traits<BiIter>::value_type const& rhs);

37     Returns: lhs.str() == rhs.

template <class BiIter>
bool operator!=(const sub_match<BiIter>& lhs,
                  typename iterator_traits<BiIter>::value_type const& rhs);

38     Returns: lhs.str() != rhs.

template <class BiIter>
bool operator<(const sub_match<BiIter>& lhs,
                  typename iterator_traits<BiIter>::value_type const& rhs);

39     Returns: lhs.str() < rhs.

template <class BiIter>
bool operator>(const sub_match<BiIter>& lhs,
                  typename iterator_traits<BiIter>::value_type const& rhs);

40     Returns: lhs.str() > rhs.

template <class BiIter>
bool operator>=(const sub_match<BiIter>& lhs,
                  typename iterator_traits<BiIter>::value_type const& rhs);

41     Returns: lhs.str() >= rhs.

template <class BiIter>
bool operator<=(const sub_match<BiIter>& lhs,
                  typename iterator_traits<BiIter>::value_type const& rhs);

42     Returns: lhs.str() <= rhs.

template <class charT, class traits, class BiIter>
basic_ostream<charT, traits>&
operator<<(basic_ostream<charT, traits>& os, const sub_match<BiIter>& m);

43     Returns: (os << m.str());

```

7.10 Class template `match_results`

[[tr.re.results](#)]

- 1 Class template `match_results` denotes a collection of character sequences representing the result of a regular expres-

sion match. Storage for the collection is allocated and freed as necessary by the member functions of class `match_results`.

- 2 The class template `match_results` satisfies the requirements of a Sequence, as specified in [lib.sequence.reqmts], except that only operations defined for const-qualified Sequences are supported.
- 3 The `sub_match` object stored at index 0 represents sub-expression 0; that is to say the whole match. In this case the `sub_match` member `matched` is always true, unless a partial match was obtained as a result of the flag `regex_constants::partial_match` being passed to a regular expression algorithm, in which case member `matched` is false, and the members `first` and `second` represent the character range that formed the partial match. The `sub_match` object stored at index `n` denotes what matched the marked sub-expression `n` within the matched expression. If the sub-expression `n` participated in a regular expression match then the `sub_match` member `matched` evaluates to true, and members `first` and `second` denote the range of characters [`first`, `second`) which formed that match. Otherwise `matched` is false, and members `first` and `second` point to the end of the sequence that was searched. [Note: The `sub_match` objects representing different sub-expressions that did not participate in a regular expression match need not be distinct.—end note]

```

template <class BidirectionalIterator,
          class Allocator
                  = allocator<sub_match<BidirectionalIterator> >
class match_results
{
public:
    typedef sub_match<BidirectionalIterator>      value_type;
    typedef typename allocator::const_reference  const_reference;
    typedef const_reference                      reference;
    typedef implementation-defined            const_iterator;
    typedef const_iterator                     iterator;
    typedef typename iterator_traits<BidirectionalIterator>::difference_type
                                              difference_type;
    typedef typename Allocator::size_type       size_type;
    typedef Allocator                         allocator_type;
    typedef typename iterator_traits<BidirectionalIterator>::value_type
                                              char_type;
    typedef basic_string<char_type>           string_type;

// construct/copy/destroy:
explicit match_results(const Allocator& a = Allocator());
match_results(const match_results& m);
match_results& operator=(const match_results& m);
~match_results();

// size:
size_type size() const;
size_type max_size() const;
bool empty() const;
// element access:
difference_type length(size_type sub = 0) const;
difference_type position(size_type sub = 0) const;
string_type str(size_type sub = 0) const;

```

```

const_reference operator[](size_type n) const;

const_reference prefix() const;

const_reference suffix() const;
const_iterator begin() const;
const_iterator end() const;
// format:
template <class OutputIterator>
OutputIterator format(OutputIterator out,
                      const string_type& fmt,
                      regex_constants::match_flag_type flags
                      = regex_constants::format_default) const;
string_type format(const string_type& fmt,
                   regex_constants::match_flag_type flags
                   = regex_constants::format_default) const;

allocator_type get_allocator() const;
void swap(match_results& that);
};

```

7.10.1 `match_results` constructors

[tr.re.results.const]

- 1 In all `match_results` constructors, a copy of the `Allocator` argument is used for any memory allocation performed by the constructor or member functions during the lifetime of the object.

```
match_results(const Allocator& a = Allocator());
```

- 2 *Effects:* Constructs an object of class `match_results`. The postconditions of this function are indicated in Table 26

Table 26: `match_results(const Allocator&)` effects

Element	Value
<code>empty()</code>	<code>true</code>
<code>size()</code>	<code>0</code>
<code>str()</code>	<code>basic_string<charT>()</code>

```
match_results(const match_results& m);
```

- 3 *Effects:* Constructs an object of class `match_results`, as a copy of `m`.

```
match_results& operator=(const match_results& m);
```

- 4 *Effects:* Assigns `m` to `*this`. The postconditions of this function are indicated in Table 27

7.10.2 `match_results size`

[tr.re.results.size]

```
size_type size() const;
```

Table 27: `match_results` assignment operator effects

Element	Value
<code>empty()</code>	<code>m.empty()</code>
<code>size()</code>	<code>m.size()</code>
<code>str(n)</code>	<code>m.str(n)</code> for all integers $n < m.size$
<code>prefix()</code>	<code>m.prefix()</code>
<code>suffix()</code>	<code>m.suffix()</code>
<code>(*this)[n]</code>	<code>m[n]</code> for all integers $n < m.size$
<code>length(n)</code>	<code>m.length(n)</code> for all integers $n < m.size$
<code>position(n)</code>	<code>m.position(n)</code> for all integers $n < m.size$

1 >Returns: One plus the number of marked sub-expressions in the regular expression that was matched.

```
size_type max_size() const;
```

2 >Returns: The maximum number of `sub_match` elements that can be stored in `*this`.

```
bool empty() const;
```

3 >Returns: `size() == 0`.

7.10.3 `match_results` element access

[tr.re.results.acc]

```
difference_type length(size_type sub = 0) const;
```

1 >Returns: `(*this)[sub].length()`.

```
difference_type position(size_type sub = 0) const;
```

2 >Returns: `std::distance(prefix().first, (*this)[sub].first)`.

```
string_type str(size_type sub = 0) const;
```

3 >Returns: `string_type((*this)[sub])`.

```
const_reference operator[](size_type n) const;
```

4 >Returns: A reference to the `sub_match` object representing the character sequence that matched marked sub-expression `n`. If `n == 0` then returns a reference to a `sub_match` object representing the character sequence that matched the whole regular expression. If `n >= size()` then returns a `sub_match` object representing an unmatched sub-expression.

```
const_reference prefix() const;
```

5 >Returns: A reference to the `sub_match` object representing the character sequence from the start of the string being matched/searched, to the start of the match found.

```
const_reference suffix() const;
```

6 *Returns:* A reference to the `sub_match` object representing the character sequence from the end of the match found to the end of the string being matched/searched.

```
const_iterator begin() const;
```

7 *Returns:* A starting iterator that enumerates over all the marked sub-expression matches stored in `*this`.

```
const_iterator end() const;
```

8 *Returns:* A terminating iterator that enumerates over all the marked sub-expression matches stored in `*this`.

7.10.4 `match_results` reformatting

[tr.re.results.reform]

```
OutputIterator format(OutputIterator out,
                      const string_type& fmt,
                      regex_constants::match_flag_type flags
                        = regex_constants::format_default);
```

1 *Requires:* The type `OutputIterator` conforms to the Output Iterator requirements [24.1.2].

2 *Effects:* Copies the character sequence [`fmt.begin()`, `fmt.end()`] to `OutputIterator out`. For each format specifier or escape sequence in `fmt`, replace that sequence with either the character(s) it represents, or the sequence of characters within `*this` to which it refers. The bitmasks specified in `flags` determines what format specifiers or escape sequences are recognized, by default this is the format used by ECMA-262 [7], part 15.4.11 `String.prototype.replace`.

3 *Returns:* `out`.

```
string_type format(const string_type& fmt,
                   regex_constants::match_flag_type flags
                     = regex_constants::format_default);
```

4 *Effects:* Returns a copy of the string `fmt`. For each format specifier or escape sequence in `fmt`, replace that sequence with either the character(s) it represents, or the sequence of characters within `*this` to which it refers. The bitmasks specified in `flags` determines what format specifiers or escape sequences are recognized, by default this is the format used by ECMA-262 [7], part 15.4.11, `String.prototype.replace`.

7.10.5 `match_results` allocator

[tr.re.results.all]

```
allocator_type get_allocator() const;
```

1 *Effects:* Returns a copy of the Allocator that was passed to the object's constructor.

7.10.6 `match_results` swap

[tr.re.results.swap]

```
void swap(match_results& that);
```

1 *Effects:* Swaps the contents of the two sequences.

- 2 *Postcondition:* `*this` contains the sequence of matched sub-expressions that were in `that`, `that` contains the sequence of matched sub-expressions that were in `*this`.
- 3 *Complexity:* constant time.

7.11 Regular expression algorithms

[tr.re.alg]

7.11.1 exceptions

[tr.re.except]

- 1 The algorithms described in this subclause may throw an exception of type `regex_error`. If such an exception `e` is thrown, `e.code()` shall return either `regex_constants::error_complexity` or `regex_constants::error_stack`.

7.11.2 regex_match

[tr.re.alg.match]

```
template <class BidirectionalIterator, class Allocator,
          class charT, class traits>
bool regex_match(BidirectionalIterator first, BidirectionalIterator last,
                 match_results<BidirectionalIterator, Allocator>& m,
                 const basic_regex<charT, traits>& e,
                 regex_constants::match_flag_type flags
                 = regex_constants::match_default);
```

- 1 *Requires:* Type `BidirectionalIterator` satisfies the requirements of a Bidirectional Iterator (§24.1.4).

- 2 *Effects:* Determines whether there is an exact match between the regular expression `e`, and all of the character sequence [`first`, `last`), where the parameter `flags` is used to control how the expression is matched against the character sequence. Returns `true` if such a match exists, `false` otherwise.

- 3 *Postconditions:* If the function returns `false`, then the effect on parameter `m` is unspecified, otherwise the effects on parameter `m` are given in table 28.

```
template <class BidirectionalIterator,
          class charT, class traits>
bool regex_match(BidirectionalIterator first, BidirectionalIterator last,
                 const basic_regex<charT, traits>& e,
                 regex_constants::match_flag_type flags
                 = regex_constants::match_default);
```

- 4 *Effects:* Behaves “as if” by constructing an instance of `match_results< BidirectionalIterator >` what , and then returning the result of `regex_match(first, last, what, e, flags)`.

```
template <class charT, class Allocator, class traits>
bool regex_match(const charT* str,
                 match_results<const charT*, Allocator>& m,
                 const basic_regex<charT, traits>& e,
                 regex_constants::match_flag_type flags
                 = regex_constants::match_default);
```

- 5 *Returns:* `regex_match(str,`
`str + char_traits<charT>::length(str), m, e, flags)`.

Table 28: Effects of `regex_match` algorithm

Element	Value
<code>m.size()</code>	<code>1 + e.mark_count()</code>
<code>m.empty()</code>	<code>false</code>
<code>m.prefix().first</code>	<code>first</code>
<code>m.prefix().last</code>	<code>first</code>
<code>m.prefix().matched</code>	<code>false</code>
<code>m.suffix().first</code>	<code>last</code>
<code>m.suffix().last</code>	<code>last</code>
<code>m.suffix().matched</code>	<code>false</code>
<code>m[0].first</code>	<code>first</code>
<code>m[0].second</code>	<code>last</code>
<code>m[0].matched</code>	true if a full match was found, and <code>false</code> if it was a partial match (found as a result of the <code>regex_constants::match_partial</code> flag being set).
<code>m[n].first</code>	For all integers $n < m.size()$, the start of the sequence that matched sub-expression n . Alternatively, if sub-expression n did not participate in the match, then <code>last</code> .
<code>m[n].second</code>	For all integers $n < m.size()$, the end of the sequence that matched sub-expression n . Alternatively, if sub-expression n did not participate in the match, then <code>last</code> .
<code>m[n].matched</code>	For all integers $n < m.size()$, <code>true</code> if sub-expression n participated in the match, <code>false</code> otherwise.

```

template <class ST, class SA, class Allocator,
          class charT, class traits>
bool regex_match(const basic_string<charT, ST, SA>& s,
                  match_results<typename basic_string<charT, ST, SA>::const_iterator,
                               Allocator>& m,
                  const basic_regex<charT, traits>& e,
                  regex_constants::match_flag_type flags
                  = regex_constants::match_default);

6   Returns: regex_match(s.begin(), s.end(), m, e, flags).

template <class charT, class traits>
bool regex_match(const charT* str,
                  const basic_regex<charT, traits>& e,
                  regex_constants::match_flag_type flags
                  = regex_constants::match_default);

7   Returns: regex_match(str,
                         str + char_traits<charT>::length(str), e, flags)

template <class ST, class SA, class charT, class traits>
bool regex_match(const basic_string<charT, ST, SA>& s,
                  const basic_regex<charT, traits>& e,
                  regex_constants::match_flag_type flags
                  = regex_constants::match_default);

8   Returns: regex_match(s.begin(), s.end(), e, flags).

```

7.11.3 regex_search

[tr.re.alg.search]

```

template <class BidirectionalIterator, class Allocator,
          class charT, class traits>
bool regex_search(BidirectionalIterator first, BidirectionalIterator last,
                  match_results<BidirectionalIterator, Allocator>& m,
                  const basic_regex<charT, traits>& e,
                  regex_constants::match_flag_type flags
                  = regex_constants::match_default);

```

- 1 *Requires:* Type BidirectionalIterator meets the requirements of a Bidirectional Iterator (24.1.4).
- 2 *Effects:* Determines whether there is some sub-sequence within [first, last) that matches the regular expression e, parameter flags is used to control how the expression is matched against the character sequence. Returns true if such a sequence exists, false otherwise.
- 3 *Postconditions:* If the function returns false, then the effect on parameter m is unspecified, otherwise the effects on parameter m are given in table 29.

```

template <class charT, class Allocator, class traits>
bool regex_search(const charT* str, match_results<const charT*, Allocator>& m,
                  const basic_regex<charT, traits>& e,
                  regex_constants::match_flag_type flags

```

Table 29: Effects of `regex_search` algorithm

Element	Value
<code>m.size()</code>	<code>1 + e.mark_count()</code>
<code>m.empty()</code>	<code>false</code>
<code>m.prefix().first</code>	<code>first</code>
<code>m.prefix().last</code>	<code>m[0].first</code>
<code>m.prefix().matched</code>	<code>m.prefix().first != m.prefix().second</code>
<code>m.suffix().first</code>	<code>m[0].second</code>
<code>m.suffix().last</code>	<code>last</code>
<code>m.suffix().matched</code>	<code>m.suffix().first != m.suffix().second</code>
<code>m[0].first</code>	The start of the sequence of characters that matched the regular expression
<code>m[0].second</code>	The end of the sequence of characters that matched the regular expression
<code>m[0].matched</code>	true if a full match was found, and false if it was a partial match (found as a result of the <code>regex_constants::match_partial</code> flag being set).
<code>m[n].first</code>	For all integers $n < m.size()$, the start of the sequence that matched sub-expression n . Alternatively, if sub-expression n did not participate in the match, then <code>last</code> .
<code>m[n].second</code>	For all integers $n < m.size()$, the end of the sequence that matched sub-expression n . Alternatively, if sub-expression n did not participate in the match, then <code>last</code> .
<code>m[n].matched</code>	For all integers $n < m.size()$, true if sub-expression n participated in the match, false otherwise.

```

        = regex_constants::match_default);

4   Returns: The result of regex_search(str,
        str + char_traits<charT>::length(str), m, e, flags).

template <class ST, class SA, class Allocator,
          class charT, class traits>
bool regex_search(const basic_string<charT, ST, SA>& s,
                  match_results<typename basic_string<charT, ST, SA>::const_iterator,
                               Allocator>& m,
                  const basic_regex<charT, traits>& e,
                  regex_constants::match_flag_type flags
                  = regex_constants::match_default);

5   Returns: The result of regex_search(s.begin(), s.end(), m, e, flags).

template <class iterator, class charT, class traits>
bool regex_search(iterator first, iterator last,
                  const basic_regex<charT, traits>& e,
                  regex_constants::match_flag_type flags
                  = regex_constants::match_default);

6   Effects: Behaves “as if” by constructing an object what of type match_results<BidirectionalIterator>
and then returning the result of regex_search(first, last, what, e, flags).

template <class charT, class traits>
bool regex_search(const charT* str
                  const basic_regex<charT, traits>& e,
                  regex_constants::match_flag_type flags
                  = regex_constants::match_default);

7   Returns: regex_search(str, str + char_traits<charT>::length(str),
        e, flags)

template <class ST, class SA,
          class charT, class traits>
bool regex_search(const basic_string<charT, ST, SA>& s,
                  const basic_regex<charT, traits>& e,
                  regex_constants::match_flag_type flags
                  = regex_constants::match_default);

8   Returns: regex_search(s.begin(), s.end(), e, flags).

```

7.11.4 regex_replace

[tr.re.alg.replace]

```

template <class OutputIterator, class BidirectionalIterator,
          class traits, class charT>
OutputIterator
regex_replace(OutputIterator out,
              BidirectionalIterator first,
              BidirectionalIterator last,

```

```

    const basic_regex<charT, traits>& e,
    const basic_string<charT>& fmt,
    regex_constants::match_flag_type flags
      = regex_constants::match_default);

```

- 1 *Effects:* Constructs a `regex_iterator` object `i` as if by `regex_iterator<BidirectionalIterator, charT, traits> i(first, last, e, flags)`, and uses `i` to enumerate through all of the matches `m` of type `match_results<BidirectionalIterator>` that occur within the sequence `[first, last]`. If no such matches are found and `!(flags & regex_constants::format_no_copy)` then calls `std::copy(first, last, out)`. Otherwise, for each match found, if `!(flags & regex_constants::format_no_copy)` calls `std::copy(m.prefix().first, m.prefix().second, out)`, and then calls `m.format(out, fmt, flags)`. Finally, if `!(flags & regex_constants::format_no_copy)` calls `std::copy(last_m.suffix().first, last_m.suffix().second, out)` where `last_m` is a copy of the last match found. If `flags & regex_constants::format_first_only` is non-zero then only the first match found is replaced.

- 2 *Returns:* `out`.

```

template <class traits, class charT>
basic_string<charT>
regex_replace(const basic_string<charT>& s,
              const basic_regex<charT, traits>& e,
              const basic_string<charT>& fmt,
              regex_constants::match_flag_type flags
                = regex_constants::match_default);

```

- 3 *Effects:* Constructs an empty string result of type `basic_string<charT>`, calls `regex_replace(back_inserter(result), s.begin(), s.end(), e, fmt, flags)`, and then returns `result`.

7.12 Regular expression Iterators

[tr.re.iterator]

7.12.1 Class template `regex_iterator`

[tr.re.register]

- 1 The class template `regex_iterator` is an iterator adapter. It represents a new view of an existing iterator sequence, by enumerating all the occurrences of a regular expression within that sequence. A `regex_iterator` uses `regex_search` to find successive regular expression matches within the sequence from which it was constructed. After the iterator is constructed, and every time `operator++` is used, the iterator finds and stores a value of `match_results<BidirectionalIterator>`. If the end of the sequence is reached (`regex_search` returns `false`), the iterator becomes equal to the end-of-sequence iterator value. The default constructor constructs an end-of-sequence iterator object, which is the only legitimate iterator to be used for the end condition. The result of `operator*` on an end-of-sequence iterator is not defined. For any other iterator value a `const match_results<BidirectionalIterator>&` is returned. The result of `operator->` on an end-of-sequence iterator is not defined. For any other iterator value a `const match_results<BidirectionalIterator>*` is returned. It is impossible to store things into `regex_iterators`. Two end-of-sequence iterators are always equal. An end-of-sequence iterator is not equal to a non-end-of-sequence iterator. Two non-end-of-sequence iterators are equal when they are constructed from the same arguments.

```

template <class BidirectionalIterator,
         class charT = iterator_traits<BidirectionalIterator>::value_type,
         class traits = regex_traits<charT> >
class regex_iterator

```

```

{
public:
    typedef basic_regex<charT, traits>           regex_type;
    typedef match_results<BidirectionalIterator>   value_type;
    typedef typename ptrdiff_t                      difference_type;
    typedef const value_type*                      pointer;
    typedef const value_type&                     reference;
    typedef std::forward_iterator_tag             iterator_category;

    regex_iterator();
    regex_iterator(BidirectionalIterator a,
                  BidirectionalIterator b,
                  const regex_type& re,
                  regex_constants::match_flag_type m
                  = regex_constants::match_default);
    regex_iterator(const regex_iterator&);
    regex_iterator& operator=(const regex_iterator&);
    bool operator==(const regex_iterator&);
    bool operator!=(const regex_iterator&);
    const value_type& operator*();
    const value_type* operator->();
    regex_iterator& operator++();
    regex_iterator operator++(int);

private:
    // these members are shown for exposition only:
    BidirectionalIterator          begin,
                                   end;
    const regex_type*              pregex;
    regex_constants::match_flag_type flags;
    match_results<BidirectionalIterator> match;
};


```

- 2 A `regex_iterator` object that is not an end-of-sequence iterator holds a *zero-length match* if `match[0].matched == true` and `match[0].first == match[0].second`. [Note: this occurs when the part of the regular expression that matched consists only of an assertion (such as '^', '\$', '\b', '\B'). —end note]

7.12.1.1 `regex_iterator` constructors

[tr.re.register.cnstr]

```
regex_iterator();
```

- 1 *Effects:* Constructs an end-of-sequence iterator.

```
regex_iterator(BidirectionalIterator a, BidirectionalIterator b,
              const regex_type& re,
              regex_constants::match_flag_type m
              = regex_constants::match_default);
```

- 2 *Effects:* Initializes `begin` and `end` to point to the beginning and the end of the target sequence, sets `pregex` to `&re`, sets `flags` to `f`, then calls `regex_search(begin, end, match, *pregex, flags)`. If this call returns `false` the constructor sets `*this` to the end-of-sequence iterator.

3 *Postconditions:* `*this == that.`

7.12.1.2 regex_iterator comparisons

[tr.re.register.comp]

```
bool operator==(const regex_iterator& right);
```

1 *Returns:* true if `*this` and `right` are both end-of-sequence iterators or if `begin == right.begin, end == right.end, pregex == right.pregex, flags == right.flags, and match[0] == right.match[0]`, otherwise false.

```
bool operator!=(const regex_iterator& right);
```

2 *Effects:* Returns `!(*this == right)`.

7.12.1.3 regex_iterator dereference

[tr.re.register.deref]

```
const value_type& operator*();
```

1 *Returns:* `match`.

```
const value_type* operator->();
```

2 *Returns:* `&match`.

7.12.1.4 regex_iterator increment

[tr.re.register.incr]

```
regex_iterator& operator++();
```

1 *Effects:* Constructs a local variable `start` of type `BidirectionalIterator` and initializes it with the value of `match[0].second`.

2 If the iterator holds a zero-length match and `start == end` the operator sets `*this` to the end-of-sequence iterator and returns `*this`.

3 Otherwise, if the iterator holds a zero-length match the operator calls `regex_search(start, end, match, *pregex, flags | regex_constants::match_not_null | regex_constants::match_continuous)`. If the call returns `true` the operator returns `*this`. Otherwise the operator increments `start` and continues as if the most recent match was not a zero-length match.

4 If the most recent match was not a zero-length match, the operator sets `flags` to `flags | regex_constants::match_prev_avail` and calls `regex_search(start, end, match, *pregex, flags)`. If the call returns `false` the iterator sets `*this` to the end-of-sequence iterator. The iterator then returns `*this`.

5 In all cases in which the call to `regex_search` returns `true`, `match.prefix().first` shall be equal to the previous value of `match[0].second`, and for each index `i` in the half-open range `[0, match.size())` for which `match[i].matched` is `true`, `match[i].position()` shall return `distance(begin, match[i].first)`.

6 *[Note:* this means that `match[i].position()` gives the offset from the beginning of the target sequence, which is often not the same as the offset from the sequence passed in the call to `regex_search`. —end note]

- 7 It is unspecified how the implementation makes these adjustments.
- 8 [Note: this means that a compiler may call an implementation-specific search function, in which case a user-defined specialization of `regex_search` will not be called. —end note]

```
    regex_iterator operator++(int);
```

- 9 *Effects:*

```
    regex_iterator tmp = *this;
    ++(*this);
    return tmp;
```

7.12.2 Class template `regex_token_iterator`

[tr.re.tokiter]

- 1 The class template `regex_token_iterator` is an iterator adapter; that is to say it represents a new view of an existing iterator sequence, by enumerating all the occurrences of a regular expression within that sequence, and presenting one or more sub-expressions for each match found. Each position enumerated by the iterator is a `sub_match` class template instance that represents what matched a particular sub-expression within the regular expression.
- 2 When class `regex_token_iterator` is used to enumerate a single sub-expression with index -1 the iterator performs field splitting: that is to say it enumerates one sub-expression for each section of the character container sequence that does not match the regular expression specified.
- 3 After it is constructed, the iterator finds and stores a value `match_results<BidirectionalIterator>` `position` and sets the internal count `N` to zero. It also maintains a sequence `subs` which contains a list of the sub-expressions which will be enumerated. Every time `operator++` is used the count `N` is incremented; if `N` exceeds or equals `subs.size()`, then the iterator increments member `position` and sets count `N` to zero.
- 4 If the end of sequence is reached (`position` is equal to the end of sequence iterator), the iterator becomes equal to the end-of-sequence iterator value, unless the sub-expression being enumerated has index -1, in which case the iterator enumerates one last sub-expression that contains all the characters from the end of the last regular expression match to the end of the input sequence being enumerated, provided that this would not be an empty sub-expression.
- 5 The default constructor constructs an end-of-sequence iterator object, which is the only legitimate iterator to be used for the end condition. The result of `operator*` on an end-of-sequence iterator is not defined. For any other iterator value a `const sub_match<BidirectionalIterator>&` is returned. The result of `operator->` on an end-of-sequence iterator is not defined. For any other iterator value a `const sub_match<BidirectionalIterator>*` is returned.
- 6 It is impossible to store things into `regex_iterators`. Two end-of-sequence iterators are always equal. An end-of-sequence iterator is not equal to a non-end-of-sequence iterator. Two non-end-of-sequence iterators are equal when they are constructed from the same arguments.

```
template <class BidirectionalIterator,
          class charT = iterator_traits<BidirectionalIterator>::value_type,
          class traits = regex_traits<charT> >
class regex_token_iterator
{
public:
    typedef basic_regex<charT, traits>           regex_type;
    typedef sub_match<BidirectionalIterator>        value_type;
```

```

typedef ptrdiff_t           difference_type;
typedef const value_type*   pointer;
typedef const value_type&  reference;
typedef std::forward_iterator_tag iterator_category;

regex_token_iterator();
regex_token_iterator(BidirectionalIterator a, BidirectionalIterator b,
                    const regex_type& re,
                    int submatch = 0, regex_constants::match_flag_type m
                    = regex_constants::match_default);
regex_token_iterator(BidirectionalIterator a, BidirectionalIterator b,
                    const regex_type& re,
                    const std::vector<int>& submatches,
                    regex_constants::match_flag_type m
                    = regex_constants::match_default);
template <std::size_t N>
regex_token_iterator(BidirectionalIterator a, BidirectionalIterator b,
                    const regex_type& re,
                    const int (&submatches)[N],
                    regex_constants::match_flag_type m
                    = regex_constants::match_default);
regex_token_iterator(const regex_token_iterator&);
regex_token_iterator& operator=(const regex_token_iterator&);
bool operator==(const regex_token_iterator&);
bool operator!=(const regex_token_iterator&);
const value_type& operator*();
const value_type* operator->();
regex_token_iterator& operator++();
regex_token_iterator operator++(int);
private:          // data members for exposition only:
typedef regex_iterator<BidirectionalIterator, charT, traits> position_iterator;
position_iterator position;
const value_type *result;
value_type suffix;
std::size_t N;
std::vector<int> subs;
};

```

- 7 A *suffix iterator* points to a final sequence of characters at the end of the target sequence. In a suffix iterator the member `result` holds a pointer to the data member `suffix`, the value of the member `suffix.match` is true, `suffix.first` points to the beginning of the final sequence, and `suffix.second` points to the end of the final sequence.
- 8 [Note: for a suffix iterator, data member `suffix.first` is the same as the end of the last match found, and `suffix.second` is the same as the end of the target sequence — *end note*].
- 9 The *current match* is `(*position).prefix()` if `subs[N] == -1`, or `(*position)[subs[N]]` for any other value of `subs[N]`.

7.12.2.1 regex_token_iterator constructors

[tr.re.tokiter.cnstr]

```
regex_token_iterator();
```

1 *Effects:* Constructs the end-of-sequence iterator.

```
regex_token_iterator(BidirectionalIterator a, BidirectionalIterator b,
                    const regex_type& re,
                    int submatch = 0, regex_constants::match_flag_type m
                    = regex_constants::match_default);

regex_token_iterator(BidirectionalIterator a, BidirectionalIterator b,
                    const regex_type& re,
                    const std::vector<int>& submatches,
                    regex_constants::match_flag_type m
                    = regex_constants::match_default);

template <std::size_t N>
regex_token_iterator(BidirectionalIterator a, BidirectionalIterator b,
                    const regex_type& re,
                    const int (&submatches)[R],
                    regex_constants::match_flag_type m
                    = regex_constants::match_default);
```

2 *Effects:* The first constructor initializes the member `subs` to hold the single value `submatch`. The second constructor initializes the member `subs` to hold a copy of the argument `submatches`. The third constructor initializes the member `subs` to hold a copy of the sequence of integer values pointed to by the iterator range `[&submatches, &submatches + R]`.

3 Each constructor then sets `N` to 0, and `position` to `position_iterator(a, b, re, f)`. If `position` is not an end-of-sequence iterator the constructor sets `result` to the address of the current match. Otherwise if any of the values stored in `subs` is equal to -1 the constructor sets `*this` to a suffix iterator that points to the range `[a, b)`, otherwise the constructor sets `*this` to an end-of-sequence iterator.

7.12.2.2 regex_token_iterator comparisons

[tr.re.tokiter.comp]

```
bool operator==(const regex_token_iterator& right);
```

1 *Returns:* true if `*this` and `right` are both end-of-sequence iterators, or if `*this` and `right` are both suffix iterators and `suffix == right.suffix`; otherwise returns false if `*this` or `right` is an end-of-sequence iterator or a suffix iterator. Otherwise returns true if `position == right.position`, `N == right.N`, and `subs == right.subs`. Otherwise returns false.

```
bool operator!=(const regex_token_iterator& right);
```

2 *Returns:* !(`*this == right`).

7.12.2.3 regex_token_iterator dereference

[tr.re.tokiter.deref]

```
const value_type& operator*();
```

1 *Returns:* `*result`.

```
const value_type* operator->();
```

2 *Returns:* result.

7.12.2.4 regex_token_iterator increment

[tr.re.tokiter.incr]

```
regex_token_iterator& operator++();
```

- 1 *Effects:* Constructs a local variable prev of type position_iterator and initializes it with the value of position.
- 2 If *this is a suffix iterator, sets *this to an end-of-sequence iterator.
- 3 Otherwise, if N + 1 < subs.size(), increments N and sets result to the address of the current match.
- 4 Otherwise, sets N to 0 and increments position. If position is not an end-of-sequence iterator the operator sets result to the address of the current match.
- 5 Otherwise, if any of the values stored in subs is equal to -1 and prev.suffix().length() is not 0 the operator sets *this to a suffix iterator that points to the range [prev.suffix().first, prev.suffix().second].
- 6 Otherwise, sets *this to an end-of-sequence iterator.

Returns: *this

```
regex_token_iterator& operator++(int);
```

- 7 *Effects:* Constructs a copy tmp of *this, then calls ++(*this).

8 *Returns:* tmp.

7.13 Modified ECMAScript regular expression grammar

[tr.re.grammar]

- 1 The regular expression grammar recognized by class template basic_regex is that specified by ECMA-262 [7], except as specified below.
- 2 Objects of type specialization of basic_regex store within themselves a default-constructed instance of their traits template parameter, henceforth referred to as traits_inst. This traits_inst object is used to support localization of the regular expression; basic_regex object member functions shall not call any locale dependent C or C++ API, including the formatted string input functions. Instead they shall call the appropriate traits member function to achieve the required effect.
- 3 The following productions within the ECMAScript grammar are modified as follows:

```
CharacterClass ::  
  [ [lookahead ≠ {^}] ClassRanges ]  
  [ ^ ClassRanges ]  
  
ClassAtom ::  
  -  
  ClassAtomNoDash  
  ClassAtomExClass  
  ClassAtomCollatingElement  
  ClassAtomEquivalence
```

- 4 The following new productions are then added:

```

ClassAtomExClass ::          ::= 
  [: ClassName :]

ClassAtomCollatingElement :: ::= 
  [. ClassName .]

ClassAtomEquivalence ::      ::= 
  [= ClassName =]

ClassName ::                  ::= 
  ClassNameCharacter
  ClassNameCharacter ClassName

ClassNameCharacter ::         ::= 
  SourceCharacter but not one of "." "=" ":"
```

- 5 The productions `ClassAtomExClass`, `ClassAtomCollatingElement` and `ClassAtomEquivalence` provide the equivalent functionality to the same features in POSIX regular expressions [11].
- 6 The regular expression grammar may be modified by any `regex_constants::syntax_option_type` flags specified when constructing an object of type specialization of `basic_regex` according to the rules in table 16.
- 7 A `ClassName` production when used in `ClassAtomExClass` is not valid if the value returned by `traits_inst.lookup_classname` for that name is zero. The names recognized as valid `ClassNames` are determined by the type of the traits class, but at least the following names shall be recognized: `alnum`, `alpha`, `blank`, `cntrl`, `digit`, `graph`, `lower`, `print`, `punct`, `space`, `upper`, `xdigit`, `d`, `s`, `w`. In addition the following expressions shall be equivalent:

```

\d and [:digit:]
\n and [:space:]
\w and [:alnum:]
```

- 8 The results from multiple calls to `traits_inst.lookup_classname` can be bitwise OR'ed together and subsequently passed to `traits_inst.isctype`.
- 9 A `ClassName` production when used in a `ClassAtomCollatingElement` production is not valid if the value returned by `traits_inst.lookup_collatename` for that name is an empty string.
- 10 A `ClassName` production when used in a `ClassAtomEquivalence` production is not valid if the value returned by `traits_inst.lookup_collatename` for that name is an empty string or if the value returned by `traits_inst.transform_primary` for the result of the call to `traits_inst.lookup_collatename` is an empty string.

- 11 When the sequence of characters being transformed to a finite state machine contains an invalid class name the translator shall throw an exception object of type `regex_error`.
- 12 If the *CV* of a *UnicodeEscapeSequence* is greater than the largest value that can be held in an object of type `charT` the translator shall throw an exception object of type `regex_error`. [Note: this means that values of the form "uxxxx" that do not fit in a character are invalid. —end note]
- 13 Where the regular expression grammar requires the conversion of a sequence of characters to an integral value, this is accomplished by calling `traits_inst.value`.
- 14 The behavior of the internal finite state machine representation when used to match a sequence of characters is as described in ECMAScript [7]. The behavior is modified according to any `match_flag_type` flags 7.5.2 specified when using the regular expression object in one of the regular expression algorithms 7.11. The behavior is also localized by interaction with the traits class template parameter as follows:
 - During matching of a regular expression finite state machine against a sequence of characters, two characters `c` and `d` are compared using the following rules:
 1. if (`flags() & regex_constants::icase`) the two characters are equal if `traits_inst.translate_nocase(c) == traits_inst.translate_nocase(d)`;
 2. otherwise, if `flags() & regex_constants::collate`) the two characters are equal if `traits_inst.translate(c) == traits_inst.translate(d)`;
 3. otherwise, the two characters are equal if `c == d`.
 - During matching of a regular expression finite state machine against a sequence of characters, comparison of a collating element range `c1-c2` against a character `c` is conducted as follows: if `flags() & regex_constants::collate` is false then the character `c` is matched if `c1 <= c && c <= c2`, otherwise `c` is matched in accordance with the following algorithm:

```

string_type str1 = string_type(1,
    flags() & icase ? traits_inst.translate_nocase(c1)
                      : traits_inst.translate(c1);
string_type str2 = string_type(1,
    flags() & icase ? traits_inst.translate_nocase(c2)
                      : traits_inst.translate(c2);
string_type str = string_type(1,
    flags() & icase ? traits_inst.translate_nocase(c)
                      : traits_inst.translate(c));
return traits_inst.transform(str1.begin(), str1.end())
    <= traits_inst.transform(str.begin(), str.end())
    && traits_inst.transform(str.begin(), str.end())
    <= traits_inst.transform(str2.begin(), str2.end());
  
```

- During matching of a regular expression finite state machine against a sequence of characters, testing whether a collating element is a member of a primary equivalence class is conducted by first converting the collating element and the equivalence class to sort keys using `traits::transform_primary`, and then comparing the sort keys for equality.
- During matching of a regular expression finite state machine against a sequence of characters, a character `c` is a member of a character class designated by an iterator range [`first, last`] if `traits_inst.isctype(c,`

`traits_inst.lookup_classname(first, last)`) is true.

8 C compatibility

[tr.c99]

- 1 This clause describes additions designed to bring the Standard C++ library in closer agreement with the library described in ISO/IEC 9899:1999 Standard C, as corrected through 2003 (hereafter C99, for short).
- 2 To avoid the need for language changes:
 - 1 Any use of the type `long long` in C99 is replaced in this clause by the type `_Longlong`, which behaves like a signed integer type that occupies at least 64 bits. Any header containing a declaration that uses `_Longlong` shall provide an idempotent definition of `_Longlong`.
 - 2 Any use of the type `unsigned long long` in C99 is replaced in this clause by the type `_ULonglong`, which behaves like an unsigned integer type with the same number of bits as `_Longlong`. Any header containing a declaration that uses `_ULonglong` shall provide an idempotent definition of `_ULonglong`.
 - 3 Any use of the type qualifier `restrict` in C99 shall be omitted in this clause.

8.1 Additions to header <complex>

[tr.c99.complx]

8.1.1 Synopsis

[tr.c99.complx.syn]

```
namespace std {
    namespace tr1 {
        template<class T>
            complex<T> acos(complex<T>& x);
        template<class T>
            complex<T> asin(complex<T>& x);
        template<class T>
            complex<T> atan(complex<T>& x);

        template<class T>
            complex<T> acosh(complex<T>& x);
        template<class T>
            complex<T> asinh(complex<T>& x);
        template<class T>
            complex<T> atanh(complex<T>& x);
        template<class T>
            complex<T> fabs(complex<T>& x);
    }
}
```

8.1.2 Function acos

[tr.c99.complx.acos]

- 1 *Effects:* Behaves the same as C99 function `cacos`, defined in subclause 7.3.5.1.

8.1.3 Function asin

[tr.c99.complx.asin]

- 1 *Effects:* Behaves the same as C99 function `casin`, defined in subclause 7.3.5.2.

8.1.4 Function atan

[tr.c99.complx.atan]

- 1 *Effects:* Behaves the same as C99 function `catan`, defined in subclause 7.3.5.3.

8.1.5 Function acosh

[tr.c99.complx.acosh]

- 1 *Effects:* Behaves the same as C99 function `cacosh`, defined in subclause 7.3.6.1.

8.1.6 Function asinh

[tr.c99.complx.asinh]

- 1 *Effects:* Behaves the same as C99 function `casinh`, defined in subclause 7.3.6.2.

8.1.7 Function atanh

[tr.c99.complx.atanh]

- 1 *Effects:* Behaves the same as C99 function `catanh`, defined in subclause 7.3.6.3.

8.1.8 Function fabs

[tr.c99.complxfabs]

- 1 *Effects:* Behaves the same as C99 function `cabs`, defined in subclause 7.3.8.1.

8.1.9 Additional Overloads

[tr.c99.complx.over]

- 1 The following function templates shall have additional overloads:

```
arg
conj
imag
norm
polar
real
```

- 2 The additional overloads shall be sufficient to ensure:

1. If the argument has type `long double`, then it is effectively cast to `complex<long double>`.
2. Otherwise, if the argument has type `double` or an integer type, then it is effectively cast to `complex<double>`.
3. Otherwise, if the argument has type `float`, then it is effectively cast to `complex<float>`.

- 3 Function template `pow` shall have additional overloads sufficient to ensure, for a call with at least one argument of type `complex<T>`:
1. If either argument has type `complex<long double>` or type `long double`, then both arguments are effectively cast to `complex<long double>`.
 2. Otherwise, if either argument has type `complex<double>`, `double`, or an integer type, then both arguments are effectively cast to `complex<double>`.
 3. Otherwise, if either argument has type `complex<float>` or `float`, then both arguments are effectively cast to `complex<float>`.

8.2 Header <ccomplex>

[tr.c99.cmplx]

- 1 The header behaves as if it simply includes the header `<complex>`.

8.3 Header <complex.h>

[tr.c99.cmplxh]

- 1 The header behaves as if it includes the header `<ccomplex>`, and provides sufficient *using* declarations to declare in the global namespace all function and type names declared or defined in the header `<complex>`.

8.4 Additions to header <cctype>

[tr.c99.cctype]

8.4.1 Synopsis

[tr.c99.cctype.syn]

```
namespace std {
    namespace tr1 {
        int isblank(int ch);
    }
}
```

8.4.2 Function isblank

[tr.c99.cctype.blank]

- 1 Function `isblank` behaves the same as C99 function `isblank`, defined in subclause 7.4.1.3.

8.5 Additions to header <cctype.h>

[tr.c99.ctypeh]

- 1 The header behaves as if it includes the header `<cctype>`, and provides sufficient additional *using* declarations to declare in the global namespace the additional function name declared in the header `<cctype>`.

8.6 Header <cfenv>

[tr.c99.cfenv]

8.6.1 Synopsis

[tr.c99.cfenv.syn]

```
namespace std {
    namespace tr1 {
        // types
        typedef <object type> fenv_t;
        typedef <integer type> fexcept_t;

        // functions
        int feclearexcept(int except);
        int fegetexceptflag(fexcept_t *pflag, int except);
```

```

int feraiseexcept(int except);
int fetestexceptflag(const fexcept_t *pflag, int except);
int fetestexcept(int except);

int fegetround(void);
int fesetround(int mode);

int fegetenv(fenv_t *penv);
int feholdexcept(fenv_t *penv);
int fesetenv(const fenv_t *penv);
int feupdateenv(const fenv_t *penv);
    }
}

```

- 1 The header also defines the macros:

```

FE_ALL_EXCEPT
FE_DIVBYZERO
FE_INEXACT
FE_INVALID
FE_OVERFLOW
FE_UNDERFLOW

FE_DOWNWARD
FE_TONEAREST
FE_TOWARDZERO
FE_UPWARD

FE_DFL_ENV

```

8.6.2 Definitions

[tr.c99.cfenv.def]

- 1 The header defines all functions, types, and macros the same as C99 subclause 7.6.

8.7 Header <fenv.h>

[tr.c99.fenv]

- 1 The header behaves as if it includes the header <cfenv>, and provides sufficient *using* declarations to declare in the global namespace all function and type names declared or defined in the header <cfenv>.

8.8 Additions to header <cfloat>

[tr.c99.cfloat]

- 1 The header defines the macros:

```

DECIMAL_DIG
FLT_EVAL_METHOD

```

the same as C99 subclause 5.2.4.2.2.

8.9 Additions to header <float.h>

[tr.c99.float]

- 1 The header behaves as if it defines the additional macros defined in <cfloat> by including the header <cfloat>.

8.10 Additions to header <iostream>

[tr.c99.ios]

8.10.1 Synopsis

[tr.c99.ios.syn]

```
namespace std {
    namespace tr1 {
        ios_base& hexfloat(ios_base& str);
    }
}
```

8.10.2 Function hexfloat

[tr.c99.ios.hex]

```
ios_base& hexfloat(ios_base& str);
```

- 1 *Effects:* Calls str.setf(ios_base::fixed ios_base::scientific, ios_base::floatfield).

- 2 *Returns:* str.

- 3 [Note: adding the format flag hexfloat to class ios_base cannot be done without invading namespace std, so only the named manipulator is provided. Note also that the more obvious use of ios_base::hex to specify hexadecimal floating-point format would change the meaning of existing well defined programs. C++2003 gives no meaning to the combination of fixed and scientific. —end note]

8.11 Header <cinttypes>

[tr.c99.cinttypes]

8.11.1 Synopsis

[tr.c99.cinttypes.syn]

```
#include <cstdint>

namespace std {
    namespace tr1 {
        // types
        typedef struct {
            intmax_t quot, rem;
        } imaxdiv_t;

        // functions
        intmax_t imaxabs(intmax_t i);
        intmax_t abs(intmax_t i);

        imaxdiv_t imaxdiv(intmax_t numer, intmax_t denom);
        imaxdiv_t div(intmax_t numer, intmax_t denom);

        intmax_t strtoimax(const char * s, char **endptr, int base);
        uintmax_t strtoumax(const char *s, char **endptr, int base);
        intmax_t wcstoimax(const wchar_t *s, wchar_t **endptr, int base);
    }
}
```

```

    uintmax_t wcstoumax(const wchar_t *s, wchar_t **endptr, int base);
}
}

```

- 1 The header also defines numerous macros of the form:

```

PRI{d i o u x X}[FAST LEAST]{8 16 32 64}
PRI{d i o u x X}{MAX PTR}
SCN{d i o u x}[FAST LEAST]{8 16 32 64}
SCN{d i o u x}{MAX PTR}

```

8.11.2 Definitions

[tr.c99.cinttypes.def]

- 1 The header defines all functions, types, and macros the same as C99 subclause 7.8.

8.12 Header <inttypes.h>

[tr.c99.inttypesh]

- 1 The header behaves as if it includes the header <cinttypes>, and provides sufficient *using* declarations to declare in the global namespace all function and type names declared or defined in the header <cinttypes>.

8.13 Additions to header <climits>

[tr.c99.climits]

- 1 The header defines the macros:

```

LLONG_MIN
LLONG_MAX
ULLONG_MAX

```

the same as C99 subclause 5.2.4.2.1.

8.14 Additions to header <limits.h>

[tr.c99.limitsh]

- 1 The header behaves as if it defines the additional macros defined in <climits> by including the header <climits>.

8.15 Additions to header <locale>

[tr.c99.locale]

- 1 In subclause 22.2.2.2.2, Table 58 Floating-point conversions, after the line:

```
floatfield == ios_base::scientific %E
```

add the two lines:

```
floatfield == ios_base::fixed | ios_base::scientific && !uppercase %a
floatfield == ios_base::fixed | ios_base::scientific %A
```

- 2 [Note: the additional requirements on print and scan functions, later in this clause, ensure that the print functions generate hexadecimal floating-point fields with a %a or %A conversion specifier, and that the scan functions match hexadecimal floating-point fields with a %g conversion specifier. —end note]

8.16 Additions to header <cmath>

[tr.c99.cmath]

8.16.1 Synopsis

[tr.c99.cmath.syn]

```
namespace std {
    namespace tr1 {
        // types
    }
    typedef <floating-type> double_t;
    typedef <floating-type> float_t;

        // functions
    double acosh(double x);
    float acoshf(float x);
    long double acoshl(long double x);

    double asinh(double x);
    float asinhf(float x);
    long double asinhl(long double x);

    double atanh(double x);
    float atanhf(float x);
    long double atanhl(long double x);

    double cbrt(double x);
    float cbrtf(float x);
    long double cbrtl(long double x);

    double copysign(double x, double y);
    float copysignf(float x, float y);
    long double copysignl(long double x, long double y);

    double erf(double x);
    float erff(float x);
    long double erfl(long double x);

    double erfc(double x);
    float erfcf(float x);
    long double erfccl(long double x);

    double exp2(double x);
    float exp2f(float x);
    long double exp2l(long double x);

    double expm1(double x);
    float expm1f(float x);
    long double expmil(long double x);

    double fdim(double x, double y);
    float fdimf(float x, float y);
    long double fdiml(long double x, long double y);

    double fma(double x, double y, double z);
    float fmaf(float x, float y, float z);
    long double fmal(long double x, long double y, long double z);
```

```
double fmax(double x, double y);
float fmaxf(float x, float y);
long double fmaxl(long double x, long double y);

double fmin(double x, double y);
float fminf(float x, float y);
long double fminl(long double x, long double y);

double hypot(double x, double y);
float hypotf(float x, float y);
long double hypotl(long double x, long double y);

int ilogb(double x);
int ilogbf(float x);
int ilogbl(long double x);

double lgamma(double x);
float lgammaf(float x);
long double lgammal(long double x);

long long llrint(double x);
long long llrintf(float x);
long long llrintl(long double x);

long long llround(double x);
long long llroundf(float x);
long long llroundl(long double x);

double log1p(double x);
float log1pf(float x);
long double log1pl(long double x);

double log2(double x);
float log2f(float x);
long double log2l(long double x);

double logb(double x);
float logbf(float x);
long double logbl(long double x);

long lrint(double x);
long lrintf(float x);
long lrintl(long double x);

long lround(double x);
long lroundf(float x);
long lroundl(long double x);

double nan(const char *str);
```

```
float nanf(const char *str);
long double nanl(const char *str);

double nearbyint(double x);
float nearbyintf(float x);
long double nearbyintl(long double x);

double nextafter(double x, double y);
float nextafterf(float x, float y);
long double nextafterl(long double x, long double y);

double nexttoward(double x, long double y);
float nexttowardf(float x, long double y);
long double nexttowardl(long double x, long double y);

double remainder(double x, double y);
float remainderf(float x, float y);
long double remainderl(long double x, long double y);

double remquo(double x, double y, int *pquo);
float remquof(float x, float y, int *pquo);
long double remquol(long double x, long double y, int *pquo);

double rint(double x);
float rintf(float x);
long double rintl(long double x);

double round(double x);
float roundf(float x);
long double roundl(long double x);

double scalbln(double x, long ex);
float scalblnf(float x, long ex);
long double scalblnl(long double x, long ex);

double scalbn(double x, int ex);
float scalbnf(float x, int ex);
long double scalbnl(long double x, int ex);

double tgamma(double x);
float tgammaf(float x);
long double tgammal(long double x);

double trunc(double x);
float truncf(float x);
long double truncl(long double x);

// C99 macros defined as C++ templates
template<class T>
    bool signbit(T x);
```

```

template<class T>
    bool fpclassify(T x);
template<class T>
    bool isfinite(T x);
template<class T>
    bool isinf(T x);
template<class T>
    bool isnan(T x);
template<class T>
    bool isnormal(T x);

template<class T>
    bool isgreater(T x, T y);
template<class T>
    bool isgreaterequal(T x, T y);
template<class T>
    bool isless(T x, T y);
template<class T>
    bool islessequal(T x, T y);
template<class T>
    bool islessgreater(T x, T y);
template<class T>
    bool isunordered(T x, T y);
}

```

- 1 The header also defines the macros:

```

FP_FAST_FMA
FP_FAST_FMAF
FP_FAST_FMAL

FP_ILOGB0
FP_ILOGBNAN

FP_INFINITE
FP_NAN
FP_NORMAL
FP_SUBNORMAL
FP_ZERO

HUGE_VALF
HUGE_VALL

INFINITY
NAN

MATH_ERRNO
MATH_ERREXCEPT

```

```
math_errhandling
```

8.16.2 Definitions

[tr.c99.math.def]

- 1 The header defines all of the above (non-template) functions, types, and macros the same as C99 subclause 7.12.

8.16.3 Function template definitions

[tr.c99.math.tmpl]

- 1 The function templates:

```
template<class T>
    bool signbit(T x);

template<class T>
    bool fpclassify(T x);
template<class T>
    bool isfinite(T x);
template<class T>
    bool isinf(T x);
template<class T>
    bool isnan(T x);
template<class T>
    bool isnormal(T x);

template<class T>
    bool isgreater(T x);
template<class T>
    bool isgreaterequal(T x);
template<class T>
    bool isless(T x);
template<class T>
    bool islessequal(T x);
template<class T>
    bool islessgreater(T x);
template<class T>
    bool isunordered(T x);
```

behave the same as C99 macros with corresponding names defined in C99 subclause 7.12.3 Classification macros and C99 subclause 7.12.14 Comparison macros.

8.16.4 Additional overloads

[tr.c99.math.over]

- 1 The following functions shall have additional overloads:

```
acos
acosh
asin
asinh
atan
atan2
atanh
cbrt
```

```
ceil
copysign
cos
cosh
erf
erfc
exp
exp2
expm1
fabs
fdim
floor
fma
fmax
fmin
fmod
frexp
hypot
log
ilogb
ldexp
lgamma
llrint
llround
log10
log1p
logb
lrint
lround
nearbyint
nextafter
nexttoward
pow
remainder
remquo
rint
round
scalbln
scalbn
sin
sinh
sqrt
tan
tanh
tgamma
trunc
```

- 2 Each of the above functions shall have an overload with all parameters of type `double` replaced with `long double`. If the return type of the above function is type `double`, the return type of the overload shall be `long double`.

- 3 Each of the above functions shall also have an overload with all parameters of type `double` replaced with `float`. If the return type of the above function is type `double`, the return type of the overload shall be `float`.
- 4 Moreover, there shall be additional overloads sufficient to ensure:
 1. If any argument corresponding to a `double` parameter has type `long double`, then all arguments corresponding to `double` parameters are effectively cast to `long double`.
 2. Otherwise, if any argument corresponding to a `double` parameter has type `double` or an integer type, then all arguments corresponding to `double` parameters are effectively cast to `double`.
 3. Otherwise, all arguments corresponding to `double` parameters are effectively cast to `float`.

8.17 Additions to header <math.h>

[tr.c99.mathh]

- 1 The header behaves as if it includes the header <cmath>, and provides sufficient additional *using* declarations to declare in the global namespace all the additional template function, function, and type names declared or defined in the header <cmath>.

8.18 Additions to header <cstdarg>

[tr.c99.cstdarg]

- 1 Add the function macro:

```
va_copy(va_list dest, va_list src)
```

as defined in C99 subclause 7.15.1.2.

8.19 Additions to header <stdarg.h>

[tr.c99.stdargh]

- 1 The header behaves as if it defines the additional macro defined in <cstdarg> by including the header <cstdarg>.

8.20 The header <cstdbool>

[tr.c99.cbool]

- 1 The header simply defines the macro:

```
--bool_true_false_are_defined
```

as defined in C99 subclause 7.16.

8.21 The header <stdbool.h>

[tr.c99.boolh]

- 1 The header behaves as if it defines the additional macro defined in <cstdbool> by including the header <cstdbool>.

8.22 The header <cstdint>

[tr.c99.cstdint]

8.22.1 Synopsis

[tr.c99.cstdint.syn]

```
namespace std {
    namespace tr1 {
        typedef <signed integer type> int8_t;      // optional
        typedef <signed integer type> int16_t;     // optional
        typedef <signed integer type> int32_t;     // optional
        typedef <signed integer type> int64_t;     // optional
```

```

typedef <signed integer type> int_fast8_t;
typedef <signed integer type> int_fast16_t;
typedef <signed integer type> int_fast32_t;
typedef <signed integer type> int_fast64_t;

typedef <signed integer type> int_least8_t;
typedef <signed integer type> int_least16_t;
typedef <signed integer type> int_least32_t;
typedef <signed integer type> int_least64_t;

typedef <signed integer type> intmax_t;
typedef <signed integer type> intptr_t;

typedef <unsigned integer type> uint8_t;           // optional
typedef <unsigned integer type> uint16_t;          // optional
typedef <unsigned integer type> uint32_t;          // optional
typedef <unsigned integer type> uint64_t;          // optional

typedef <unsigned integer type> uint_fast8_t;
typedef <unsigned integer type> uint_fast16_t;
typedef <unsigned integer type> uint_fast32_t;
typedef <unsigned integer type> uint_fast64_t;

typedef <unsigned integer type> uint_least8_t;
typedef <unsigned integer type> uint_least16_t;
typedef <unsigned integer type> uint_least32_t;
typedef <unsigned integer type> uint_least64_t;

typedef <unsigned integer type> uintmax_t;
typedef <unsigned integer type> uintptr_t;
}

}

```

- 1 The header also defines numerous macros of the form:

```

INT[FAST LEAST]{8 16 32 64}_MIN
[U] INT[FAST LEAST]{8 16 32 64}_MAX
INT{MAX PTR}_MIN
[U] INT{MAX PTR}_MAX
{PTRDIFF SIG_ATOMIC WCHAR WINT}{_MAX _MIN}
SIZE_MAX

```

plus function macros of the form:

```
[U] INT{8 16 32 64 MAX}_C
```

8.22.2 Definitions

[tr.c99cstdint.def]

- 1 The header defines all functions, types, and macros the same as C99 subclause 7.18.

8.23 The header <stdint.h>

[tr.c99stdint]

- 1 The header behaves as if it includes the header <cstdint>, and provides sufficient *using* declarations to declare in the global namespace all type names defined in the header <cstdint>.

8.24 Additions to header <cstdio>

[tr.c99cstdio]

8.24.1 Synopsis

[tr.c99cstdio.syn]

```
namespace std {
    namespace tr1 {
        int snprintf(char *s, size_t n, const char *format, ...);
        int vsnprintf(char *s, size_t n, const char *format, va_list ap);

        int vfscanf(FILE *stream, const char *format, va_list ap);
        int vscanf(const char *format, va_list ap);
        int vsscanf(const char *s, const char *format, va_list ap);
    }
}
```

8.24.2 Definitions

[tr.c99cstdio.def]

- 1 The header defines all added functions the same as C99 subclause 7.19.

8.24.3 Additional format specifiers

[tr.c99cstdio.spec]

- 1 The formatted output functions shall support the additional conversion specifications specified in C99 subclause 7.19.6.1.
- 2 The formatted input functions shall support the additional conversion specifications specified in C99 subclause 7.19.6.2.
- 3 [Note: These include the conversion specifiers a (for hexadecimal floating-point) and F, and the conversion qualifiers hh, h, ll, t, and z (for various integer types). They also include the ability to match and generate various text forms of infinity and NaN values. —end note]

8.24.4 Additions to header <stdio.h>

[tr.c99stdioh]

- 1 The header behaves as if it includes the header <cstdio>, and provides sufficient additional *using* declarations to declare in the global namespace all added function names defined in the header <cstdio>.

8.25 Additions to header <cstdlib>

[tr.c99cstdlib]

8.25.1 Synopsis

[tr.c99cstdlib.syn]

```
namespace std {
    namespace tr1 {
        // types
    }
    typedef struct {
        _Longlong quot, rem;
    } lldiv_t;
```

```

// functions
_Longlong llabs(long long i);
lldiv_t lldiv(_Longlong numer, _Longlong denom);

_Longlong atol(const char *s);
_Longlong strtoll(const char *s, char **endptr, int base);
_ULonglong strtoull(const char *s, char **endptr, int base);

float strtodf(const char *s, char **endptr);
long double strtold(const char *s, char **endptr);

// overloads
_Longlong abs(_Longlong i);
lldiv_t div(_Longlong numer, _Longlong denom);
}
}

```

8.25.2 Definitions

[tr.c99.cstdlib.def]

- 1 The header defines all added types and functions, other than the overloads of `abs` and `div`, the same as C99 subclause 7.20.

8.25.3 Function `abs`

[tr.c99.cstdlib.abs]

```
_Longlong abs(_Longlong i);
```

- 1 *Effects:* Behaves the same as C99 function `llabs`, defined in subclause 7.20.6.1.

8.25.4 Function `div`

[tr.c99.cstdlib.div]

```
lldiv_t div(_Longlong numer, _Longlong denom);
```

- 1 *Effects:* Behaves the same as C99 function `lldiv`, defined in subclause 7.20.6.2.

8.26 Additions to header <stdlib.h>

[tr.c99.stdlibh]

- 1 The header behaves as if it includes the header <cstdlib>, and provides sufficient additional *using* declarations to declare in the global namespace all added type and function names defined in the header <cstdlib>.

8.27 Header <ctgmath>

[tr.c99.ctgmath]

- 1 The header simply includes the headers <ccomplex> and <cmath>.
- 2 [Note: the overloads provided in C99 by magic macros are already provided in <ccomplex> and <cmath> by "sufficient"

additional overloads. —*end note*]

8.28 Header <tgmath.h>

[tr.c99.tgmathh]

- 1 The header effectively includes the headers <complex.h> and <math.h>.

8.29 Additions to header <ctime>

[tr.c99.ctime]

- 1 The function `strftime` shall support the additional conversion specifiers and modifiers specified in C99 subclause 7.23.3.4.
- 2 [Note: These include the conversion specifiers C, D, e, F, g, G, h, r, R, t, T, u, V, and z, and the modifiers E and O. —*end note*]

8.30 Additions to header <cwchar>

[tr.c99.cwchar]

8.30.1 Synopsis

[tr.c99.cwchar.syn]

```
namespace std {
    namespace tr1 {
        float wcstof(const wchar_t *nptr, wchar_t **endptr);
        long double wcstold(const wchar_t *nptr, wchar_t **endptr);
        _Longlong wcstoll(const wchar_t *nptr, wchar_t **endptr, int base);
        _ULonglong wcstoull(const wchar_t *nptr, wchar_t **endptr, int base);

        int vfwscanf(FILE *stream, const wchar_t *format, va_list arg);
        int vswscanf(const wchar_t *s, const wchar_t *format, va_list arg);
        int vwscanf(const wchar_t *format, va_list arg);
    }
}
```

- 1 Moreover, the function `wcsftime` shall support the additional conversion specifiers and modifiers specified in C99 subclause 7.23.3.4.

8.30.2 Definitions

[tr.c99.cwchar.def]

- 1 The header defines all added functions the same as C99 subclause 7.24.

8.30.3 Additional wide format specifiers

[tr.c99.cwchar.spec]

- 1 The formatted wide output functions shall support the additional conversion specifications specified in C99 subclause 7.24.2.1.
- 2 The formatted wide input functions shall support the additional conversion specifications specified in C99 subclause 7.24.2.2.
- 3 [Note: These are essentially the same extensions as for the header <cstdio>. —*end note*]

8.31 Additions to header <wchar.h>

[tr.c99.wcharh]

- 1 The header behaves as if it includes the header <cwchar>, and provides sufficient additional *using* declarations to declare

in the global namespace all added function names defined in the header <cwchar>.

8.32 Additions to header <cwctype>

[tr.c99.cwctype]

8.32.1 Synopsis

[tr.c99.cwctype.syn]

```
namespace std {
    namespace tr1 {
        int iswblank(wint_t ch);
    }
}
```

8.32.2 Function iswblank

[tr.c99.cwctype.iswblank]

- 1 Function `iswblank` behaves the same as C99 function `iswblank`, defined in subclause 7.25.2.1.3.

8.33 Additions to header <wctype.h>

[tr.c99.wctypeh]

- 1 The header behaves as if it includes the header <cwctype>, and provides sufficient additional *using* declarations to declare in the global namespace the additional function name declared in the header <cwctype>.

Annex A Implementation quantities [tr.limits]

- 1 The maximum number of arguments that can be forwarded by `reference_wrapper` (clause 2.1.2) is implementation defined. This limit should be at least 10.
- 2 The member function adapter `mem_fn` (clause 3.3) is passed a pointer to a member function that takes n arguments. The maximum value of n is implementation defined.
- 3 The number of placeholder types in namespace `tr1::placeholders`, and the maximum number of arguments that can be passed to a bind function object (clause 3.4), are implementation defined. Recommended minimum values are:
 - Number of placeholder types in namespace `tr1::placeholders` — 9.
 - Number of arguments that can be passed to a bind function object — 10.
- 4 N_{\max} , the maximum number of function call arguments supported by class template `function` (clause 3.5), is implementation defined. Implementations are encouraged to support at least 10 arguments.
- 5 The maximum number of elements in one tuple type (clause 6.1) is implementation defined. This limit should be at least 10.

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